

## ATARI BASIC

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## To the Reader

With the advent of integrated circuits and miniaturization in electronics, suddenly a complete computer, with all the peripherals or attachments needed to use it, can be purchased for as little as $\$ 600$. Now a computer for your home, club, school or business is in the same price range as the less expensive stereo component systems! These inexpensive computers, among them the ATARI computers, use the computer language BASIC. This book will teach you how to write programs using the BASIC language, specifically for ATARI computers.

BASIC was originally developed at Dartmouth College by John Kemeny and Thomas Kurtz who recognized the need for an all-purpose computer language that would be suitable for beginning programmers whose educational backgrounds would be varied and diverse. Beginners All-purpose Symbolic Instruction Code (BASIC) was originally designed as a simple language which could be learned in a few short hours. With improvements over the years, the language now may take a few days to learn, but you will find that you can do nearly anything you want in BASIC.

If you do have an ATARI computer to use, be certain that BASIC is installed in the computer's memory, so it will understand instructions given in BASIC. It is the nature of progress to find ways of improving on things, and BASIC is no exception, so you may find that your BASIC has some extra statements and refinements that were not in the 8K ATARI BASIC we used in writing this book. So we encourage you to experiment and, if you get stuck, consult your reference manual. If that doesn't do it, call ATARI or write the authors, and you'll find people to point you in the right directions.

Also, notice that there is an appendix of functions. By Chapter 3 or 4, you should begin browsing the function appendix and your reference manual to enhance your understanding of the capabilities of your computer. Learn how to save (CSAVE) your programs on the cassette recorder, if you purchased a system that included one or opted to include one on your computer system. As you progress to writing longer programs that are developed and modified, having an early version on tape saves tedious typing time.

And notice the ERROR message appendix. Believe us, you'll refer to it as often as we have for clues as to what we typed wrong, or where our logic temporarily foiled us. There is a saying among programming afficionados: 'Keep on hackin'.' So give it another try.

Now take a look at How to Use This Book, and then go on to learn BASIC!

## How to Use this Book

With this book's self-instructional format, you'll be actively involved in learning BASIC for the ATARI computer. The material is presented in short numbered sections called frames, each of which teaches you something new about ATARI BASIC and gives you a question or asks you to write a program. Correct answers are given following the dashed line. For the most effective learning we urge you to use a thick paper to keep the answers out of sight until you have written your answer.

You will learn best if you actually write out the answers and try the programs out on the ATARI computer. The questions are carefully designed to call your attention to important points in the examples and explanations, and to help you learn to apply what is being explained or demonstrated.

Each chapter begins with a list of objectives-what you will be able to do after completing that chapter. If you have had some previous experience using BASIC and the objectives for that chapter look familiar, take the Self-Test at the end of that chapter first to see where you should start your close reading of the book. If you do well, study only the frames indicated for the questions you missed. If you miss many questions, start work at the beginning of the chapter.

The Self-Test can also be used as a review of the material covered in the chapter. You may test yourself immediately after reading the chapter. Or you may wish to read a chapter, take a break, and save the Self-Test as a review before you begin the next chapter. At the end of the book is a Final Self-Test which will allow you to test your overall understanding of ATARI BASIC.

This is a self-contained book for learning ATARI BASIC, but what you learn will be theoretical until you actually sit down at a computer terminal and apply your knowledge of the computer language and programming techniques. So we strongly recommend that you and this book get together with an ATARI computer. BASIC will be easier and clearer if you have even occasional access to a computer so that you can try the examples and exercises, make your own modifications, and invent your own programs for your own purposes. You are now ready to teach yourself how to use ATARI BASIC.

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## ATARI BASIC

## CHAPTER ONE

## Your ATARI Personal Computer

This chapter will introduce you to the ATARI 400 and the ATARI 800 Personal Computers for home, school, club, or business use. When you complete this chapter, you will have a thorough introduction to these two computers and the expansion components which are currently available for them. You will also be able to use the following words and phrases from the language of the computer world.

Computer language
BASIC and, specifically ATARI BASIC
CPU or Central Processing Unit
Keyboard
Screen or television screen
Printer
Program
Program recorder
ROM cartridge containing ATARI BASIC
Operating System program
ROM module
RAM memory
RAM memory module
BASIC statements
Line numbers

You may be using this book with either the ATARI 400 or the ATARI 800 personal computer system. The 400 consists of the 400 computer console with a flat-panel keyboard, your television set, and, possibly, the optional ATARI 410 program recorder. The 800 has a typewriter-like keyboard and comes with the program recorder. There are other differences between the two systems which we will note as we go along.


Before you go any farther, it would be a good idea to set up your computer so that you can use it as you read this book. Packed in the carton with your ATARI 400 or 800 you will find the Operators Manual. This pamphlet will tell you how to attach the television, turn on the power to your computer, and use the program cartridges which come with it. The Operators Manual contains a lot of information in a small space so don't feel you must read every word of it right away. But do get your computer "up and running in BASIC" if you haven't done so before, and then come back to this book.

Welcome back! Now let's get better acquainted with your ATARI computer. Of course, the most obvious feature of the computer is its keyboard:


This is your means of communicating with your ATARI computer. It is called an input device, because you can use the keyboard to put information into the computer.

1. The keyboard is the input device that will allow you to communicate with the computer in the computer language called $\qquad$ .


BASIC
2. The part of the computer's electronics that actually 'computes' is called the CPU or Central Processing Unit. It is located on a single printed circuit board under the ribbed cover at the back of the console.

Also under that ribbed cover of the console is the computer's memory bank. The first section of the memory bank contains the 8 K Operating System ROM Module or Read-Only-Memory. The ROM Module has a program, a set of instructions, which tells the computer how it is to respond to messages from the outside world. From our point of view, the ROM and its programs are part of the computer itself.
(a) The computing action takes place in the $\qquad$ .
(b) Another of the electronics that contains the Operating System is stored in ROM, which stands for $\qquad$ .
(a) CPU (Central Processing Unit)
(b) Read Only Memory
3. We mentioned the '‘ 8 K Operating System"' that helps the computer interpret our instructions to it. The " 8 K " is a way of measuring the size of computer memory. The K stands for thousands of bytes of memory. Byte is a computer term that refers to units of memory. Each memory byte can store approximately one letter, number, or other character, so 8 K can hold around 8 thousand characters.

Therefore, 16 K would indicate the capacity to store about $\qquad$ characters.

```
_ _ - - - - _ _ _ -
```

16 thousand
4. Both the 400 and the 800 have a second memory section which contains 8 K of RAM or Random $A$ ccess Memory. This is where the computer stores information that you enter through the keyboard. We often refer to RAM memory as our workspace. We can write in it or erase it with just a few keystrokes.

RAM is different from ROM, the Read Only Memory. The computer uses the ROM, but ROM is permanent in that it cannot be erased or changed by you from the keyboard.

Answer the following questions by writing RAM and/or ROM.
(a) Which can be erased? $\qquad$
(b) Which is permanent? $\qquad$
(c) Which has a size indicated by such notations as 8 K ?
(d) Which is used to store information entered from the keyboard? $\qquad$

-     -         -             -                 -                     -                         -                             - 

(a) RAM
(b) ROM
(c) RAM and ROM
(d) RAM
5. If you have an ATARI 800 you can purchase extra RAM memory modules to expand the workspace in your computer. You won't need extra memory while you are using this book, but in the future you may find you want to write longer programs which require more RAM for storage.

Make sure you have the ATARI BASIC cartridge in the cartridge slot of your computer (follow the instructions in your Operators Manual). Inserting a cartridge does for the computer what adding an extra piece of already-educated gray matter would do for your brain. It makes the memory bigger and gives it more information. This cartridge contains another preprogrammed 8K ROM; the computer instantly knows how to speak ATARI BASIC when this cartridge is in place. Now you need to learn ATARI BASIC to communicate instructions to the computer. A set of one or more instructions to the computer that tells it what to do is called a program. Your program, or instructions, must be entered or typed in to the computer in BASIC, following the rules for BASIC you will learn in this book. Your instructions to make the computer do what you want it to do, and following the rules of BASIC, is called a $\qquad$ .
6. Let's pretend you are typing a program into the computer. As soon as the computer receives a character from the keyboard (as you begin typing) it displays that same character on the television screen, thus providing us with a record of what we have typed.

Therefore, the television screen is an output device, for it takes what you put in, and puts it back out again. This allows you to make sure that you did, indeed, enter what you thought you did. Later, when the computer follows the instructions in your programs, the results are also displayed on the screen. This is another example of the TV as an $\qquad$ device.

-     -         -             -                 -                     -                         -                             -                                 - 

output
7. Look at the photo of the ATARI 400 computer connected to a television on page 2.
(a) We use the keyboard to type information into the computer. What happens to the information that we type?
(b) How does the computer communicate with us, the users?

-     -         -             -                 -                     -                         -                             -                                 -                                     - 

(a) It is sent to the computer and then printed on the screen.
(b) It prints information on the screen.
8. If you have an ATARI 800, you also have a program recorder to use with your computer. It is similar to a home cassette recorder. (You may buy the recorder to go with your 400 system if you like.)

The program recorder is a memory storage device which is separate from the computer's own electronic memory. It can be used to store or save your computer programs and information (called data) such as mailing lists, recipes, appointments, and budget or accounting figures. Once you have mastered the BASIC computer language, you will find this kind of storage device quite handy and easy to use. In addition to cassette tapes, there are other ways to store information and programs separate from the computer. All such external storage methods are convenient ways to feed or "load" programs and information you often use into the computer without taking all the time needed to type them in from a keyboard. Magnetic disks are another external storage device. However, in this book you need only the three main parts of a computer system we have discussed earlier, which are $\qquad$ .

9. Think back over frames 1 through 8 . We have described the ATARI computer. For our purposes, the important ingredients are these:
(1) The computer itself-the central processing unit with its supporting electronic circuitry hidden away inside the console.
(2) An input device-the keyboard, which we use to type information into our computer.
(3) An output device-the TV screen, which displays information typed on the keyboard and/or sent by the computer.
(4) BASIC installed in the computer, ready to go.

In this book, we will show you many programs in ATARI BASIC, and will help you learn to read, understand, and use these programs for your own enjoyment. We will concentrate on applications that we think will be of interest to users of home/school/personal computers. And so . . . for our appetizer, a computer game.

```
1\varnothing\varnothing REMARK *** THIS IS A SIMPLE COMPUTER GAME
11\varnothing LET X = INT(1\varnothing\varnothing*RND(1))+1
120 PRINT
13\varnothing PRINT "I'M THINKING OF A NUMBER FROM 1 TO 1\varnothing\varnothing." computer program.
14\varnothing PRINT "GUESS MY NUMBER!!!"
15\varnothing PRINT : PRINT "YOUR GUESS"; : INPUT G
160 IF G<X THEN PRINT "TRY A BIGGER NUMBER." : GOTO 15\varnothing
17\varnothing IF G>X THEN PRINT "TRY A SMALLER NUMBER.": GOTO 15\emptyset
18\varnothing IF G=X THEN PRINT "THAT'S IT!!! YOU GUESSED MY NUMBER." : GOTO 11\varnothing
RUN
I'M THINKING OF A NUMBER FROM 1 TO 1\varnothing\varnothing.
GUESS MY NUMBER::! 
YOUR GUESS? 50, And this is what the computer does that
TRY A BIGGER NUMBER. appears on the screen.
    The guesses are typed by the computer
YOUR GUESS? }7
TRY A SMALLER NUMBER.
YOUR GUESS? }6
TRY A SMALLER NUMBER.
YOUR GUESS? }5
TRY A BIGGER NUMBER.
YOUR GUESS?.62
TRY A SMALLER NUMBER.
YOUR GUESS? 6\varnothing
TRY A BIGGER NUMBER.
user.
This part is called a RUN of the program. The computer generates a random number from 1 to 100 . The player types in guesses. After each guess, the computer types a clue to help the player make a better guess.
If this sounds confusing, read on! All will be revealed. And it won't be long before you can read and write programs like this in BASIC.
```

```
YOUR GUESS? 61
```

YOUR GUESS? 61
THAT'S IT:!: YOU GUESSED MY NUMBER.
I'M THINKING OF A NUMBER FROM 1 TO 1\varnothing\varnothing.
GUESS MY NUMBER::!
YOUR GUESS?
And so on. Chances are that the computer will have a different number this time.

```

Look again at the program shown in our computer game. The program consists of nine (9) lines, each containing one or more BASIC statements. Each line begins with a line number.

This is a line number.


In our program, each numbered line contains one or more BASIC \(\qquad\) . The numbers, 100 through 180 , are called \(\qquad\) .
- - - - - - - -
statements; line numbers
10. The program in frame 9 was typed, one line at a time, on the keyboard. As we typed it, the program was stored in the computer's memory and also displayed on the \(\qquad\) .

TV screen (or video screen)
Note: The TV screen can hold up to 24 lines. So, if the screen is filled, new information typed in will cause old information to be "scrolled up" or "pushed off" the top of the screen.
11. First, we typed in the entire program (lines 100 through 180). At the end of each line we pressed the RETURN key. This process is called "entering the program." This stored the program in the computer's memory. Then we typed RUN. This tells the computer to RUN, or carry out, the program. Computer people also say "to execute the program.' In other words, after storing the program, we then told the computer to follow the instructions (statements) of the program, or execute the program.

If there is a program in the computer's memory, then typing RUN tells the computer to .
- - - - - - - - -
carry out or execute the instructions in the program.
12. During the RUN, the computer obeyed the instructions (statements) in the program, as follows: First, the computer generated a random number from 1 to 100, inclusive (line 110). This number is an integer-a "whole" number with no fractional part.
```

11\varnothing LET X = INT(1\varnothing目RND(1))+1

```

Next, the computer typed instructions to the player (lines 120, 130, 140, and 150).
```

1ø\varnothing REMARK *** THIS IS A SIMPLE COMPUTER GAME
12\emptyset PRINT
13\varnothing PRINT "I'M THINKING OF A NUMBER FROM 1 TO 1\varnothing\varnothing."
14\varnothing PRINT "GUESS MY NUMBER!!!"'

```

Then, the computer asked for a guess (line 150).
```

15\varnothing PRINT : PRINT "YOUR GUESS"; INPUT G

```

After the player typed a guess, and pressed the RETURN key, the computer compared the guess with its secret number and gave the player the appropriate response (lines 160, 170, and 180).
```

160 IF G<X THEN PRINT "TRY A BIGGER NUMBER." : GOTO 150
170 IF G>X THEN PRINT "TRY A SMALLER NUMBER." : GOTO 15@
18\varnothing IF G=X THEN PRINT "THAT'S IT!:! YOU GUESSED MY NUMBER." : GOTO 11\varnothing

```

If the player did not guess the computer's number, the computer went back to line 150 and asked for another guess. But, if the lucky player did guess the secret number, the computer acknowledged the correct guess and went back to line 110 to "think" of another number.
```

1\varnothing\varnothing REMARK *** THIS IS A SIMPLE COMPUTER GAME

```

Oh yes, line 100 is a REMARK statement. It doesn't tell the computer to do anything. It is simply included to tell something about the program to us humans who may read the program itself.

What do we type to instruct the computer to execute or carry out a program? \(\qquad\)


Now, to see how much you've learned from this first chapter, try the SelfTest. Then on to Chapter 2 where you'll start to learn how to actually use the computer.

\section*{SELF-TEST}

Try this Self-Test, so you can evaluate how much you have learned so far.
1. What does your computer use for an output device? \(\qquad\) .
2. What do the following abbreviations stand for?
(a) CPU \(\qquad\)
(b) RAM \(\qquad\)
(c) ROM \(\qquad\)
3. Since a computer doesn't have legs, what do we want a computer to do when we tell it to RUN? \(\qquad\)

\section*{Answers to Self-Test}

The frame numbers in parentheses refer to the frames in the chapter where the topic is discussed. You may wish to refer to these for quick review.
1. A screen or television set (frame 6)
2. (a) Central Processing Unit or computer
(b) Random Access Memory or user workspace
(c) Read Only Memory (frames 2, 4)
3. Execute the program (follow the instructions we give it) (frames 11, 12)

\section*{CHAPTER TWO}

\section*{Getting Started}

To get you started in computer programming in BASIC, we will now introduce you to some of the statements used to instruct the computer, that is, to tell it what you want accomplished. In this chapter, you will use the direct, or immediate, mode of operation. Using direct mode, you tell the computer something to do, and it does it immediately. When you complete this chapter, you will be able to:
- use direct statements to instruct the computer;
- recognize error messages from the computer;
- use the PRINT statement with quotation marks to print strings (messages);
- correct typing errors or delete a statement with errors;
- use direct statements to do arithmetic;
- compute values of simple mathematical expressions using the symbols and rules of BASIC for arithmetic;
- recognize and convert floating point or E notation to ordinary numbers.
1. Now we begin 'talking'' with the computer. We assume that your ATARI computer system is set up and ready to go, with the BASIC language cartridge inserted in the language cartridge slot. You can find directions on how to do this in the Operators Manual for your computer. If you own an ATARI 400, you will consult the very friendly and helpful ATARI \(400^{\text {TM }}\) OPERATORS MANUAL. If you are using an ATARI 800, you will avidly peruse the ATARI \(800^{\mathrm{TM}}\) OPERATORS MANUAL. As you work through this book, you will find your ATARI OPERATORS MANUAL a constant source of know-how and inspiration!

Ready? Turn on the computer.* CLICK! The TV screen will look like this:


Your ATARI computer is ready for you to use. You know that it is ready because it typed READY and turned on the tiny rectangle called the
\(\qquad\) .
cursor
2. We will, of course, use the keyboard to communicate with the computer.


In the diagram, there is a large black arrow pointing to the key labeled
\(\qquad\) .

\footnotetext{
*Remember, we assume that you know how to hook up the various components of your ATARI system and turn it on. If not, consult your friendly ATARI OPERATORS MANUAL.
}
3. Your computer is waiting patiently for you to do something. So, try this: Type your name and press the RETURN key. The computer will probably print an error message on the screen. Here is what happened when Karl typed his name.


Then, Karl pressed the RETURN key.


Hmmm . . . Why did that happen? Well, you see, the computer is of quite limited intelligence. It simply did not understand the word, KARL.
(a) If you type something, then press RETURN, and the computer types

ERROR, what is the computer trying to tell you? \(\qquad\)
(b) After typing ERROR- KARLD, what did the computer do? \(\qquad\)
(a) It does not understand you.
(b) It turned on the cursor.

The cursor is the computer's way to let you know that everything is OK. No damage has been done. The computer is very patient and forgiving. After you make a mistake, it will display the error and then turn on the cursor to let you know it is ready for you to try again.

\footnotetext{
*By \(i t\), we mean the computer. Saves space in writing this book!
}
4. Find the SHIFT key and the CLEAR key. Press the SHIFT key and, while holding it down, press the CLEAR key. The screen will now look like this:


Except for the cursor, the screen is blank! Pressing SHIFT and CLEAR together erases the screen, leaving only the cursor in its home position.
(a) Where is the home position of the cursor? \(\qquad\)
(b) To clear the screen and home the cursor, press \(\qquad\) and \(\qquad\) , together.
(a) In the upper left corner of the screen.
(b) SHIFT; CLEAR

Another way to clear the screen and home the cursor is to press CTRL and CLEAR together. CTRL is an abbreviation for CONTROL. The CTRL key is located on the left of the keyboard, directly above the SHIFT key.
5. To avoid misunderstandings with a computer, we must learn its language. We will start with some simple, one-line statements that the computer does understand.

In this chapter we will use direct statements. Direct statements do not have line numbers. When you type a direct statement and press RETURN, the computer executes the statement immediately, then forgets the statement. We call this BASIC's direct mode of operation. Here is another example of a statement that is "executed in direct mode."

Then we press RETURN.

We type: print "my human understands me"
It types: MY HUMAN UNDERSTANDS ME

Now you complete the following.

We type: print "burglars are in the house!"


It types:
```

BURGLARS ARE IN THE HOUSE!

```

Along with the burglar message, we could also arrange (as we will see later) to have the computer sound an audible alarm. For example, it might play The Jailhouse Blues in four part harmony! Hopefully, this might remind the burglar of the possible consequences of crime and thus prevent the attempted theft. More about that later!


6．The statement PRINT＂MY HUMAN UNDERSTANDS ME＂is called a PRINT statement．It tells the computer to print something on the screen．The computer prints the verbal message following the word PRINT．Note that the message is enclosed in quotation marks．This message，enclosed in quotation marks，is called a string．


This is a string．It is enclosed in quotation marks．The quotation marks enclose the string，but are not part of the string．

A string may include：
Numerals（ \(0,1,2, \ldots\) ．
Letters（A，B，C，．．）
Special characters（ \(+,-,{ }^{*}, /, \wedge\) ，comma，period，etc．）
Since quotation marks define the beginning and the end of a string，do you think they can be used as a character in the string？


No，they cannot．（That would really confuse the computer！）However，single quotes（＇）can be used in a string．For example：

We type：Print＂they said，＇all right．＇＂
It types：they said，＇all right．＇
Complete the statement so that the computer types what we say it types．
We type：PRINT \(\qquad\)
It types：the roast is done．turn off the oven．
－ーーーーーーーーー
＂THE ROAST IS DONE．TURN OFF THE OVEN．＂

Did you remember the quotation marks？Someday，of course，the computer will turn off the oven！Almost anything electric can be controlled by the computer， with the proper electronic connections and program，of course．
7. Have you made any typing mistakes yet? In case you should make a typing error, BASIC has a dandy way of fixing it. Watch while we make a typing error.
We type: ptint "dentist appointment today"
It types: ERror - ptint 回dentist appointment today"
We misspelled PRINT, so the computer doesn't know what we want. However, if we had noticed that we hit \(T\) when we meant to hit \(R\), we could have corrected our mistake by using the DELETE BACK S key. Each time we press this key, the cursor moves back (to the left) one space and erases the character in that space.

We type
Then press DELETE BACK S
Press DELETE BACK S again
and yet again


What will happen if we press DELETE BACK S two more times? \(\qquad\)
— - - - - - - - -
The cursor will move two places to the left, erasing A and B.
8. Complete the following so that the computer prints what we want it to print.

We type: Primr ___ "tomorrow is your mother's birthday!!!"
It types: tomorrow is your mother's birthday!!!


DELETE BACK S
DELETE BACK S NT

Remember: To delete the last character typed, press DELETE BACK S. To delete two characters, press DELETE BACK S twice. And so on.
9. The DELETE BACK S key is great for deleting errors that you have just made. But, suppose you are typing a long line and are almost to the end when, alas, out of the left corner of your left eye, you spot a mistake way back at the beginning. If you complete the line and press RETURN, you will probably get an error message. You would like to just abort the line-that is, erase it from the beginning.

Well you can! Hold down the SHIFT key and press the DELETE BACK S key.

We type: primt "once upon a time there was a


The computer erases the entire line and turns on the cursor. Whenever we see the cursor, what is the computer telling us?

It is our turn to type.
10. We can also tell the computer to do arithmetic and print the answer. In other words, we can use the computer as a calculator.

We type: PRINT \(7+5\)
It types: 12
The statement PRINT \(7+5\) tells the computer to compute the value of \(7+5\) (do the arithmetic) and then print the answer.

Note that actual calculations are indicated to the computer by not using quotation marks in the PRINT statement. Compare the formats below.

We type: PRINT " \(13+6\) " We type: PRINT \(13+6\)
It types: \(13+6\)
It types: 19


This is a string. The computer prints it exactly as it appears.


This is a numerical expression (no quotation marks). The computer does the arithmetic and prints the result.

Your turn. Complete the following, showing what the computer typed.
We type: PRINT \(23+45\)
It types: \(\qquad\)
We type: PRINT \(1+2+3+4+5\)
It types: \(\qquad\)
We type: PRINT " \(1+2+3+4+5 "\)
It types: \(\qquad\)
```

-     -         -             -                 -                     -                         -                             - 

6
1 5
1+2+3+4+5

```
11. Subtraction? Of course.

We type: PRINT 7-5
It types: 2

We type: PRINT 25.68-37.95
It types: -12.27


Complete the following, showing what the computer typed.
We type: PRINT 29-13
It types: \(\qquad\)
We type: PRINT 1500-2000
It types: \(\qquad\)
We type: PRINT " 1500 - \(20 \varnothing \varnothing\) "
It types: \(\qquad\)
```

_ - - - - - _ _ -
16
-500
1500 - 2000

```
12. BASIC uses + for addition and - for subtraction, just as we do with paper and pencil. However, for multiplication, BASIC uses the asterisk (*).

We type: PRINT 7 * 5
It types: 35
We type: PRINT 1.23 * 4.567
It types: 5.61741
We type: PRINT 9 * 8
It types: \(\qquad\)
We type: PRINT 3.14 * \(2 \varnothing\)
It types: \(\qquad\)
\[
\begin{aligned}
& ------------1 \\
& 72 \\
& 62.8
\end{aligned}
\]
13. For division, use the slash (/).

We type: PRINT 7/5
It types: \(\quad 1.4\)
We type: PRINT 13/16
It types: \(\varnothing .8125\)
We type: PRINT 24/3
It types: \(\qquad\)
We type: PRINT \(3.14 / 4\)
It types: \(\qquad\)

8
ø. 785
14. The computer will print up to 9 or 10 digits as the result of an arithmetic operation. If the true result would have more digits, the printed result will be truncated (chopped) to 9 or 10 digits.

We type: PRINT 1.2345 * 6.78999
It types: 8.38224265
Complete answer is 8.382242655 which has 10 digits.

We type: PRINT 1/3
It types: ø.3333333333
Complete answer cannot be given with a finite number of digits. It goes on forever as a repeating decimal.

We type: PRINT 2/3
It types: \(\varnothing .6666666666\)
Truncated at the 10 th digit.
Suppose the complete result of an arithmetic operation is 1.234567898765 . What might the computer print? \(\qquad\)
Suppose the complete result is 3.14159265359 . What might the computer print?
```

-     -         -             -                 -                     -                         -                             -                                 - 

1.23456789 OR 1.234567898
3.14159265 OR 3.141592653

```
15. Write PRINT statements to tell the computer to evaluate each of the following numerical expressions. Also show the result printed by the computer.

Numerical expression
(a) \(10+6\)
(b) \(15-8\)
(c) \(23 \div 5\)
(d) \(3 \times 13\)

PRINT statement and result
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)
(e) \(8 \div 3\)
(f) \(120 \div 7\) \(\qquad\)
\(-\infty-\infty-\infty-\infty\)
(a) PRINT \(1 \varnothing+6\)
(b) \begin{tabular}{l}
16 \\
7 \\
7 \\
\hline
\end{tabular}
(c) PRINT \(23 / 5\)
(d) \(\begin{gathered}4.6 \\ \text { PRINT } \\ 3\end{gathered}{ }^{*} 13\)
(e) PRINT \(8 / 3\)

Truncated to nine digits
2. 6666666
(f) PRINT 120/7
17.14295714 Truncated to ten digits (We will also accept 17.1429571)
16. The computer does arithmetic in left to right order, with all multiplications (*) and/or divisions (/) performed before additions (+) and/or subtractions (-).
\[
\left.\begin{array}{l}
* \\
/
\end{array}\right\} \text { before }\left\{\begin{array}{l}
+ \\
-
\end{array}\right.
\]

Shown below are some BASIC expressions in which two or more operations are used. For some of these expressions, we have shown the value computed by the computer after it does the indicated arithmetic. You complete the rest.
\begin{tabular}{ll} 
Expression & \begin{tabular}{l} 
Value computed \\
by computer
\end{tabular} \\
\(2 * 3-4\) & 2 \\
\(2+3 * 4\) & 14 \\
\(2 * 3+4 * 5\) & - \\
\(2+3 * 4-5\) & - \\
\(2 * 3+4 * 5-6 * 7\) & - \\
------- \\
26 & \(2 * 3+4 * 5=6+20=26\) \\
9 & \(2+3 * 4-5=2+12-5=9\) \\
-16 & \(2 * 3+4 * 5-6 * 7=6+20-42=-16\)
\end{tabular}
17. Here are more examples and exercises, using division (/). Study the examples and then complete the exercises. Be sure to follow the computer's order described in frame 16.
\begin{tabular}{lll} 
Expression & \begin{tabular}{l} 
Value computed \\
by computer
\end{tabular} & \begin{tabular}{l} 
How it did the \\
arithmetic
\end{tabular} \\
\(3 / 4+5\) & 5.75 & \(3 / 4+5=.75+5=5.75\) \\
\(2-3 / 4\) & 1.25 & \(2-3 / 4=2-.75=1.25\) \\
\(2 * 3+4 / 5\) & 6.8 & \(2 * 3+4 / 5=6+.8=6.8\) \\
\(3 / 4+5 * 6\) & & \\
\(2-3 / 4+5\) & \\
-------- & \\
\(30.75 \quad 3 / 4+5 * 6=.75+30=30.75\) & \\
6.25 & \(2-3 / 4+5=2-.75+5=6.25\) &
\end{tabular}
18. Following the computer's rules, give the computed value for each of the expressions below. (Remember, do arithmetic in left to right order.)

Expression Value computed by computer
2*3/4
3/4*5
3/4/5
2*3/4+3/4*5
- - - - - - - -
1.5 Multiply 2 by 3, then divide result by 4.
3.75 Divide 3 by 4, then multiply result by 5 .
0.15 Divide 3 by 4, then divide result by 5 .
5.25 First compute \(2 * 3 / 4\), then compute \(3 / 4 * 5\), then add the two results.
19. For each of the following numerical expressions, show the order in which the computer does the arithmetic by putting numbers 1,2 , or 3 in the circles above the operation symbols. We have completed the first three for you.
(a) \(2 \stackrel{1}{+} 4-4\)
(c) \(2 \stackrel{\text { ? ? ? ? }}{2} / 4\)
(e) \(2+3 * 4-2\)
(g) \(2+3 / 4 * 2\)
(b) \(2 \stackrel{\text { 2 }}{-2} 4\)
(d) \(2 / 3 / 4\)

(f) \(2-3 * 4+1\)
(h) \(2+3 * 4\)

(d) \(2 / 314\)

(2) (1) 3
(f) \(2-3 * 4+1\)
(g) \(2+3+(4)+2\)
(2) (1)
(h) \(2+3\) * 4
20. If you want to change the order in which operations are done by the computer, use parentheses. Operations in parentheses are done first.

Starting with the leftmost inner set of parentheses, the computer does arithmetic within each set of parentheses in left to right order, with all multiplications (*) and/or divisions (/) before additions (+) and/or subtractions (-).
\[
* \text { before }\left\{\begin{array}{l}
+ \\
-
\end{array}\right.
\]

Look at these examples of how the order of operations can give different results.


Complete the following.
\begin{tabular}{ll} 
Expression & Value computed by computer \\
\((2+3) /\left(4^{*} 5\right)\) & \\
\(2+3^{*}(4+5)\) & \\
\(1 /(3+5)\) & \\
- & - \\
& \\
0.25 & \((2+3) /\left(4^{*} 5\right)=5 / 20=.25\) \\
29 & \(2+3^{*}(4+5)=2+3^{* 9}=2+27=29\) \\
0.125 & \(1 /(3+5)=1 / 8=.125\)
\end{tabular}
21. Let's take another look at the order in which arithmetic is done. In the expressions below, the numbers in the circles show the order in which the operations are carried out. Write the final value for each expression. The operations are always done in the innermost set of parentheses first.

Expression

\((3 * 4+5 * 6-7) / 8\)
-127
4.375
22. Your next task is to write a proper PRINT statement to tell the computer to compute and print the value of each expression listed below. We have shown the actual value printed by the computer. Remember to indicate all multiplication and division operations with the proper BASIC symbol.
\begin{tabular}{lll} 
Expression & PRINT statement & Result \\
\(2 \times 3+6 \div 7\) & & 6.85714285 \\
\(16(33-21)\) & \(\square\) & 192 \\
\(3.14 \times 2 \times 2\) & & 12.56 \\
\(\frac{88-52}{18+47}\) & \(--\ldots\) & 0.5538461538
\end{tabular}
```

PRINT 2*3+6/7
PRINT 16*(33-21) (Did you remember the asterisk?)
PRINT 3.14*2*2
PRINT (88-52)/(18+47)

```
23. For each numerical expression, show the order of operations by putting numbers \(1,2,3\), and so on, in the circles above the operation.
(a) \(2+(3-4)\)

(b) \(2 \underset{\sim}{\text { P }}\) ? \((3 / 4) *(2+3)\)
(c) \(2 /(3 * 4)\)
(e) \((2+3) /(4+\underset{+}{+} 1)\)
(g) \(2+((3+4)+8)\)
(b) \(2 /(3 / 4) *(2+3)\)

(d) \((2+3) * 4\)
(f) \(2 /(3+4)\)
(h) \(1+1 /(2+1 /(3+1 / 4))\)
(2)
(a) \(2+(3-4)\)
(b) (1) 2
(b) \(2 /(3 / 4) *(2+3)\)
(2) (1)
(c) \(2 /(3 * 4)\)
(d) \((2+3) * 4\)

(e) \((2+3) /(4+1)\)
(f) \(2 \stackrel{1}{\mid}(3+4)\)
(3) (1) 2
(g) \(2+((3+4)+8)\)
(h) \(1+1 /(2+1 /(3+1 / 4))\)
24. There is a fifth arithmetic symbol in BASIC, which indicates raising a number to a power. This operation is called exponentiation.
\({ }^{\wedge}\) means raise to a power
SHIFT


The volume of a cube is a good example of how exponential numbers are used.


Volume of a cube: \(V=S^{3}\), where \(S\) is the length of a side.

If \(S=5\) and \(V=5^{3}\), then
\(V=5^{3}=5 \times 5 \times 5=125\).


We press the SHIFT and \(\rightarrow_{*} \wedge\) keys together to tell the computer to raise a number to a power.
\begin{tabular}{lll} 
We type: & PRINT \(5^{\wedge} 3\) & \(\left(5^{\wedge} 3\right.\) means \(5^{3}\) or \(\left.5 \times 5 \times 5\right)\) \\
It types: & 124.99999998 & Hmmm \(\ldots\) Call it 125.
\end{tabular}

Now complete the following. Give your answers as whole numbers.
We type: PRINT \(2{ }^{\wedge} 3\)

It types:
We type: PRINT 2 ^ 4
It types:
We type: PRINT 2 ^ 5
It types:
We type: PRINT 7^2
It types:
\(\ldots-\ldots\)
8
16
\(2^{\wedge} 3=2^{3}=2 \times 2 \times 2=8\)
32
\(2^{\wedge} 4=2^{4}=2 \times 2 \times 2 \times 2=16\)
49
\(2^{\wedge} 5=2^{5}=2 \times 2 \times 2 \times 2 \times 2=32\)
\(7^{\wedge} 2=7^{2}=7 \times 7=49\)
(The computer gave 7.99999986)
(The computer gave 15.9999993 )
(The computer gave 31.99993444 )
(The computer gave 48.99999631 )
25. Write a PRINT statement to evaluate each expression. We have supplied the results.
\begin{tabular}{|c|c|c|}
\hline Expression & PRINT statement & Result \\
\hline \(3^{7}\) & & 2187 \\
\hline \(8 \times 8 \times 8 \times 8 \times 8\) & & \[
\begin{aligned}
& 32768 \\
& \left(\text { Use }^{\wedge}\right)
\end{aligned}
\] \\
\hline \(1.06{ }^{10}\) & & 1.79085 \\
\hline \(3^{2}+4^{2}\) & & 25 \\
\hline
\end{tabular}

PRINT \(3 \wedge 7\)
PRINT 8 - 5 (PRINT \(8 * 8 * 8 * 8 * 8\) will also produce the desired result.) PRINT 1.06 ^ \(1 \varnothing\)
26. Suppose we put \(\$ 123\) into a savings account that pays \(6 \%\) interest per year, compounded yearly. The amount of money in the account after N years can be computed using the compound interest formula shown below.
\(A=P(1+R / 100)^{N}\)
where:
\(\mathrm{P}=\) Principal, or original amount put into the account.
\(\mathrm{R}=\) Rate of interest per year, in percent.
\(\mathrm{N}=\) Number of years.
\(\mathrm{A}=\) Amount in account at the end of N years.
In our problem, \(\mathrm{P}=\$ 123, \mathrm{R}=6 \%\), and we want to know the value of A for \(\mathrm{N}=2, \mathrm{~N}=5\), and \(\mathrm{N}=12\) years.

We type: PRINT \(123^{*}(1+6 / 1 \varnothing \varnothing) \wedge 2\)
It types: \(138.203 \longleftrightarrow\) After 2 years

We type: PRINT 123* (1+6/19ø)^5
It types: \(164.602 \longleftarrow\) After 5 years
Your turn. Write the PRINT statement for \(\mathrm{N}=12\). We have supplied the result printed by the computer.

We type:
It types: 247.5 After 12 years our money doubled.
27. Computers use a special notation to indicate very large numbers, or very small decimal fractions. This method of representing numbers is called floating point notation. You decipher it in the same way you do the scientific notation commonly used in mathematics and science textbooks.

For example, the population of the earth is about 40 billion people.
40 billion \(=40,000,000,000\)
Now let's ask the computer to print the population of the earth.
We type: PRINT \(40 \varnothing \sigma \varnothing \sigma \varnothing \varnothing \sigma \varnothing \varnothing\)
It types:
\(4 \mathrm{E}+1 \varnothing\)

Our ATARI computer printed 40 billion as a floating point number. Read it as follows.
\[
\begin{aligned}
& 4 \mathrm{E}+10=\text { four times ten to the ninth power, or } \\
& 4 \mathrm{E}+10=4 \times 10^{10}
\end{aligned}
\]

Floating point notation is simply a shorthand way of expressing very large or very small numbers. In floating point notation, a number is represented by a mantissa and an exponent.


The mantissa and the exponent are separated by the letter \(\qquad\) .


E
NOTE: In typing numbers into the computers, we may not use commas as we normally do when writing numerals. Commas have a special use in BASIC PRINT statements. Please be patient. We will get to it soon.
28. Here are some examples showing numbers in good old everyday notation and again in floating point notation.

One trillion
ordinary notation: \(1,000,000,000,000\)
floating point notation: \(1 \mathrm{E}+12\)
Volume of the earth in bushels
ordinary notation: \(31,708,000,000,000,000,000,000\)
floating point notation: \(3.1708 \mathrm{E}+22\)

Speed of a snail in miles per second ordinary notation: . 0000079
floating point notation: 7.9E-6 (Exponent is negative.)
In each floating point number above, underline the mantissa and circle the exponent.
\(-\ldots--\ldots-\ldots-\ldots\)
\(1 \mathrm{E}+12\)
\(3.1708 \mathrm{E}+22\)
\(7.9 \mathrm{E}-6\)
29. Here are more examples, showing how the ATARI computers print floating point numbers.

We type: PRINT 123456789
It types: 12345789
We type: PRINT 12345678899
It types: \(1.23456788 \mathrm{E}+1 \varnothing\)
We type: PRINT \(1234567806 \infty\)
It types: \(1.2345678 \mathrm{E}+1 \varnothing\)
Our ATARI computer prints at most nine digits for the mantissa and chops the mantissa at the ninth digit. The mantissa is printed as a nonzero digit to the left of the decimal point and up to eight digits to the right of the decimal point.

We type: PRINT 333333333333
It types: \(\qquad\)
We type: PRINT 666666666666
It types: \(\qquad\)
- - - - - - - - -
3. \(33333333 E+11\)
\(6.66666666 \mathrm{E}+11\)
30. It works the same way with very small numbers.

We type: PRINT .øøøøøळ 1234567889
It types: 1.23456788 En Negative exponent
We type: PRINT .øøøøøø 1234567884
It types: \(1.23456788 \mathrm{E}-\sigma 7\) Negative exponent
The mantissa is printed with how many digits to the left of the decimal point? \(\qquad\) Up to how many digits to the right of the decimal point? \(\qquad\)
- - - - - - - - -
one; eight (See frames 28 and 29 for examples of mantissas with fewer than 8 digits to the right of the decimal point.)
31. Numbers printed in floating point notation can be converted to ordinary notation, as follows. When the exponent is positive, we do the following.
(a) Write the mantissa separately.
(b) Move the decimal point of the mantissa to the right the number of places specified by the exponent. If necessary, add zeros.

Example: \(6.12345678 \mathrm{E}+08\)
(a) 6.12345678
(b) 6.123456789 . (Move point 8 places.)

Therefore, \(6.12345678 \mathrm{E}+08=612,345,678\)
Example: \(4 \mathrm{E}+09\)
(a) 4 .
(b) 4.000000000 . (Move point 9 places and add 9

Therefore, \(4 \mathrm{E}+09=4,000,000,000\)
Now you try it: \(1,2345678 \mathrm{E}+13\)
(a)
(b)

Therefore, \(1.2345678 \mathrm{E}+13=\) \(\qquad\)
- - - - - - - - -
(a) 1.2345678
(b) 1.2345678000000 (Move point 13 places.)
\(12,345,678,000,000\)
32. When the exponent is negative, we simply change the direction that the decimal point moves.
(a) Write the mantissa separately.
(b) Move the decimal point of the mantissa to the left the number of places specified by the exponent. If necessary, add zeros.

Example: 7.9E-06
(a) 7.9
(b) . 000007.9 (Move point 6 places and add 5 zeros)

Therefore, \(7.9 \mathrm{E}-06=.0000079\)
Your turn. \(1.23456 \mathrm{E}-08\)
(a)
(b)

Therefore, \(1.23456 \mathrm{E}-08=\) \(\qquad\)
- - - - - - - -
(a) 1.23456
(b) . 00000001.23456
. 0000000123456
33. Write each of the following floating point numbers in ordinary notation.

Floating point notation
(a) \(1.23456 \mathrm{E}+06\)
(b) \(1.23456 \mathrm{E}-06\)
(c) \(1.23456 \mathrm{E}+07\)
(d) \(1.23456 \mathrm{E}-09\)
(e) \(1 \mathrm{E}+11\)
(f) \(1 \mathrm{E}-11\)
(a) 1234560 or \(1,234,560\)
(b) .00000123456
(c) 12345600 or \(12,345,600\)
(d) .00000000123456
(e) \(100,000,000,000\)
(f) . 00000000001
34. Write each "ordinary" number in ATARI BASIC floating point notation.

Ordinary notation
(a) \(1,234,560,000\)
(b) . 000000123456
(c) \(10,000,000,000\)
(d) .000000001
(e) 1234567888888
(f) . 000001234567888888
(g) \(6.02 \times 10^{21}\) (See note.)
(h) \(1.67 \times 10^{-11}\) (See note.)

Note: the numbers in (g) and (h) are written in scientific notation commonly used in mathematics and science.
- - - - - - - - -
(a) \(1.23456 \mathrm{E}+09\)
(b) \(1.23456 \mathrm{E}-07\)
(c) \(1 \mathrm{E}+10\)
(d) \(1 \mathrm{E}-09\)
(e) \(1.23456788 \mathrm{E}+12\) Mantissa truncated to 9 digits
(f) \(1.23456788 \mathrm{E}-06 \quad\) Mantissa truncated to 9 digits
(g) \(\quad 6.02 \mathrm{E}+21\)
(h) \(1.67 \mathrm{E}-11\)
35. Perhaps you have heard of the ancient story of the wise person who did a great service for a wealthy king. The king asked this person what reward would be appropriate. The person's request was simple. She asked only for grains of wheat, computed as follows. For the first square on a chess board, one grain of wheat; for the second square, 2 grains of wheat; for the third square, 4 grains of wheat and so on, doubling at each square. It goes on as shown below.

Square number Grains of wheat
1 \(2 \quad 2\)
\(3 \quad 4\)
\(4 \quad 8\)
\(5 \quad 16\)
\(6 \quad 32\)
\(7 \quad 64\)

And so on. For square N , there will be \(2^{\mathrm{N}-1}\) grains. Let's find out how many grains on square 16.

We type: PRINT 2 ^ 15 Since \(N=16, N-1=15\).
It types: 32768
Your turn. Write a PRINT statement to find out how many grains of wheat for square number 64.

We type: \(\qquad\)
It types: \(9.2233704 \mathrm{E}+18\) That's a lot of wheat!
```

-     -         -             -                 -                     -                         -                             - 

PRINT 2 ^ 63

```


\section*{SELF-TEST}

Try this Self-Test, so you can evaluate how much you've learned so far.
1. In this chapter, we used direct statements. Direct statements do not have line numbers. When we type a direct statement and press RETURN, what does the computer do? \(\qquad\)
\(\qquad\)
\(\qquad\)
2. Assume that you are typing a statement into the computer, and you make a typing error. How would you correct the error? \(\qquad\)
3. Write the symbols used in ATARI BASIC for the following arithmetic operations.
addition
subtraction
multiplication
division
\(\qquad\)
exponentiation
(raising a number to a power) \(\qquad\)
4. Complete the following.

We type: please do the homework on page 157
It types:
5. Complete the following.

We type: print "please do the homework on page 157"
It types:
6. Complete the following.

We type: PRINT 9*37/5+32
It types: \(\qquad\)
7. The formula to convert temperature from degrees Fahrenheit to degrees Celsius is shown below.


Write a PRINT statement to tell the computer to compute and print the degrees Celsius (value of C ) if \(\mathrm{F}=72\) degrees.
8. Complete the following.

We type: priny "the quick red fox ju
SHIFT DELETE BACK S
It types:
9. What does the following statement tell the computer to do?

PRINT \(23+45\)
10. Indicate which of the following numerical expressions are valid, as written, in BASIC.
(a) \(2 * 3 * 4 * 5\)
(b) \(7(8+9)\)
(c) \(1.23 \div 4.567\)
\(\qquad\) (d) \(3^{\wedge} 2+4^{\wedge} 2\)
_-
(e) \(\frac{1}{37-29}\)
\(\qquad\) (f) \((1+7 / 100)^{3}\)
\(\qquad\) (g) \(2^{\wedge} 2^{\wedge} 2\)
11. For each invalid numerical expression in problem 10, write a valid BASIC numerical expression.
12. For each of the following numerical expressions, show the order in which the computer does the arithmetic by putting numbers \(1,2,3\), and so on, in the circles above the operation symbols.
(a) \(2+4-4\)
(b) 2 ? 3 * 4
(c) \(2 * 3 / 4\)
(d)

(f) \(2-3 * 4\)
(e) \(2 / 3 * 4\)
(g) \(2+3 / 4\)
(i)

(h) \(2 \stackrel{\uparrow}{\uparrow} 3 * 4\)
(k) \(2 / 3 \uparrow 4\)
(m) \(1+2\) ? \(3 \stackrel{\Im}{\uparrow} 4\)
(1) \(2 \uparrow 3 \uparrow 4\)

13. For each numerical expression, show the order of operations by putting numbers \(1,2,3\), and so on, in the circles above the operation.
(a) \(2+(3-4)\)
(b) \(2 /(3 / 4)\)
(c) \(2 /(3 * 4)\)
(d) \((2-3) * 4\)
(e) \((2+3) / 4\)
(f) \(\left.2 \bigodot_{\uparrow} \bigcap_{3}^{*} 4\right)\)
(g) \(2 \stackrel{\uparrow}{\uparrow}(3 \stackrel{\uparrow}{\uparrow} 4)\)
(h) \(1+1+(2+1 /(3+1 / 4))\)
14. Write each of the following floating point numbers in ordinary notation.

Floating point notation
(a) \(1.23456 \mathrm{E}+05\)
(b) \(1.23456 \mathrm{E}-05\)
(c) \(1.23456 \mathrm{E}+08\)
(d) \(1.23456 \mathrm{E}-08\)
(e) \(1 \mathrm{E}+12\)
(f) \(1 \mathrm{E}-12\)

Ordinary notation
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)
15. Write each "ordinary" number in ATARI BASIC floating point notation.

Ordinary notation
(a) \(1,234,560,000,000\)
(b) .00000000123456
(c) \(10,000,000,000\)
(d) . 0000000001
(e) 12345678999
(f) . 00000123456789
(g) \(\quad 6.02 \times 10^{23}\) (See note.)
(h) \(1.67 \times 10^{-21}\) (See note.)

Note: The numbers in (g) and (h) are written in scientific notation commonly used in mathematics and science.

\section*{Answers to Self-Test}

The frame numbers in parentheses refer to the frames in the chapter where the topic is discussed. You may wish to refer to these for quick review.
1. Executes the statement, then "forgets" it (frame 5)
2. Press DELETE BACK S to delete the mistake, then type the correct character (frames 7-9)
3. addition + subtraction multiplication division exponentiation (frames 10-24)
4. ERROR - PLEASE DO THE HOMEWORK (The computer does not understand what we want.) (frame 3)
5. PLEASE DO THE HOMEWORK ON PAGE 157 (frames 5-6)
6. 98.6 (frames 16-24)
7. PRINT 5/9*(F-32) or PRINT (5/9)*(F-32) Did you remember the asterisk? By the way, we will also accept PRINT 5*(F-32)/9 (frames 20-23)
8. Only the cursor shows. Entire line deleted. (frame 9)
9. Evaluate the numerical expression \(23+45\) and print the result. The computer will add 23 and 45 , getting 68, and print 68 . (frame 10)
10. Expressions (a), (d) and (g) are valid. In (g), the computer will evaluate \(2^{\wedge} 2^{\wedge} 2\), as follows: \(2^{\wedge} 2^{\wedge} 2=4^{\wedge} 2=16\). In other words, the computer will do it left to right, as if it were written \(\left(2^{\wedge} 2\right)^{\wedge} 2\). (frames 24-26)
11. (b) \(7^{*}(8+9)\)
(c) \(1.23 / 4.567\)
(e) \(1 /(37-29)\)
(f) \((1+7 / 100)^{\wedge} 3\)
(frames 16-26)
12. (a) \(2+4-4\)
(b) \(2 * 3 * 4\)
(1) 2
(c) \(2 * 3 / 4\)
(d) \(2 / 3 / 4\)
(1) 2
(e) \(2 / 3 * 4\)
(2) (1)
(g) \(2+3 / 4\)
(i) \(2 \stackrel{\text { a }}{*} 3 \stackrel{1}{\uparrow} 4\)
(2) (1)
(k) \(2 / 3 \uparrow 4\)
(3) (2) 1
(m) \(1+2 * 3 \uparrow 4\)
(frames 16-25)
13.
(2) (1)
(a) \(2+(3-4)\)
(b) \(2 /(3 / 4)\)
(c) \(2 /(3 * 4)\)
(d) \((2-3) \stackrel{2}{*} 4\)
(e) \((2+3) \stackrel{(1)}{+} 4\)
(f) \(2 \stackrel{2}{\uparrow}\left(3{ }^{*} 4\right)\)
(g) \(2 \stackrel{2}{\uparrow}(3 \stackrel{1}{\uparrow} 4)\)
\(\left.\begin{array}{l}\text { (6) (2) ( } \\ +1 \\ +1 \\ +1 \\ +1 \\ +1 \\ +1 \\ +1 \\ +1\end{array}\right)\)
(frames 16-25)
14. (a) 123,456
(b) .0000123456
(c) \(123,456,000\)
(d) . 0000000123456
(e) \(1,000,000,000,000\)
(f) . 000000000001
(frames 29-34)
15. (a) \(1.23456 \mathrm{E}+12\)
(b) \(1.23456 \mathrm{E}-09\)
(c) \(1 \mathrm{E}+10\)
(d) \(1 \mathrm{E}-10\)
(e) \(1.23456789 \mathrm{E}+10\)
(f) \(1.23456789 \mathrm{E}-06\)
(g) \(\quad 6.02 \mathrm{E}+23\)
(h) \(\quad 1.67 \mathrm{E}-21\)
(frames 29-34)

\section*{CHAPTER THREE}

\section*{Assignment Statements, Stored Programs, and Branching}

This chapter introduces some of the most useful BASIC statements. From here on, we can work with more interesting programs to illustrate home, school, and personal applications of computers.

In this chapter, you will learn the function and format for the statements and commands listed below.
\begin{tabular}{ll} 
Statements: & LET, INPUT, GO TO, PRINT, REMARK \\
Commands: & NEW, RUN, LIST
\end{tabular}

You will learn how you can store programs for automatic and repetitive execution. You will also learn about variables and be able to supply values for variables used in BASIC programs. When you have finished this chapter, you will be able to:
- write programs in which values are assigned to variables by means of LET statements or INPUT statements;
- distinguish between and use numeric variables and string variables;
- write programs in which a value calculated by a BASIC expression is assigned to a numerical variable in a LET statement;
- store a BASIC program in the computer's memory;
- erase an unwanted program from the computer's memory, LIST a program currently in the computer, and RUN (execute) a program;
- edit, correct, and delete statements in a stored program;
- write programs that use the GO TO statement to repeat a portion of a program or to skip over a portion of a program;
- use REMARK statements to make programs more readable and understandable by humans;
- write PRINT statements which identify printed results with descriptive messages.
1. To illustrate the concept of variable and the function of the LET statement in BASIC, imagine that there are 26 little boxes inside the computer. Each box can contain one number at any one time.
A
\begin{tabular}{|c|c|}
\hline & 7 \\
\hline & 5 \\
\hline C & \\
\hline D & \\
\hline E & \\
\hline F & 2 \\
\hline G & \\
\hline
\end{tabular}

\begin{tabular}{|c|c|}
\hline \multicolumn{2}{|l|}{0} \\
\hline P & \(4 \mathrm{E}+09\) \\
\hline \multicolumn{2}{|l|}{Q} \\
\hline \multicolumn{2}{|l|}{R} \\
\hline S & -6 \\
\hline T & \\
\hline U & \\
\hline
\end{tabular}


We have already stored numbers in some of the boxes. For example, 7 is in box A and 5 is in box B .
(a) What number is in box F ? \(\qquad\)
(b) In J? \(\qquad\)
(c) -6 is in box \(\qquad\) -
(d) 2.5 is in box \(\qquad\) .
(e) What box contains a floating point number? \(\qquad\)
- - - - - - - - -
(a) 2; (b) 4 ; (c) S ; (d) X ; (e) P (The floating point number is \(4 \mathrm{E}+09\).)
2. Boxes C and N are shown below. Use a pencil to do the following.
(a) Put 8 into box C . In other words, write the numeral " 8 "' in the box labeled "C." Do this before you go on to (b).
(b) Put 12 into N . Do this before you go on to (c).
(c) Put 27 into N. But wait! A box can hold only one number at a time. Before you can enter 27 into N , you must first erase the 12 that you previously entered.
N \(\square\)

Fill in the boxes before you look at the answer.

3. When the computer puts a number into a box, it automatically erases the previous content of the box, just as you did. In order to put 27 into box N , you first erased the previous content, 12.

We call \(\mathrm{A}, \mathrm{B}, \mathrm{C}, \ldots, \mathrm{Z}\) variables. The number in box A is the value of \(A\); the number in box B is the value of \(B\); the number in box C is the value of \(C\), and so on.

We use the LET statement to instruct the computer to 'put a number in a box." To say it more technically, we are assigning a numerical value to a variable.

We type: Let \(A=7\)
We type: PRINT A

It types: 7
In this program, the variable is \(\qquad\) and the value assigned to it by the LET statement is \(\qquad\) —.

A; 7
4. Complete the following.
(a) We type: LET \(x=23\)
PRINT \(x\)
(b)
We type: \(\begin{aligned} & \text { LET } z=-1 \\ & \text { PRINT } z\end{aligned}\)
It types: \(\qquad\) It types: \(\qquad\)
(c) We type: Let \(A=1\)
LET \(A=2\)
(d)
We type:
\[
\begin{aligned}
& \text { LET } D=7 \\
& \text { LET } W=D
\end{aligned}
\]
It types: \(\qquad\) It types: \(\qquad\)
(a) 23
(b) -1
(c) 2 (The statement LET A \(=2\) replaced the value previously assigned by LET \(\mathrm{A}=1\).)
(d) 7 (LET \(\mathrm{W}=\mathrm{D}\) copies the value in D into W . The value is still in D , also.)
5. Write a LET statement to assign the value 3.14 to P and a PRINT statement to print the value of P .

We type: \(\qquad\)
\(\qquad\)
It types: \(\qquad\)

LET \(P=3.14\)
PRINT \(P\)
3.14

Note: In ATARI BASIC, the word LET can be omitted. For example, we can type \(\mathrm{P}=3.14\) instead of LET \(\mathrm{P}=3.14\).
6. Once we have assigned a value to a variable, that variable can be used in mathematical expressions.

We type: LET \(A=7\)
\[
\text { LET } B=5
\]


We now have 7 in box A and 5 in box B .


We type: PRINT A + b
It types: \(12 \quad\) Since \(A=7\) and \(B=5, A+B=7+5=12\).
We type: PRINT A - b
It types: \(2 \quad\) Since \(A=7\) and \(B=5, A-B=7-5=2\).
Your turn. Complete the following.
We type: PRINT A*B
It types: \(\qquad\)
We type: PRINT A/B
It types: \(\qquad\)
7. The variables that we have used so far are called numeric variables. The value assigned to a numeric variable must be a number.

BASIC has another type of variable, called a string variable. The value assigned to a string variable must be a string. A string variable is indicated by a letter followed by a dollar sign(\$).

Before we use a string variable, we must first tell the computer how long the string might be. That is, we must tell the computer how much memory might be needed to hold the string. We do this with a DIMension statement. For example, the following DIM statement tells the computer to make room for a string of up to 5 characters in length.

We type: DIM N\$(5)
It types: READY
We have told the computer that a string variable called \(\mathrm{N} \$\) can have as many as 5 characters in length.

We type: Let ns = "Jerry"
This assigns the value JERRY to the string variable N\$.
N\$

Now, let's print the value of \(\mathrm{N} \$\).
We type: PRINT Ns
It types: JERRY
Complete the following.
We type: DIM \(\mathbf{Z \$ ( 1 \varnothing \infty )}\)
LET \(Z \$=\) "MY HUMAN UNDERSTANDS ME" PRINT Z\$

It types:


MY HUMAN UNDERSTANDS ME

Our DIM statement reserved space for up to 100 characters. Our actual string, in this case, is shorter than 100 characters. Chapter 9 will describe strings in much more detail.
8. Let's look at a problem. We have three bicycles with wheels of 16-, 24-, and 26 -inch diameters. For each bike, we want to know how far the bike travels during one revolution of the wheel. This distance, of course, is the circumference of the wheel. Let's use \(D\) to represent the diameter of the wheel and \(C\) to represent the circumference.
\[
C=\pi D
\]
where \(\pi=3.14159 \ldots\)


We will use 3.14 as a crude approximation to \(\pi\). We could do this problem as follows.

We type: PRINT 3.14 * 16
It types: 50.24
We type: PRINT 3.14 * 24
It types: \(\quad 75.36\)
We type: PRINT 3.14 * 26
It types: 81.64
Here is another way to do it. Complete the parts we have omitted
```

We type: LET D = 16
PRINT 3.14 * D
It types: $\quad 50.24$
We type: $\begin{aligned} & \text { LET } D=24 * \\ & \\ & \text { PRINT } 3.14 * D\end{aligned}$

```

It types: \(\qquad\)
We type: LET \(\qquad\)

It types: 81.64
75.36
\(D=26\)
PRINT 3.14 * D
9. Now we are ready to take the big step from one-at-a-time direct statements to a stored program. We will store this program in the memory of our computer. (Just look at it, then read on.)
```

1\varnothing LET D = 16
2\varnothing PRINT 3.14 * D

```

The above program has two statements, each on a single line. Each statement begins with a line number (in this case, the 10 and 20). A line number can be an integer from 1 to 32767.

When we type statements with line numbers, the statements are not executed when you press RETURN. Instead, the statements are stored in the computer's memory for later execution.

As you learned in Chapter 2, statements without line numbers are called direct statements. The computer executes a direct statement immediately and then forgets it. However, this does not happen when we type a statement with a line number. Instead, what does happen?
```

-     -         -             -                 -                     -                         -                             -                                 - 

```

The statement is stored in the computer's memory for later execution. That is, the computer remembers the statement.
10. The line numbers tell the computer the order in which it is to follow statements in the program. It is not necessary for line numbers to be consecutive integers (e.g., \(1,2,3,4,5 \ldots\) ). It is common practice to number by tens as we do in the following program. Then, if we wish, we can easily insert or add more statements into the program between existing statements.
```

1\varnothing LET D = 16
2\varnothing PRINT 3.14* D

```

How many additional lines could be added betwen line 10 and line 20 ?
\(\qquad\)
- - - - - - - -

9 (lines \(11,12,13,14,15,16,17,18,19)\)
Of course, you don't have to number by tens. If you prefer numbering by thirteens or fives or jumping around, help yourself!
11. Before we store a program, we must first remove or erase any old programs that may already be stored in the computer's memory.

We type: New And, of course, press RETURN.
It types: Ready
The computer has erased the portion of its memory that stores BASIC programs. It is now ready to accept a new program.

How do we erase, remove, or delete an old program from the computer's memory?

We type NEW and press RETURN key.
Note: If we misspell NEW, we may get an error message. For example:
We type: \({ }^{\text {gnu }}\)
It types: error- gnud
Our computer doesn't appreciate puns, but if we type NEW correctly and press RETURN, all is well.
12. Now we are ready to store our two-line program from frames 9 and \(\mathbf{1 0}\). First, we must erase any old program by typing \(\qquad\) and pressing the RETURN key. To store the program, we type the first line or statement and press the RETURN key, then type the second line and \(\qquad\)

NEW; press the RETURN key
13. Let's do it.

We type: New
It types: ready
We type: \(1 \varnothing\) LET \(D=16\) \(2 \emptyset\) PRINT 3.14*D

If we make a typing error, we start over. The program is now stored. The computer is waiting patiently for our next statement or command.

Hmmmm . . . we wonder if the program really is stored in the computer's memory. We can find out by typing LIST and pressing the RETURN key.

We type: LIST

\section*{And press RETURN.}
```

It types: 1\varnothing LET D=16
20 PRINT 3.14*D
READY

```

The command LIST tells the computer to type all of the program statements that are currently stored in its memory. After listing the program, the computer types READY to let us know it is our turn again. If there is no program stored, the computer will simply type READY.

How do we tell the computer to type out the program that is currently stored in its memory? \(\qquad\)
- - - - - - - - -

We type LIST and press the RETURN key.
14. Listing a BASIC program lets us know whether or not a program is stored in the computer's memory. We may want to add more statements to the program. Or we may wish to see if we have typed the statements correctly. If we want the computer to execute the program, we type \(\qquad\) . If we want the computer to tell us if there is a program stored in its memory, and to type out the program for us, we type \(\qquad\) .

15. After you type RUN to tell the computer to execute a program, or after you type LIST to command the computer to tell us 'what's on its mind"' (that is, what is stored in its memory), what else do you have to do before the computer will respond? \(\qquad\)
press the RETURN key
16. Assume you have typed our little program into the computer.
```

1\varnothing LET D = 16
20 PRINT 3.14 * D

```

The program is stored in the computer's memory. Now you want the computer
to execute (carry out) the program. Type RUN and press the RETURN key. We type: run

And press RETURN.
It types: \(\quad 5 \boldsymbol{0 q} .24\)
READY
The computer has RUN the program. That is, it has executed the statements of the program in line number order. First, the computer was told to assign a value to a variable with this statement: 10 LET \(\mathrm{D}=16\). That means that the computer placed the value \(\qquad\) in the box identified by the variable
\(\qquad\) .

16; D
17. After following the instruction in the statement with line number 10 , the computer went on to the next statement in line number order: 20 PRINT 3.14*D. Part of line 20 tells the computer to multiply two numbers. One number is given in the statement. The other number is stored in a place labeled by the variable D . What are the two values that the computer uses to multiply?
3.14 and 16 (Because 16 is the value of D.)
18. In the last frame we saw that part of line 20 tells the computer to multiply two values. What else does line 20 tell the computer to do? \(\qquad\)
\(\qquad\)


PRINT the results of the multiplication
Note: some computers require an END statement as the last statement in the program, as we show below. Our ATARI computer does not need END, but you may use it if you wish.
```

1\varnothing LET D = 16
2ø PRINT 3.14* D
3% END

```
19. Let's review what happens when we use our little program that calculates the circumference of a bicycle wheel.
READY
1\varnothing LET D = 16
2@ PRINT 3.14 * D
LIST
1ø LET D=16
2ø PRINT 3.14*D
READY
RUN
    50.24
READY
```

```
```

NEW

```
```

```
NEW
```

First, we erase any old program.

Then, we type in this program, which consists of two statements.

Next, we tell the computer to LIST the program.
The computer LISTs (types) the program,
then types READY and stops.
Finally, we tell the computer to RUN the program.
It executes the program,
then types READY and stops.
The program is still stored in the computer's memory. What will happen if we now type RUN $\qquad$

-     -         -             -                 -                     -                         -                             - 

The computer will execute the program again. Since nothing in the program has changed, the same result (50.24) will be printed.
20. What happens if we make a typing mistake in entering a program?

We type: $1 \varnothing$ LET $F=16$ We typed $F$ instead of $D$.
20 PRINT $3.14^{*} D$
We type: run
It types: $\varnothing$

We type: LIST
It types: $\begin{aligned} & 1 \varnothing \text { LET } F=16 \\ & \\ & 2 \varnothing \text { PRINT } 3.14 * D\end{aligned}$

We type: $1 \varnothing$ LET $D=16$

We type: List
It types: $1 \varnothing$ LET $D=16$ $2 \varnothing$ PRINT 3.14*D

Oops! Something wrong. Let's look at the program.

Sure enough, we notice that we mistakenly hit F instead of D in line 10.

We retype line 10 , correctly. This replaces the old line 10.

To make sure the new line 10 replaced the old line 10 , we LIST the corrected program (and also check to make sure we typed it right this time!)

Suppose we had seen the mistake immediately after we had typed it. How could we have corrected it?

We could have pressed the DELETE BACK S key, then the correct letter.
21. We assume that our circumference program is still stored in memory. Now we want to change the value assigned to $D$. To do this, we replace line 10 with a different line 10. After making this change, we will LIST the modified program.

We type: $\begin{aligned} & 1 \varnothing \text { LET } \\ & \text { LIST }\end{aligned}$
It types: $1 \varnothing$ LET $D=24$ Here is the new line 10, and the old 2ø PRINT 3.14*D line 20.

How do we replace a line in a stored program? $\qquad$

We type a new line with the same line number as the line we wish to replace.
Note: We do not type NEW because we want line 20 to remain in the computer while we change only line 10. Typing NEW would erase both statements from the computer's memory.
22. We will RUN the modified program of frame 23.

| We type: | RUN |
| :--- | :--- |
| It types: | $\mathbf{7 5 . 3 6}$ |

Your turn. Complete the following.
We type: $\quad 1 \varnothing$ LET $D=26$
We type: LIST

23. How fast does your money grow?

Problem: We put P dollars in a savings account which pays R percent interest, per year, compounded yearly. How much money will we have in the account at the end of N years?

P is the original amount (principal).
R is the interest rate, in percent, per year.
N is the number of years.
A is the amount after N years.

$$
A=P(1+R / 100)^{N} \quad \text { Formula for } A \text {, given } P, R \text {, and } N
$$

Below is a program to compute A for $\mathrm{P}=\$ 1000, \mathrm{R}=6 \%$, and $\mathrm{N}=3$ years. Complete line 40 in correct BASIC notation, using the formula above as a guide.

```
10 LET P = 10\varnothing\varnothing
2\emptyset LET R = 6
30 LET N = 3
4\varnothing LET A =
50 PRINT A
```

$P^{*}(1+R / 1 \varnothing \varnothing)^{\wedge} N$ (Did you remember the asterisk? Did you remember to use ^ to tell the computer to raise to a power?)
24. We will store and RUN the program, then ask you to make some changes.

We type: New
$1 \varnothing$ LET P $=1 \varnothing \varnothing \varnothing$
$2 \varnothing$ LET $R=6$
$3 \varnothing$ LET $N=3$
$4 \varnothing$ LET $A=P^{*}(1+R / 1 \varnothing \varnothing)^{\wedge} N$
$5 \emptyset$ PRINT A
RUN

Don't forget, we are usually omitting the READY typed by the computer. We also will omit reminders to use the RETURN key after entering a statement or a command such as RUN, LIST, or NEW

It types: $1191 . \boldsymbol{\sigma l}_{1596}$

Now, show how to change line 30 so that $N=5$.
We type: $\qquad$
RUN
It types: 1338.22554
Value of A for $\mathrm{P}=1000, \mathrm{R}=6, \mathrm{~N}=5$.

-     -         -             -                 -                     -                         -                             -                                 - 

$3 \varnothing$ LET $N=5$
25. Now change the program so that $R=7 \%$ and $N=8$ years.

We type:

RUN
It types:

-     -         -             -                 -                     -                         -                             -                                 - 

$2 \varnothing$ LET R=7
$3 \varnothing$ LET $N=8$
26. Now show how the computer will respond if we type LIST.

We type: List
It types: $\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

```
- - - - - - - - 
1\varnothing LET P=1\varnothing\varnothing\varnothing
20 LET R=7
3\varnothing LET N=8
4| LET A=P*(1+R/1\varnothing\varnothing)^N
50 PRINT A
```

27. LET statements are all fine and good, but what a hassle to change all those LET statements every time you want to change the values of variables. Ah, but leave it to BASIC to come up with a clever solution-the INPUT statement.

The INPUT statement allows the computer user to assign different values to variables each time a program is RUN without modifying the program itself. When the computer comes to an INPUT statement in a program, it types a question mark and waits for the user to enter a value for a variable. Below is an example:

| We type: | NEW |  |
| :--- | :--- | :--- |
|  | $1 \varnothing$ INPUT <br> $2 \varnothing$ PRINT A <br> RUN | First, we erase any old program, then enter this <br> program. |
| It types: | $? \square$ | Then we tell the computer to RUN the program. |
|  |  | The computer types a question mark, turns on the <br> cursor, then waits. |

When we typed RUN, what did the computer do?

-     -         -             -                 -                     -                         -                             - 

It typed a question mark and waited for us to do something.
Note: The question mark is an example of a prompt. The computer types a prompt to tell you it is your turn to do something. The message READY is another example of a prompt.
28. The INPUT statement causes the computer to type a question mark, then stop and wait. It is waiting for a value to assign the variable which appears in the INPUT statement. Computers are very patient. If we don't cooperate by typing a value, the computer will simply wait, and wait, and wait.

So let's cooperate with our ever-patient computer and type in a value for A. We will enter 3 as a value to be assigned to A, then press RETURN. The computer will put our value into box $A$, then continue running the program.


After we typed 3 as the value for $A$ and then pressed RETURN, the computer went on to line 20 and printed our value.

After we typed RUN and pressed the RETURN key, the computer typed a _. We then typed 3, which is our value for the INPUT
variable $\qquad$ . The computer then executed the PRINT A statement (line 20)
and printed the $\qquad$ of $A$.

question mark; A; value
29. The program can be RUN again with a different value of A supplied by the user. Pretend you are the computer, and show how a RUN would look if your human computer user typed 23 as the value of $A$.

RUN
$\qquad$
$\qquad$

-     -         -             -                 -                     -                         -                             -                                 -                                     - 

?23
23
30. Now let's use an INPUT statement to enter (type in) data for our familiar bicycle wheel problem. Data is the name for information used by a computer program.

We type: NEW
$1 \varnothing$ INPUT D
$2 \varnothing$ PRINT $3.14 * D$

It types: $\stackrel{\text { RUN }}{?}$
The computer wants a value for D , the diameter of our bicycle wheel. It will then compute the distance traveled in one revolution, and print it. Let's do it for $\mathrm{D}=16, \mathrm{D}=24$, and $\mathrm{D}=26$.

$-\ldots-\ldots-\ldots-\ldots-$

326
81.64
31. One INPUT statement can be used to assign values to two or more variables.

```
1\varnothing input A,b Two variables, A and B.
2\emptyset PRINT A+B
RUN
? 7,5 Two values, 7 and 5.
```

When the computer typed a question mark, we typed two numbers separated by a comma, then pressed the RETURN key. The computer assigned the first number as the value of A and the second number as the value of B . Note the following.


The value 7 is assigned to the variable A , and the value 5 is assigned to the variable $B$.

Here is the summary; you fill in the blanks. When a program containing an INPUT statement with multiple variables is RUN, the first value typed in by the user after the INPUT question mark will be assigned to the $\qquad$ variable that appears in the INPUT statement; the $\qquad$ value typed in by the user will be assigned to the second variable appearing in the INPUT statement, and so on. Both the variables in the INPUT statement in the program, and the values typed in by the user when the program is RUN, must be separated by
$\qquad$ .

## _ - - - - - - - - -

first; second; commas
32. Here is another RUN of the program in frame 31. We want to enter 73 as the value of A and 59 as the value of B.

```
RUN
? }73\mathrm{ Oops! We absentmindedly hit the RETURN key.
?!
Oops! We absentmindedly hit the RETURN key.
```

The computer typed another question mark and turned on the cursor. This means "Didn't you forget something?"

We then completed the RUN by entering the second number, the value of B .

What happens if we don't enter a numerical value for every variable in an INPUT statement?

The computer types another question mark.
Note: If you enter more numbers than there are variables, the computer will ignore the extra values.
33. Suppose you and a bunch of friends, all bicycle aficionados, are gathered about your computer, and they are marveling at your newly acquired computer programming skills. You decide to demonstrate how the computer works by using the program to compute the distance traveled in one turn of the wheel. However, you have to do a separate RUN of the program for each friend. But wait-first add a new statement to the program.

```
1\varnothing INPUT D
2ø PRINT 3.14*D
```

$3 \varnothing$ GO TO 1ø $\longleftarrow$ Something new-a GO TO statement,

In BASIC, a GO TO statement tells the computer to jump to or branch to the line number following the words GO TO, and then to continue following the instructions in the program in the usual line number order.

In the above program, the GO TO statement tells the computer to jump to line $\qquad$ and start the program over again.


10


```
34. Let's see what happens when we RUN the program. (Assume that you, or
someone, has typed NEW, then entered the program.)
```

```
RUN
```

RUN
?16 Following each question mark, we typed the value of D. The
?16 Following each question mark, we typed the value of D. The
5ø. 24
5ø. 24
?24
?24
75.36
75.36
?26
?26
81.64
81.64
3

```
3
```

Well, we are finished, but the computer doesn't know that we are finished. It is hung up on line 10, waiting for INPUT data. How do we get out of this situation?
Easy! Just press the BREAK key.
$? \longleftarrow$ We press the BREAK key.
stopped at line $10 \longleftarrow$-It types the line number where the BREAK occurred and turns on the cursor

Suppose the computer is executing an INPUT statement and has typed a question mark. If we press the BREAK key, what does the computer do? $\qquad$
---------

It "escapes" from the INPUT statement, types STOPPED AT $\ell$ (where $\ell$ is the line number where the BREAK occurred) and turns on the cursor.
35. Remember: BASIC statements are executed in line number order, unless a GO TO statement changes the order. In the program from frame 33, the statements are executed in the order shown below by the arrows.


Around and around and around-until you quit by pressing the BREAK key.

The above program is an example of a loop. The GO TO statement causes the computer to 'loop back'" to the beginning. In this program, the computer loops back to an INPUT statement and then stops. Watch out! We can write programs with nonstop loops. Here is an example. Type NEW before you enter the program.

```
13 PRINT "TO STOP ME, PRESS THE 'BREAK' KEY"
27 GO TO 13
```

Do not RUN this program yet! Instead, draw arrows as we did on the previous page to show how the computer executes the program.

RUN
13 PRINT "TO STOP ME, PRESS THE 'BREAK' KEY"
27 GO TO 13


We have used line numbers 13 and 27 to remind you that you don't have to number by 10 , although we usually do.
36. Now let's enter the program of frame 35 and RUN it. Remember, to stop the computer, press the BREAK key.

```
13 PRINT "TO STOP ME, PRESS THE 'bREAK' KEY"
27 GO,TO 13
RUN
TO STOP ME, PRESS THE 'bREAK' KEY
TO STOP ME, PRESS THE 'bREAK' KEY
TO STOP ME, PRESS THE 'bREAK' KEY
TO STOP ME, PRESS THE 'BREAK' KEY
TO STOP ME, PRESS THE 'bREAK' KEY
STOPPED AT LINE 13 (OR 27) & We pressed the BREAK key!
```

The computer executed line 13 over and over again, because the GO TO statement in line 27 repeatedly told the computer to go back to line 13 . This is a "forever" loop-it just keeps going around and around until someone interrupts it. Sometimes this is referred to as an "infinite" loop, because it does not stop automatically.

How do we interrupt, or stop, the computer when it is running a program?

We press the BREAK key.
37. Now that you know how to stop a runaway computer by pressing the BREAK key, let's write a ''Happy Computer'' program. This program will quickly fill the screen with laughter! Remember: before entering the program, type NEW to erase any old program. Then, enter the following program. The program contains some old statements, such as PRINT and GO TO, and a new statement called REMARK. We use the REMARK statement to tell something about the program to a human who may be reading the program. The computer simply ignores REMARK statements.


OK, run this program. Did the screen fill with laughter? $\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

We think you answered YES. When we did it, the entire screen quickly filled with HA HA.
38. Try the above program with line 110 modified as follows:
$11 \varnothing$ PRINT "HA HA "


Run the modified program. Did only the left portion of the screen fill with HA HA? $\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

Again, we think you answered YES. The semicolon causes the computer to print across the screen from left to right. When the computer gets to the right edge, it simply continues on the next line. Without the semicolon, the computer starts a new line after each PRINT statement.
39. The REMARK statement has a short form that you can use. The short form is simple, the first three letters in REMark. When executing a program, the computer only "looks" at the first three letters, and if those three letters are REM, then the computer will skip on to the next statement in line number order without considering the rest of the statement. Therefore, you could use the word REMEMBER instead of REMark and the effect would be the same.

Rewrite line 100 in frame 37 using the short form of the REMark
statement

```
- - - - - - - - - 
1\varnothing\varnothing REM FILL THE SCREEN WITH 'LAUGHTER'
```

40. When the computer executes a PRINT statement that has only the word PRINT following the line number and nothing else in the statement, it does the same thing that happens when you press the RETURN key. It spaces down one line on the screen. This has the effect of leaving a blank or "empty" line on the screen. An "empty" PRINT statement is very handy for making the printout of a program easier to read.

Here is a RUN from our bicycle wheel program from Frames 33 and 34.

```
RUN
316
    50.24
?24
    75.36
?26
    81.64
?!
```



Well, let's make it less crowded! We will add the following empty PRINT statement to the program.

```
25 PRINT
```

| We type: | $1 \varnothing$ INPUT D |
| :--- | :--- |
|  | $2 \varnothing$ PRINT $3.14 * D$ |
|  | 25 PRINT |
|  | $3 \varnothing$ GOTO $1 \varnothing$ |

Let's RUN it and see what happens.

Note the line space. The "empty" line is provided by line 25 .
724
75.36
Another line space.
$? 26$
81.64
Still another line space.
? $\quad$ and so on.

Compare the two RUNs. What does 25 PRINT tell the computer to do?

Print a line space ("empty"' line) after printing the value of $3.14 *$ D. This happens before the computer executes GO TO 10.
41. Now, in order to make things really clear when dealing with INPUT statements, we need a way to inform the user what the INPUT statement is asking for. Let's add this statement to the bicycle program:

```
5 PRINT "WHEEL DIAMETER" ;
```

See the semicolon at the end of the PRINT statement? When a semicolon is used at the end of a PRINT statement, the computer stays on the same line of the screen instead of going to the beginning of the next line. Here is our revised program.

```
5 PRINT "WHEEL DIAMETER" ;
10 INPUT D
2\varnothing PRINT 3.14*D
25 PRINT
3ø GO TO 1ø
```

Let's RUN the modified program.
We type: It types:


Aha! Now we know exactly what the computer wants. It wants a value for WHEEL DIAMETER. OK, we type 16 as the value of WHEEL DIAMETER and press RETURN. Show what happens next.
WHEEL DIAMETER? 16

5ø. 24
WHEEL DIAMETER?
42. Now what the computer wants is clearly identified by the string enclosed in quotation marks in the PRINT statement. We use the same approach in a PRINT statement to identify the calculation performed by the computer for that statement (see line 20).


The statement 20 PRINT "DISTANCE IN ONE TURN IS"; 3.14*D tells the computer to:
(1) print the string DISTANCE IN ONE TURN IS, then
(2) compute and print the value of $3.14^{*} \mathrm{D}$.

Let's try it. Complete the RUN.
RUN
WHEEL DIAMETER? 16
DISTANCE IN ONE TURN IS $5 \varnothing .24$
WHEEL DIAMETER? 24
DISTANCE IN ONE TURN IS
WHEEL DIAMETER? 26

```
75.36
DISTANCE IN ONE TURN IS 81.64
WHEEL DIAMETER? « Our everfriendly cursor.
```

43. Rewrite the program in frame 42 so that a RUN looks like the one shown below.

RUN

```
IF YOU ENTER THE DIAMETER OF A BICYCLE
WHEEL, THEN I WILL TYPE THE DISTANCE
TRAVELED IN ONE TURN OF THE WHEEL.
WHEEL DIAMETER?16
DISTANCE IN ONE TURN IS 50.24
WHEEL DIAMETER?24
DISTANCE IN ONE TURN IS 75.36
WHEEL DIAMETER? . . . and so on. To stop, press BREAK.
```

Write the program below.

```
1% REMARKABLE* BICYCLE PROGRAM
2\varnothing PRINT "IF YOU ENTER THE DIAMETER OF A BICYCLE"
3ø PRINT "WHEEL, THEN I WILL TYPE THE DISTANCE"
4\varnothing PRINT "TRAVELED IN ONE TURN OF THE WHEEL"
5| PRINT
6』 PRINT "WHEEL DIAMETER";
7& INPUT D
8% PRINT "DISTANCE IN ONE TURN IS" ;3.13*D
9@ GO TO 5ø
```

[^0]44. The INPUT statement, like the LET statement, belongs to the class of BASIC instructions called assignment statements. The value we type in response to a question mark is assigned to the variable in the INPUT statement. If the INPUT variable is a string variable, we can type in a string as the value and it will be assigned to the string variable. Here is a simple example. You do the parts that we omit.


WHAT IS YOUR NAME? FIREDRAKE, THE DRAGON

## LEROY FINKEL

FIREDRAKE, THE DRAGON

In Chapter 9, we will discuss strings in much detail.
45. Here's a program that lets you use the computer as an adding machine, by repeating an "adding routine" with a GO TO loop. A "routine" is one or more statements to complete a computing task.

```
1\varnothing\varnothing REM ** WORLD'S MOST EXPENSIVE ADDING MACHINE
11\varnothing PRINT "I'M THE WORLD'S MOST EXPENSIVE ADDING"
12\varnothing PRINT "MACHINE. EACH TIME I TYPE ' }X=?\mathrm{ ?' YOU"
130 PRINT "TYPE A NUMBER AND PRESS THE RETURN KEY."
14\varnothing PRINT "I WILL THEN TYPE THE TOTAL OF ALL THE"
150 PRINT "NUMBERS yOU HAVE ENTERED."
160 LET T=0
17\varnothing PRINT "x="; Lines 170 through 220 are a GO TO
19\varnothing INPUT X loop. These lines are done for each
2\varnothing\varnothing LET T=T+X NOM SO FAR IS";T TOTAL SNEM entered by the user.
210 PRINT "TOTAL SO FAR IS";T
22\varnothing GOTO 17\varnothing
```

Lines 170 through 220 are a GO TO loop. These lines are done for each number entered by the user.

Notice the LET statements using the variable T in lines 160 and 200. Line 160 is outside the GO TO loop. It is executed once before the loop begins, setting T equal to zero. This is called initializing, giving an initial or starting value to a variable.

Line 200 is inside the GO TO loop. Therefore line 200 will be executed each time through the loop. In line 200, a new value of T is computed by adding the old value stored in box ' T to the INPUT value of X entered by the computer user.

(a) Suppose the old value of T is zero and the INPUT value of X is 12.

What is the new value of T ? $\qquad$
(b) Suppose the old value of T is 12 and the INPUT value of X is 43 . What is the new value of T ? $\qquad$
(a) 12; (b) 55
46. Note how the PRINT statements (lines $110-150$ ) are used to provide the user with an explanation and instructions for using the program. Are the PRINT statements inside or outside the GO TO loop? $\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

outside

Therefore, lines $110-150$ will be done once, when you first type RUN. Of course, if you interrupt the computer (by pressing BREAK) and RUN the program again, lines $110-150$ will be done again.
47. It's RUN time. Let's see how the progam works.

## RUN

```
I'M THE WORLD'S MOST EXPENSIVE ADDING
```

MACHINE. EACH TIME I TYPE ' $x+$ ?' YOU
type a number and press the return key.
I will then type the total of all the
numbers you have entered.
$\mathrm{x}=$ ? 12
total so far is 12
$x=? 43$
TOTAL SO FAR IS 55
$\mathrm{x}=$ ? 33
TOTAL SO FAR IS 88
$\mathrm{x}=$ ? 92
TOTAL SO FAR IS $18 \varnothing$
$x=? 76.25$
TOTAL SO FAR IS 256.25
$x=? \llbracket$ Do you remember how to get out of this? If not, check frame 34.

From the listing in frame 45 , let's focus on the statement in line 200. For the RUN above, the first time through the program the values of the variables to the right of the $=$ symbol in 200 LET $\mathrm{T}=\mathrm{T}+\mathrm{X}$ will be:


So the new value for T is 12 . The value is printed. Notice that the computer substitutes the current values in the boxes for the variables to the right of the $=\quad$ sign each time it executes line 200.
For the second time through the "loop"' section of the program show the values:


The new value of $T$ is $\qquad$ .

```
LET T = 12 + 43
55
```


48. Now that you know how to stop a "runaway" computer, try this program, which causes the computer to print counting numbers, $1,2,3,4,5$, and so on, until you press BREAK.

```
1\varnothing LET N=1
2\varnothing PRINT N
30 LET N=N+1
4\varnothing GO TO 2\varnothing
RUN
    1
    2
    3
    5
    6
    7
STOPPED AT LINE 2\emptyset
```

How does it work? Follow the arrows.


This program is another example of a loop. Line 10 is outside the loop. Lines 20,30 , and 40 comprise the loop; they are repeated over and over and over. Line 10 is done once, initializing N equal to one.

Line 30 is inside the loop. It will be done each time through the loop. In line 30 , a new value of N is computed by adding 1 to the old value of N .

(a) Suppose the old value of N is 1 . What will the new value of N be? $\qquad$
(b) Suppose the old value of N is 2 . What will the new value of N be? $\qquad$
(a) 2; (b) 3 (Line 20 will print the new value next time around the loop.)
49. With a counting loop and a few other statements, we can write a program to show how our money grows, year by year. Here it is.

```
1ø\varnothing REM***WATCH YOUR MONEY GROW
11\varnothing PRINT "IF YOU TYPE THE AMOUNT OF PRINCIPAL"
12ø PRINT "AND THE INTEREST RATE PER YEAR, I WILL"
13\varnothing PRINT "SHOW YOU HOW YOUR MONEY GROWS, YEAR BY"
14\varnothing PRINT. "YEAR. TO STOP ME, PRESS THE BREAK KEY."
15ø PRINT
16\varnothing PRINT "PRINCIPAL";
165 INPUT P
17\varnothing PRINT "INTEREST RATE";
175 INPUT R
18\varnothing LET N=1 & Start year (N) at 1.
19\emptyset PRINT
20ø LET A=P*(1+R/1ø\varnothing)NN
21\emptyset PRINT "YEAR =";N
220 PRINT "AMOUNT =";A
230 LET N=N+1
24\varnothing GOTO 19\varnothing
RUN
IF YOU TYPE THE AMOUNT OF PRINCIPAL
AND THE INTEREST RATE PER YEAR, I WILL
SHOW YOU HOW YOUR MONEY GROWS, YEAR BY
YEAR. TO STOP ME, PRESS THE BREAK KEY.
PRINCIPAL? 1ø\varnothing\varnothing
INTEREST RATE? }
YEAR = 1
AMOUNT = 1059.99999
YEAR = 2
AMOUNT = 1123.59997
YEAR = 3
```



```
AMOUNT = 1191.@1596
```

And so on, until someone presses BREAK. Which statements are part of the loop? Give the line numbers. $\qquad$
$19 \varnothing, 2 \varnothing \varnothing, 21 \varnothing, 22 \varnothing, 23 \varnothing$, AND $24 \varnothing$
We suggest that you also draw a box around the loop with a felt tip pen. Note that lines 100 through 180 are outside the loop. They are done once during a RUN, while lines 190 through 240 are repeated over and over until you press

## BREAK.

## SELF-TEST

Try this Self-Test, so you can evaluate how much you have learned in this chapter.

1. Before entering a program, we usually first type NEW and press RETURN. Why? $\qquad$
$\qquad$
2. How do we tell the computer to type a complete listing of a program stored in its memory? $\qquad$
3. Assume that we have just stored a program in the computer's memory. How do we tell the computer to execute the program? $\qquad$
$\qquad$
4. Assume that the following program is stored in the computer's memory.
```
1\varnothing PRINT "MY COMPUTER UNDERSTANDS ME"
2\emptyset PRINT "MY COMPUTER CONFUSES ME"
```

Describe how to replace the second statement (line 20) without erasing the entire program.
5. What is the difference between direct statements and statements to be stored in the computer's memory for later execution? $\qquad$
$\qquad$
6. We store the following program and RUN it.

```
1\varnothing\varnothing PRINT "I PROMISE NOT TO CHEW BUBBLE GUM IN CLASS"
2\varnothing\varnothing GO TO 1\varnothing\varnothing
```

How do we stop the computer?
7. Each of the following statements contains an error. Mark the error and show the statement in correct BASIC format (syntax, that is).
(a) $2 \varnothing$ PRINT DISTANCE IN ONE TURN IS; 3. $14^{*} \mathrm{D}$
(b) $2 \varnothing$ "DISTANCE IN ONE TURN IS";3.14*D
(c) $2 \varnothing$ LET $P^{*}(1+R / 1 \varnothing \varnothing)^{\wedge} N=A$
(d) $2 \varnothing$ TYPE " $X=" ;$
8. Describe what is wrong with each statement.
(a) 99999 LET $A=7$
(b) $30 \quad$ GO TO 3.14
(c) $3 \varnothing$ GO TO - $1 \varnothing 0$
(d) 10 INPUT, $Z$
(e) 10 INPUT $Z$,
9. Describe what is wrong with each program.
(a) $1 \varnothing$ INPUT $A$

20 INPUT $B$
30 PRINT $A+B$
40 GO TO 12
(b) $1 \emptyset$ LET $A=7$
$2 \varnothing$ LET B $=5$
$3 \varnothing$ PRINT $X+y$
10. Complete the RUN on the line provided.

```
1\varnothing PRINT "A=";
15 INPUT A
2ø PRINT "B=";
25 INPUT B
3\varnothing PRINT "A + B ="; A+B
RUN
A=? 7
B=? 5
```

11. Write a program to convert temperatures, given in degrees Celsius, to degrees Fahrenheit, using the following formula.

$$
F=\frac{9}{5} C+32
$$

A RUN of your program should look like this.

```
RUN
YOU ENTER DEGREES CELSIUS.
I WILL TYPE DEGREES FAHRENHEIT.
DEGREES CELSIUS? Ø
DEGREES FAHRENHEIT = 32
DEGREES CELSIUS? 1ø\varnothing
DEGREES FAHRENHEIT = 212
DEGREES CELSIUS? 37
DEGREES FAHRENHEIT = 98.6
DEGREES CELSIUS?
```

And so on.
12. Congratulations! You are the big winner on a TV show. Your prize is selected as follows.

A number from 1 to 1000 is chosen at random. Call it N. You then select one, and only one, of the following prizes. You have 60 seconds to make your selection.

PRIZE NO. 1: You receive N dollars
PRIZE NO. 2: You receive D dollars, where $\mathrm{D}=1.01^{\mathrm{N}}$
Perhaps you recognize the formula for D. It is the amount you would receive if you invested $\$ 1$ at $1 \%$ interest per day, compounded daily for N days.

The question, of course, is: For a given value of N , which prize do you take, PRIZE NO. 1 or PRIZE NO. 2? Write a program to help you decide. A RUN might look like this.

```
RUN
N=? 1ø\varnothing
PRIZE NØ. 1 = 1\varnothing\varnothing
Take PRIZE NO. 1
PRIZE NØ. 2 = 2.7Ø4781277
N=? 50. 
PRIZE NØ. 1 = 5ø\varnothing Take PRIZE NO. 1
PRIZE NØ. 2 = 144.772491
N=? 100\varnothing
PRIZE NØ. 1 = 1\varnothing\varnothing\varnothing
Take PRIZE NO. 2
PRIZE NØ. 2 = 20959.0741
N=?
And so on.
```

13. Write this program to assist you in performing that tiresome task called "balancing the checkbook." Here is a RUN of our program.
```
RUN
I WILL HELP YOU BALANCE YOUR CHECKBOOK.
ENTER CHECKS AS NEGATIVE NUMBERS AND
DEPOSITS AS POSITIVE NUMBERS.
OLD BALANCE? 123.45
```

CHECK OR DEPOSIT? - 3.95
NEW BALANCE: 119.5
CHECK OR DEPOSIT? -25
NEW BALANCE: 94.5
CHECK OR DEPOSIT? -73.69
NEW BALANCE: 20.81
CHECK OR DEPOSIT? -8. 24
NEW BALANCE: 12.57
CHECK OR DEPOSIT? $5 \emptyset$
NEW BALANCE: 62.57
CHECK OR DEPOSIT?

Remember to enter checks as negative numbers.

At last! A deposit, and just in time!
And so on. Do you remember how to get out of this? If not, see frame 36.
14. Suppose we enter this program and then type RUN. Show the first seven numbers printed by the computer.

```
1\varnothing LET N = 1
20 PRINT N
3\varnothing LET N = N + 1
5ø GO TO 2\varnothing
```

RUN
$\square$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

How do we stop the computer from continuing to print numbers? $\qquad$
15. The U.S. is going metric, so here is a metric problem. Write a program to convert feet and inches to centimeters, as indicated by the following RUN. RUN

FEET $=$ ? 5
INCHES =? 11 CENTIMETERS $=18$ Ø. 34

FEET =? 3 INCHES =? $\quad 6$ CENTIMETERS $=91.44$

FEET = ?
And so on.

## Answers to Self-Test

The frame numbers in parentheses refer to the frames in the chapter where the topic is discussed. You may wish to refer to these for quick review.

1. This erases, or removes, any old program that might be in the computer's memory. If we don't do this, statements of an old program might be intermingled with statements of the new program, thus causing mysterious and unpredictable behavior when we try to RUN the new program. (frames 11, 12)
2. Type LIST and press the RETURN key. (frames 13, 14)
3. Type RUN and press the RETURN key. (frames 14,16 )
4. Type a new line numbered 20 and press the RETURN key. The old statement 20 is automatically erased and we may now replace it. If we type the line number (and only the line number) of a statement and press RETURN, the computer deletes from its memory the statement (if any) with that line number. (frame 21)
5. Direct statements do not have line numbers and are executed immediately after we press RETURN. A statement to be stored must have a line number; the computer "remembers" it for later execution (at "RUN time" as we sometimes say). (frame 9)
6. Press the BREAK key. (frames 34-36)
7. 

(a) 20 PRINT DISTANCE IN ONE TURN IS $3.14^{*} \mathrm{D}$ Quotation marks missing 20 PRINT "DISTANCE IN ONE TURN IS " ;3.14*D frames $(42,43)$
(b) $2 \not \varnothing^{\prime D}$ ISTANCE IN ONE TURN IS " ;3.14*D

PRINT is missing.

2ø PRINT "DISTANCE IN ONE TURN IS " ;3.14*D (frame 42)
(c) $2 \varnothing$ LET $P^{*}(1+R / 1 \varnothing \varnothing)^{\wedge} N=A$
$2 \varnothing$ LET $A=P^{*}(1+R / 1 \varnothing \varnothing)^{\wedge} N$
(d) 2ø TYPE " $X=$ "; $X$

20 PRINT "X="; $x$

Left side of $=$ must be only a variable. (frames 1-4)

Computer doesn't know what TYPE means.
8. (a) line number too big (frame 9)
(b) 3.14 is not a valid line number because it is not an integer in the range 1 to 65335 (frame 9)
(c) -100 is not a valid line number (frame 9)
(d) should not be a comma following the word INPUT (frame 31)
(e) should not be a comma at the end of the INPUT statement (INPUT statements with two or more variables have commas between variables.) (frame 31)
9. (a) The program does not have a line number 12. Therefore, the computer cannot execute the statement 40 GO TO 12. Instead, it will type ERROR- 12 AT LINE 40. (frames 33, 35, 36)
(b) The PRINT statement does not use the same variables assigned values in the first two statements. (In ATARI BASIC, the computer would print a 0 (zero) for the PRINT statement.) We probably should have done one of the following.

```
1\varnothingLET A = 7 1\varnothing LET X = 7
2ø LET B = 5 20 LET Y = 5
3\varnothing PRINT A + B 3ø PRINT }X+Y (frames 1-6
```

10. Here is the complete RUN.
```
RUN
A=? 7
B=? 5
A+B=12
```

This statement: $3 \varnothing$ PRINT " $A+B=" ; A+B$
Caused this: $\quad A+B=12$
(frame 42)
11. $10 \varnothing$ REM*** CONVERT CELSUIS TO FAHRENHEIT
$11 \varnothing$ PRINT "YOU ENTER DEGREES CELSUIS,"
12の PRINT "I WILL TYPE DEGREES FAHRENHEIT."
$13 \varnothing$ PRINT
$14 \varnothing$ PRINT "DEGREES CELSUIS";
158 INPUT C
160 PRINT "DEGREES FAHRENHEIT $=" ;(9 / 5) * C+32$
$17 \varnothing$ GOTO $13 \varnothing$
(frames 42, 43)
12. $1 \varnothing \varnothing$ REM***TV SHOW PRIZE PROBLEM
$11 \varnothing$ PRINT
$12 \varnothing$ PRINT "N=";
125 INPUT N
13ø PRINT "PRIZE Nø. $1=": N$
$14 \varnothing$ PRINT "PRIZE NØ. $2=" ; 1 . \emptyset 1^{\wedge} N$
150 GOTO $11 \varnothing$
(frames 42, 43)
13. $1 \varnothing \varnothing$ REM***CHECKBOOK BALANCING PROGRAM

```
    11\varnothing PRINT "I WILL HELP YOU BALANCE YOUR CHECKBOOK."
```

    \(12 \varnothing\) PRINT "ENTER CHECKS AS NEGATIVE NUMBERS AND"
    \(13 \varnothing\) PRINT "DEPOSITS AS POSITIVE NUMBERS."
    \(14 \varnothing\) PRINT
    \(15 \varnothing\) PRINT "OLD baLance";
    155 INPUT B
    \(16 \varnothing\) PRINT
    17ヵ PRINT "CHECK OR DEPOSIT";
    175 INPUT X
    189 LET B=B \(+\mathrm{x} \longleftarrow\) Compute new balance as shown below.
    \(19 \varnothing\) PRINT "NEW BALANCE: "; \(B\)
    2øø GOTO \(16 \varnothing\)
    $18 \varnothing$ LET $=$
(frames 47-49)
14. RUN This program illustrates a counting loop. Once you type

1
2
3
4
5
6
7 AND SO ON.

```
15. 1øø REM***CONVERT FEET AND inches to CENTIMETERS
110 PRINT
\(12 \varnothing\) PRINT "FEET \(=\) ";
125 INPUT \(F\)
\(13 \varnothing\) PRINT "INCHES \(=\) ";
135 INPUT I
\(14 \varnothing\) LET T \(=122^{*} \mathrm{~F}+\mathrm{I}\)
150 LET \(\mathrm{C}=2.54\) * T
\(16 \varnothing\) PRINT "CENTIMETERS \(={ }^{*} ; C\)
\(17 \varnothing\) GO TO \(11 \varnothing\)
T is total number of inches in F'I'.
C is total of centimeters in T".
```

(frame 42)

## CHAPTER FOUR

## Decisions Using IF-THEN Statements

By now you have probably gotten the idea that a computer only does what you very specifically tell it to do. So how can a computer ever decide anything on its own? Well, it can't decide 'on its own,'" but it can make certain comparisons that you instruct it to make, and then either execute or skip other statements in the program according to whether the comparison you specified is true or false. The statement that you use to set up such comparisons is the IF-THEN statement. (As you will see, IF-THEN is actually a whole family of statements.) When you finish this chapter, you will be able to:

- use the IF-THEN statement;
- use the following comparisons in an IF-THEN statement:

| Symbol | Meaning |
| :--- | :--- |
| $<$ | less than |
| $>$ | greater than |
| $=$ | equal to |
| $<>$ | not equal to |
| $>=$ | greater than or equal to |
| $<=$ | less than or equal to |

- use the RND function to generate random numbers;
- use the INT function to "drop" the fractional part of a number;
- use the INT and RND functions together to generate random digits;
- use the ON-GOTO statement to selectively branch to various statements in a program;
- use a colon (:) to separate multiple statements in the same line as a means to organize your programs and to save computer memory space;
- use multiple statements per line to increase the usefulness of IF- THEN statements.

1. In this chapter, we present a very important capability of BASIC-the ability to compare and decide. We will begin with the IF-THEN statement, which tells the computer to carry out a specified operation IF a given condition is TRUE. However, if the condition is FALSE (not true), the operation will not be done. An IF-THEN statement is shown below.
```
15\varnothing IF }X>>\varnothing\mathrm{ THEN PRINT "YOUR NUMBER IS POSITIVE"
```

This IF-THEN statement tells the computer: If the value of X is greater than zero, then print the message, YOUR NUMBER IS POSITIVE, and go on to the next statement in line number order. The symbol > means "is greater than."

If the value of X is less than zero or equal to zero, the computer does not print the message. Instead it simply continues executing the program in the line number order.

Here is another way to look at it. Follow the arrows.
The condition.


FALSE.
What is the condition in the above IF-THEN statement?
$\mathrm{X}>0$ or X is greater than zero
2. Using our sample statement from frame 1:
(a) Suppose $\mathrm{X}=3$. Is the condition TRUE or FALSE? $\qquad$
(b) Suppose $X=-7$. Is the condition TRUE or FALSE? $\qquad$
(c) Suppose $\mathrm{X}=0$. Is the condition TRUE or FALSE? $\qquad$
(a) TRUE. The computer will print the message: YOUR NUMBER IS POSITIVE.
(b) FALSE. The computer will not print the message.
(c) FALSE. The computer will not print the message.
3. The symbol > in an IF-THEN comparison means "is greater than." The symbol $=$ means "is equal to." You can guess that the symbol $<$ used in an IF-

THEN comparison means $\qquad$ .
$\qquad$
"is less than'"
4. Here is a simple program illustrating the use of the IF-THEN statement. This program has three IF-THEN statements that tell the computer to "compare and decide." Remember, the message in an IF-THEN PRINT statement will be printed only if the comparison is true.

```
1\varnothing\varnothing REM***DETERMINE IF X IS POSITIVE, NEGATIVE OR ZERO
11\varnothing PRINT "WHEN I ASK, YOU ENTER A NUMBER AND I""
12ø PRINT "WILL TELL YOU WHETHER YOUR NUMBER IS"
13ø PRINT "POSITIVE, NEGATIVE OR ZERO"
135 PRINT
14\varnothing PRINT "WHAT IS YOUR NUMBER";
145 INPUT X
15\emptyset IF X>\varnothing THEN PRINT "YOUR NUMBER IS POSITIVE"
16\varnothing IF X<\emptyset THEN PRINT "YOUR NUMBER IS NEGATIVE"
17\varnothing IF }X=\varnothing\mathrm{ THEN PRINT "YOUR NUMBER IS ZERO"
180 GOTO 135
RUN
WHEN I ASK, YOU ENTER A NUMBER AND I
WILL TELL YOU WHETHER YOUR NUMBER IS
POSITIVE, NEGATIVE OR ZERO
WHAT IS YOUR NUMBER? -7 «ఒ This message printed by line 160.
YOUR NUMBER IS NEGATIVE
WHAT IS YOUR NUMBER? 3 « This message courtesy of line 150.
YOUR NUMBER IS POSITIVE
WHAT IS YOUR NUMBER? ø « % Thank you, line 170.
YOUR NUMBER IS ZERO
WHAT IS YOUR NUMBER?
And so on. (Do you remember how to stop a program waiting at the INPUT question mark?)
```

(a) What is the condition in line 150 ?
(b) What is the condition in 160 ?
(c) What is the condition in line 170 ?
(a) $\mathrm{X}>0$ or X is greater than zero
(b) $\mathrm{X}<0$ or X is less than zero
(c) $\mathrm{X}=0$ or X is equal to zero
5. In running the program from frame 4, the computer executes lines 100 through 130 once, since they are "outside the loop." Lines 135 through 180 are included in the loop and are executed for each value of X supplied by the user after an INPUT question mark. Suppose the user runs the program and types 13 after the INPUT question mark, then presses RETURN. This assigns the value 13 to the variable $X$. Now look back at the program. Since $X=13$ ( 13 is the value of X), the condition in line 150 is TRUE and the conditions in lines 160 and 170 are FALSE. So, the computer will print the message in line 150 , but will not print the messages in lines 160 and 170.
(a) Suppose $\mathrm{X}=-7$. The condition in line 160 is (TRUE or FALSE)
$\qquad$ and the conditions in lines 150 and 170 are
(TRUE or FALSE) $\qquad$ .
(b) Suppose $\mathrm{X}=0$. Which condition is TRUE? (Give line number.) $\qquad$
Which conditions are FALSE? (Give line numbers.) $\qquad$
(a) TRUE; FALSE. The computer will print the message in line 160 , but will not print the messages in lines 150 and 170.
(b) line 170 ; lines 150 and 160. The computer will print the message in line 170 , but will not print the messages in lines 150 and 160 .
6. The program on the following page compares two numbers, A and $B$, and prints an appropriate message. Complete lines 160 and 170 so that the program will RUN as shown.

```
1\varnothing\varnothing REM***COMPARE TWO NUMBERS, A AND B
110 PRINT "WHEN I ASK, ENTER VALUES FOR A AND B."
12\emptyset PRINT
13ø PRINT "A = ";
135 INPUT A
140 PRINT "B = ";
145 INPUT B
15ø IF A>B THEN PRINT "A IS GREATER THAN B"
160 IF A<B
170
18\varnothing GOTO 12\varnothing
RUN
WHEN I ASK, ENTER VALUES FOR A AND B.
A =? 1
B =? 2
A IS LESS THAN B
A =? 7
B =? 2
A IS GREATER THAN B
A =? 55
B =? 55
A IS EQUAL TO B
A =?
160 IF A<B THEN PRINT "A IS LESS THAN B"
17\varnothing IF A=B THEN PRINT "A IS EQUAL TO B"
```


## 7. Let's look at another IF-THEN statement.

This statement:
19 IF $X=-1$ THEN GO TO $23 \varnothing$
Tells the computer: If the value of X is equal to -1 , then go to line 230 . If the value of X is not equal to -1 , the computer continues in usual line number order.

In general, the IF-THEN statement has the following form.

## IF condition THEN statement

The statement could be almost any BASIC statement. The condition is usually a comparison between a variable and a number, between two variables, or between two BASIC expressions. On the following page is a handy table of comparison symbols.

BASIC symbol
$=$
$<$
$>$
$<=$
$>=$
$<>$

Comparison
is equal to
is less than is greater than is less than or equal to
is greater than or equal to
is not equal to

Math symbol
$=$
$<$
$>$
$\leqq$
$\geqq$
$\neq$

Write each of the following conditions in proper BASIC.
(a) M is greater than 10.
(b) Z is less than or equal to A squared. $\qquad$
(c) X is not equal to Y .
(d) 3 times P is equal to Z times Q .

-     -         -             -                 -                     -                         -                             -                                 - 

(a) $\mathrm{M}>10$
(b) $\mathrm{Z}<=\mathrm{A}^{\wedge} 2$ or $\mathrm{Z}<=\mathrm{A}^{*} \mathrm{~A}$
(c) $\mathrm{X}<>\mathrm{Y}$
(d) $3^{*} \mathrm{P}=\mathrm{Z}^{*} \mathrm{Q}$
8. So far you have seen two members of the IF-THEN family of statements.

$$
\begin{array}{ll}
\text { IF-THEN PRINT } & \text { (message in quotes) } \\
\text { IF-THEN GOTO } & \text { (line number) }
\end{array}
$$

The second IF-THEN statement shown above tells the computer to branch or GOTO the line number given, if the comparison is true. You may omit the instruction GOTO following THEN, and just specify the line number. Show how you could write the following statement in shorter form.

```
190 IF }X=-1 THEN GOTO 23\varnothing
```

$\qquad$
$19 \varnothing$ IF $X=-1$ THEN $23 \varnothing$
9. Remember, the basic form of the IF-THEN statement is as follows. IF (condition) THEN (almost any BASIC statement)

Since almost any BASIC statement can follow THEN, we could have the computer assign a value or ask for an INPUT (provided that the condition or comparison is true) in an IF-THEN statement.

```
IF Y = 3 THEN LET X = 1
IF X*X + Y*Y<25 THEN PRINT "YOUR GUESS IS INSIDE THE CIRCLE"
```

It's your turn to practice writing the IF-THEN statements that will assign values if the comparison is true. From the following descriptions, write an IFTHEN statement.
(a) If A does not equal B then assign the new value 10 to variable B .
(b) IF H is more than 100, have the computer say "OOPS! TOO MANY HOURS."

(a) IF A<>B THEN B $=1 \varnothing$ (Remember, you can omit the LET in an assignment statement.)
(b) IF H>1øø THEN PRINT "OOPS! TOO MANY HOURS."
10. For each description, write an IF-THEN statement.
(a) If the value of A is less than or equal to 10 , go to line 100 .
(b) If A is less than $2^{*} \mathrm{~B}$, then increase the old value of T by 1 .
(c) If X is greater than 2 times Y , then print the message X IS MORE THAN Y DOUBLED.
(d) If Z does not equal -1 , then INPUT a new value for X .
(a) IF $A<=1 \varnothing$ THEN $1 \varnothing \varnothing$ (The GOTO is optional and usually omitted).
(b) IF A $<2 *$ B THEN $T=T+1$ or IF $A<2 * B$ THEN LET $T=T+1$
(The LET may be included or omitted.)
(c) IF $x>2$ * $y$ then PRint " $x$ is more than $y$ doubled"
(d) IF $z<>-1$ THEN INPUT $x$
11. One common use of the IF-THEN statement is to recognize a signal called a "flag"' that terminates one process and begins another. Here is another version
of the "World's Most Expensive Adding Machine"' which you first encountered in Chapter 3, frame 45. You may wish to review that frame before plunging onward.

```
1\varnothing\varnothing REM***WORLD'S MOST EXPENSIVE ADDING MACHINE
11\varnothing PRINT "I AM THE WORLD'S MOST EXPENSIVE ADDING"
12\varnothing PRINT "MACHINE. EACH TIME I TYPE 'X=?' YOU"
13\varnothing PRINT "TYPE A NUMBER. WHEN YOU ARE FINISHED,"
14% PRINT "TYPE - }1\mathrm{ AND I WILL TYPE THE TOTAL"
150 PRINT "OF YOUR PREVIOUS NUMBERS."
16\varnothing T = \varnothing
170 PRINT " Lines }170\mathrm{ through 220 are a GOTO loop. However, if
18\varnothing PRINT "X =" ; someone types -1 for the value of X, line 200 will
20\varnothing IF X=-1 THEN 23ø cause the computer to jump out of the loop and go to
210 T = T + X
220 GOTO 170
230 PRINT This section of the program tells the computer to
24\varnothing PRINT "TOTAL =" ; T print a line space, the total of the numbers, and then
25@ PRINT
26\varnothing GOTO 11ø
RUN
I AM THE WORLD'S MOST EXPENSIVE ADDING
MACHINE. EACH TIME I TYPE ' }X=/\prime' YOU
TYPE A NUMBER. WHEN YOU ARE FINISHED
TYPE -1 AND I WILL TYPE THE TOTAL
OF YOUR PREVIOUS INPUTS.
x =? 6.95
x =? . 47
X =? 8.49
X =? 3.ø6
x=?-1 «. Aha! Here is our flag saying "that's all folks."
TOTAL=18.97
I AM THE WORLD'S MOST EXPENSIVE ADDING And so on.
```

The flag used in our program is -1 ; statement 200 checks each and every input value of $X$ and, if it is -1 , causes the computer to jump out of the loop to line 230. Lines 230 through 260 print the total ( T ) and then cause the computer to jump back to line 110 and start over.

Any unusual number that will not be used as a normal INPUT value could be used as a flag.

Modify the program so that, instead of using -1 as the flag, we use 999999 as the flag. You will have to change lines 140 and 200
$\qquad$

```
14ø PRINT "TYPE 999999 AND I WILL TYPE THE TOTAL"
20\varnothing IF X=999999 THEN 23ø
```

12. In our program in frame 11 we first used -1 as the flag. This may not be a good idea if some of the values we wish to use are negative. For example, here are temperatures recorded during one cold week in Minneapolis, Minnesota.

| S | M | T | W | T | F | S |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 3 | -9 | -15 | -23 | -25 | -30 |

In this case, using 999999 as the flag would prevent confusion between a temperature of -1 and an end-of-data flag of -1 .

With a few changes, we can modify the program in frame 11 and obtain a program to compute the mean, or average, of a set of numbers. The formula for determining the mean of a set of N numbers is as follows.

$$
\text { Mean }=\frac{\text { Sum or total of the Numbers }}{\text { Number of Numbers }}=\frac{\mathrm{T}}{\mathrm{~N}}
$$

In the Friendly "Mean"' Progam, we use the variable T for the total (sum) of the numbers, and N for the number of numbers. Complete the program.

```
1ø\varnothing REM***A FRIENDLY 'MEAN' PROGRAM
11\varnothing PRINT "I WILL COMPUTE THE MEAN OF NUMBERS."
120 PRINT "WHEN I TYPE ' }X=\mathrm{ ? TYPE A NUMBER. WHEN"
13ø PRINT "FINISHED ENTERING NUMBERS, TYPE 999999"
14\varnothing LET T=\varnothing
15@ LET N= We will use N to count the
16@ PRINT
17\varnothing PRINT "X = ";
175 INPUT X
180 IF X=999999 THEN 220
190 LET T=T+X
20\emptyset LET N=
Increase the count by one.
21\varnothing GOTO 16\emptyset
22ø PRINT
23ø PRINT "N = "; _ First, print the number of
24D PRINT "TOTAL = "; T numbers.
25ø PRINT "MEAN = "; Compute and print the
26\varnothing PRINT
270 GOTO 110 numbers.
160 PRINT
170 PRINT "X \(=\) ";
175 INPUT \(X\)
19 Ø LET \(T=T+X\)
200 LET N= Increase the count by one.
\(21 \varnothing\) GOTO 160
220 PRINT
\(23 \varnothing\) PRINT "N = "; First, print the number of
250 PRINT "MEAN = ";
```

Compute and print the mean.

The RUN is on the next page.

```
RUN
I WILL COMPUTE THE MEAN OF NUMBERS.
WHEN I TYPE 'X =?' TYPE A NUMBER. WHEN
FINISHED ENTERING NUMBERS, TYPE 999999.
X =? 10
x =? 3
X =? -9
x =? -15
x =? -23
x =? -25
x =? -3ø
X=? 999999 «
N=7 N
TOTAL =-89 That was the cold week that was, or yes, that was a
MEAN =-12.71428571 mean week.
15\varnothing LET N=\varnothing
2\varnothing\varnothing LET N=N+1
23\varnothing PRINT "N = ";N
25ø PRINT "MEAN = "; T/N
```

13. For temperatures in Minneapolis, 999999 is a good flag. We assume, of course, that the temperature never reaches 999999 degrees, even in the summer. For other types of data, 999999 may not be a good flag. One of the most outrageous and least likely BASIC numbers we can think of is the floating point number, 1E97. For most data, 1 E 97 would be a good flag. So, modify lines 130 and 180 in the program of frame 12 so that the flag is 1 E 97 .

130
180

```
130 PRINT "FINISHED ENTERING NUMBERS, TYPE 1E97."
18\varnothing IF X=1E97 THEN 22\varnothing
```

14. You have helped us write several computer programs using IF-THEN comparisons. Now it is time for you to do a solo flight and write a program on your own. Think carefully about the use of IF-THEN comparisons, and what the computer will do if the conditions are TRUE or if they are FALSE. On the following page is a RUN of the program we want you to write.
```
RUN
INPUT A NUMBER AND I WILL TELL YOU IF
IT IS 1\varnothing\varnothing OR LESS, OR OVER 1\varnothing\varnothing.
YOUR NUMBER? }9
YOUR NUMBER IS 1ø\emptyset OR LESS.
YOUR NUMEER? 1\varnothing1
YOUR NUMBER IS OVER 1ø\emptyset.
YOUR NUMBER? 1\varnothing\varnothing
YOUR NUMBER IS 1\varnothing\varnothing OR LESS.
YOUR NUMBER?
```

Now you write the program.

```
1ø\varnothing REM***NUMBER SIZE PROGRAM
11\varnothing PRINT "INPUT A NUMBER AND I WILL TELL YOU IF"
12\varnothing PRINT "IT IS 1\varnothing\varnothing OR LESS, OR OVER 1\varnothing\varnothing."
130 PRINT
14\varnothing PRINT "YOUR NUMBER";
145 INPUT N
15\varnothing IF N <= 1\varnothing\varnothing THEN PRINT "YOUR NUMBER IS 1\emptyset\varnothing OR LESS.
16\varnothing IF N>1\varnothing\varnothing THEN PRINT "YOUR NUMBER IS OVER 1\varnothing\varnothing."
17\varnothing GOTO 13&
```

15. Soon we will enter the fun-filled realm of computer games. But first, you should learn about random numbers and the unpredictable BASIC function known as RND.

Random numbers are numbers chosen at random from a given set of numbers. Many games come with dice or a spinner or some other device for generating random numbers. Roll the dice; they come up 8 . Move 8 spaces.

Functions are automatic features of BASIC that you use to perform special operations. These functions are like built-in programs; most of them could be replaced by a program or segment of a program. However, computers are called upon often enough to do the operations accomplished by these functions that it is worthwhile to "build them in" to the computer language.

BASIC provides a special function, called the RND function, that generates numbers that seem to be chosen at random, like picking numbers out of a hat. The program on the following page shows the use of the RND function. We
show you the program (enclosed in a box) and two different runs of that program. We interrupted the first RUN by pressing BREAK, then typed RUN again.

```
1\varnothing PRINT RND(1)
2\varnothing GOTO 1\varnothing
RUN RUN
0.2772064208 Ø.4468536376
\emptyset.0455932617 Ø.2126617431
\varnothing.6158294677 Ø.75856ø18ø6
\varnothing.ø782165524 Ø.5531ø05859
0.2481689453 Ø.1878662109
\varnothing.1948242187 ø.0785217285
\varnothing.9686126708 6.83401722E-Ø3
\varnothing.5149536132 Ø.2ø4711914
\varnothing.8614654541 STOPPED AT LINE 10
STOPPED AT LINE 1\varnothing
We pressed BREAK
We pressed BREAK
```

Two runs of the program are shown. Are the lists of random numbers in the two runs the same? $\qquad$

-     -         -             -                 -                     -                         -                             - 

No. In fact, don't expect to enter our program into your computer, type RUN, and get either list. That's the idea of random numbers. They are, well, random!
16. The statement 10 PRINT RND(1) causes the computer to produce a different list of random numbers each time the program is RUN. The RND function generates numbers that appear to be chosen at random. On our ATARI computer, the RND function is written RND(1).

We use the number 1 in parentheses. However, any positive number is OK, even numbers with decimal fractions! On our computer, a positive number in parentheses following RND will cause the computer to produce a different list of random numbers each time.

Examine the random numbers in frame 15.
(a) Is any number less than zero (negative)? $\qquad$
(b) Is any number equal to zero? $\qquad$
(c) Is any number greater than one? $\qquad$
(d) Is any number equal to one? $\qquad$
(e) From the evidence, it appears that random numbers produced by the RND function are $\qquad$ zero and $\qquad$ one.
(a) no
(b) no
(c) no
(d) no
(e) greater than; less than. However, we haven't shown much evidence-only a few random numbers. We suggest you run off a bunch of random numbers on your computer in order to get more evidence. (But remember! Evidence is not proof.)
17. It's true that random numbers produced by the RND function are greater than zero and less than one. Another way to say it: random numbers produced by the RND function are between 0 and 1 . Or, in still another way: $0<$ RND(1) $<1$.

However, random numbers between 0 and 1 are not always convenient. Sometimes we would like random digits (the numbers $0,1,2,3,4,5,6,7,8$, and 9 ) or random integers (whole numbers) from 1 to 100 . Below is a RUN in which the computer acts as a teaching machine to teach one-digit addition to children.
RUN

$7+2=? 9$
RIGHT ON...GOOD WORK!:!
$8+\varnothing=$ ?

New problem. . . . And so on.

Undoubtedly, you are anxious to see the program. Patience! Let's build it, piece by piece. First, how do we generate random digits?

The random numbers produced by the RND function are uniformly distributed between 0 and 1 . That is, they are "spread evenly" between 0 and 1. Each random number is about as likely (or unlikely) to occur as any other random number.
$\operatorname{RND}(1)$ is between 0 and 1 , but is never 0 or 1 . Therefore, $10 * \operatorname{RND}(1)$ is between 0 and $\qquad$ .

10 BUT 10*RND(1) is never equal to zero or ten.
18. Below is a program to print random numbers between 0 and 10 . We show you two RUNs to remind you that you get a different list each time.

```
1\varnothing PRINT 1涘RND(1)
2ø GOTO 1\varnothing
```

RUN
7.00805664
8.13720703
2.74749755
6.07574462
3. 90029907

1. $66 \varnothing \varnothing 0366$
4.94537259
ø. 382461547
6.671295166
4.277496337 STOPPED AT LINE $1 \varnothing$
STOPPED AT LINE $1 \varnothing$

Each random number in the runs is greater than zero and less than ten. Each random number can be thought of as having an integer part to the left of the decimal point and a fractional part to the right of the decimal point.

The integer part of 7.00805664 is 7 and the fractional part is .00805664 .
The integer part of 0.382461547 is zero (0). The fractional part is .382461547.
(a) What is the integer part of 1.66000366 ? $\qquad$
The fractional part? $\qquad$
(b) What is the integer part of 4.83612061 ? $\qquad$
The fractional part? $\qquad$
_ - - - - - - - -
(a) 1;. 66000366
(b) $4 ; .83612061$
19. Now you write three short programs to print random numbers in the ranges specified.
(a) between 0 and 100
(b) between 0 and 50
(c) between 0 and 6

| (a) | $1 \varnothing$ PRINT 1øø*RND(1) <br> $2 \varnothing$ GOTO $1 \varnothing$ |
| :---: | :---: |
|  | RUN |
|  | 73.3308125 |
|  | 12.7318066 |
|  | 37.9114539 |
|  | 87.8885027 |
|  | 2.109360ø1 |
|  | 20.1256433 |
|  | 69.5790782 |
|  | 4.26022968 |
| (c) | $1 \varnothing$ PRINT 6 *RND (1) |
|  | $2 \varnothing$ GOTO $1 \varnothing$ |
|  | RUN |
|  | 2.60018182 |
|  | 1.31444039 |
|  | 3.24057255 |
|  | ๑. 1153584267 |
|  | ๑. $\varnothing 2287558154$ |
|  | 2.90792334 |
|  | 5.72100528 |
|  | $2.832169 \varnothing 4$ |

(a) $1 \varnothing$ PRINT $1 \varnothing \varnothing$ *RND (1)
$2 \varnothing$ GOTO $1 \varnothing$

RUN
73.3388125
12.7318066
87.8885027
2. $109360 \varnothing 1$
20.1256433
4.26022968
(c) $1 \varnothing$ PRINT $6 *$ RND (1) 2ø GOTO $1 \varnothing$

RUN

1. 31444030
3.24057255
๑. 1153584267
Ф. 82287558154
2.90792334
2.ø32169ø4
(b) $1 \varnothing$ PRINT $5 \varnothing$ *RND (1) $2 \varnothing$ GOTO $1 \varnothing$

## RUN

28.9513492
35.5718117
44.6059096
11.4345026
6.48894357
15.2396084
20. For each random number between 0 and 10 , the integer (whole number) part is a single digit. Wouldn't it be nice if we could direct the computer to delete the fractional part and keep the integer part?

Well, as you may suspect, we can. BASIC has another clever and useful function called INT. Here are some examples.

| INT $(3)=3$ | INT (7) = 7 |
| :--- | :--- |
| INT $(3.14159)=3$ | INT (7.99999) $=7$ |
| INT $(1.23456)=1$ | INT $(.999999)=0$ |

(Say it like this: "The integer part of 3.14159 is 3. '')
In general, if X is any positive number, $\operatorname{INT}(\mathrm{X})$ is the integer part of X . Now, you apply INT to some of the random numbers from frame 18.
(a) $\operatorname{INT}(7.00805664)=$ $\qquad$ (b) $\operatorname{INT}(0.382461547)=$ $\qquad$
(c) INT $(2.74749755)=$ $\qquad$ (d) $\operatorname{INT}(9.85137939)=$ $\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

(a) 7
(b) 0
(c) 2
(d) 9
21. Caution. INT works as shown in frame 20 only for positive numbers or zero. In general, INT(X) computes the greatest integer less than or equal to $X$. For example:

| INT (3.14) $=3$ | but | INT $(-3.14)=-4$ |
| :--- | :--- | :--- |
| INT (7) $=7$ | and | INT $(-7)=-7$ |
| INT $(.999)=0$ | but | INT $(-.999)=-1$ |

For positive numbers, or zero, INT (X) computes the integer part of X . In a program, the value assigned to X will be substituted for X in the INT parentheses when the program is RUN. The computer then performs the INT function on the numerical value. Of course, any variable could be used instead of the letter X , as long as it has been assigned a value earlier in the program.

You be the computer and show what you will print when your human tells you to RUN the following programs.
(a) $18 \quad \mathrm{X}=15.77$
2. PRINT INT( $x$ )
RUN
(b) $10 \mathrm{~A}=99.999$ 2ø PRINT INT(A) RUN
(c) $1 \varnothing \mathrm{~F}=98.6$ $2 \varnothing$ PRINT INT (F) RUN
(a; 15; (b) 99; (c) 98
22. Instead of a number, we can write a variable, a function, or any BASIC expression in the parentheses that follow the word INT.

INT( )
-Any BASIC number, variable, function or expression here
You should be able to distinguish between values, variables, expressions, functions, and strings. To show that you can, identify each of the following with one of the words given above in italics.
(a) X
(b) $\mathrm{X}^{*} 2$
(c) $\mathrm{RND}(1)$
(d) "A + B IS AN EXPRESSION"
(e) 22
(f) $1+1$
(g) $\quad \operatorname{INT}(52.88)$
(h) " = "
(i) $4^{*}(3+\mathrm{X})$
(j) Which of the above could be used in the parentheses of a function such as INT or RND? $\qquad$
(a) variable
(b) expression
(c) function
(d) string
(e) value
(f) expression
(g) function
(h) string
(i) expression
(j) a, b, c, e, f, g, and i
23. Remember, the general form for the INT function is as follows.

INT( )
Any BASIC number, variable, function or expression here
So, it is OK to write INT(10*RND(1)). This is an expression containing a function as part of the expression.
$\mathrm{RND}(1)$ is a random number between 0 and 1.
$10 * \operatorname{RND}(1)$ is a random number between 0 and 10 .
$\mathrm{INT}\left(10^{*} \mathrm{RND}(1)\right)$ is a random digit.
The program on the following page causes the computer to generate and print random digits. Digits are the numbers $0,1,2,3,4,5,6,7,8$, and 9 , or 0 to 9 , inclusive. Note the "inclusive" means it includes both 0 and 9 , as well as the digits between 0 and 9 .


This program prints random digits, which are integers from $\qquad$
to _ , inclusive.


0; 9
24. Now write a short program to print random integers (whole numbers) from 0 to 19 , inclusive. Our RUN looks like this.


-     -         -             -                 -                     -                         -                             -                                 - 

```
1\emptyset PRINT INT(2目RND(1))
```

$2 \varnothing$ GOTO $1 \varnothing$

Be sure to match the parentheses. There must be a right, or closing, parenthesis for every left, or opening, parenthesis; if not, the computer will give you an error message when you RUN the program.
25. What if we want random integers from 1 to 20 , inclusive, instead of from 0 to 19 ? Well, that's easy. Simply add a 1 to the random integer. You could do it in two ways.

```
1\varnothing PRINT INT(2目RND(1)+1)
2\varnothing GOTO 1\varnothing
```

```
Or 1\varnothing PRINT INT(2苜RND(1))+1
2\varnothing GOTO 1\varnothing
RUN
    14
    2\varnothing
    2\varnothing
    16
    1 9
    7
    2\varnothing
    2
    1 5
```

The " +1 " can be added to the random number either before or after taking the integer part of $20^{*} \mathrm{RND}(1)$. The resulting random integer will be the same in either case.

Now you write three simple programs to print a list of random integers.
(a) from 1 to 10 , inclusive
(b) from 1 to 100 , inclusive
(c) from 1 to 12, inclusive
(a) $1 \varnothing$-PRINT INT( $1 \varnothing^{*}$ RND (1) ) +1 Or $1 \varnothing$ PRINT INT( $\left.1 \varnothing^{*} \operatorname{RND}(1)+1\right)$ $2 \varnothing$ GOTO $1 \varnothing$
$2 \emptyset$ GOTO $1 \varnothing$
(b) $1 \varnothing$ PRINT $\operatorname{INT}\left(1 \varnothing \varnothing^{*} \operatorname{RND}(1)\right)+1$ Or $1 \varnothing$ PRINT INT(1øø*RND(1)+1)
$2 \varnothing$ GOTO $1 \varnothing$
$2 \varnothing$ GOTO $1 \varnothing$
(c) $1 \varnothing$ PRINT INT(12*RND(1))+1 Or $1 \varnothing \operatorname{PRINT} \operatorname{INT}(12 * R N D(1)+1)$
$2 \varnothing$ GOTO $1 \varnothing \quad 2 \varnothing$ GOTO $1 \varnothing$
26. What if we want random integers from 5 to 10 inclusive? Here is a hint: to get random integers from 1 to 10 instead of 0 to 9 , we added $a+1$. Look at it like this.

$$
\begin{array}{r}
0 \text { to } 9 \\
+\quad+1 \\
\hline 1 \text { to } 10
\end{array}
$$

(a) The function INT (6*RND(1)) will generate what random digits? $\qquad$
(b) What should we add to this expression INT(6*RND(1)) in order to generate integers from 5 to 10 inclusive? $\qquad$
(c) What should we add in order to generate integers from 11 to 16 inclusive?
$\qquad$
$\qquad$
(a) 0 to 5 inclusive, that is, $0,1,2,3,4$, and 5 , a total of 6 digits.
(b) +50 to 5

$$
\begin{array}{rr}
+5 & +5 \\
\hline 5 & 10
\end{array}
$$

(c) +110 to 5

$$
\begin{array}{rr}
+11 & +11 \\
\hline 11 & 16
\end{array}
$$

27. Look back at the RUN in frame 17 before we continue. Now we are ready to build the addition practice program. Here is the first section of the program that produced the RUN.
```
1\varnothing\varnothing REM***ADDITION PRACTICE PROGRAM
2\emptyset\emptyset REM***GENERATE RANDOM NUMBERS, A AND B
210 LET A=INT(1\varnothing*RND(1))
22\emptyset LET B=INT(10*RND(1))
```

The values of $A$ and $B$ will be $\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

random digits $(0,1,2,3,4,5,6,7,8$, or 9$)$
28. Ready for the next piece? Here we go.

```
3ø\emptyset REM***PRINT PROBLEM AND ASK FOR ANSWER
310 PRINT
32ø PRINT A; " + " ; B; " = " ;
330 INPUT C
```

Line 320 is something new. The statement PRINT A; " + '"; B; " = "; tells the computer to print the value of A, then print + , then print the value of $B$, then print $=$. These items are separated by semicolons. The fourth semicolon, at the very end, tells the computer not to go to the next line down on the CRT. In other words, it tells the computer to stay where it stopped printing.

Do you remember? The INPUT statement causes the computer to print a question mark. This question mark will be printed on the same line as the information from the PRINT statement, because of that semicolon at the end of line 320.

For example, if $\mathrm{A}=7$ and $\mathrm{B}=5$, then lines 320 and 330 will cause the computer to print the following.
from line 320 ( from line 330 (INPUT question mark)

If $A=3$ and $B=4$, what will be printed by lines 320 and 330 ? $\qquad$

```
---- - - - - -
\(3+4=\) ? (This, of course, is the random problem which helps the eager young learner practice addition.)
```

29. After the learner types an answer and presses the RETURN key, the computer assigns the answer value to variable $C$ and continues.

Note how we are using REM (REMARK) statements to tell something about each piece of the program. This doesn't help the computer, but it does help people read and understand how the program works.

```
4\emptyset\varnothing REM***IS THE ANSWER CORRECT?
410 IF C=A + B THEN 61\varnothing
```

If the student's answer (C) is correct, the computer will go to line $\qquad$

610 (If the answer is not correct, the computer continues in regular line number order.)
30. If the student's answer is not correct, then the IF-THEN condition is false. The computer next does the following as it continues on in the program in line number order.

```
5@\varnothing REM***ANSWER IS NOT CORRECT
51\varnothing PRINT "HMMM...I GET A DIFFERENT ANSWER."
52ø GOTO 31\varnothing
```

Assume an incorrect answer. The computer prints HMMM . . . I GET A DIFFERENT ANSWER, then goes to line 310. From there (check previous frames if necessary), what happens next?

-     -         -             -                 -                     -                         -                             - 

The computer repeats the problem.
Note: In a previous book, we had the computer type YOU GOOFED. TRY

AGAIN. Now that we know more about learners, we wish to make the computer seem friendly and compassionate, rather than nasty and authoritarian. Remember that what the computer "says" depends on the person who writes the program, and not the machine itself.
31. Review frame 29, which shows lines 400 and 410 of the program. If the learner's answer is correct, line 410 causes the computer to go to line 610.

```
60ø REM***ANSWER IS CORRECT
61\varnothing PRINT "RIGHT ON...GOOD WORK!!!"
620 GOTO 21ø
```

Assume a correct answer. The computer prints RIGHT ON . . . GOOD WORK!!! and then goes to line 210. What happens next?

The computer generates a new problem (new values for A and B ) and prints the new problem.
32. Below is a listing of the complete ADDITION PRACTICE PROGRAM.

```
1ø\varnothing REM***ADDITION PRACTICE PROGRAM
2ø\varnothing REM***GENERATE RANDOM NUMBERS, A AND B
21\varnothing LET A=INT(1\varnothing*RND(1))
22\varnothing LET B=INT(1\varnothing*RND(1))
3ø\varnothing REM***PRINT PROBLEM AND ASK FOR ANSWER
31\varnothing PRINT
32ø PRINT A; " + " ; B; " = ";
33ø INPUT C
4ø\emptyset REM***IS THE ANSWER CORRECT?
410 IF C=A+B THEN 610
5\emptyset\emptyset REM***ANSWER IS NOT CORRECT
51\varnothing PRINT "HMMM...I GET A DIFFERENT ANSWER."
52ø GOTO 31ø
6Ø\varnothing REM****ANSWER IS CORRECT
616 PRINT "RIGHT ON...GOOD WORK!!!"
620 GOTO 21ø
```

Change line 210 so that the value of A is a random integer from 0 to 19 , inclusive, instead of 0 to 9 .

```
210 LET A =
```

$\qquad$
$21 \varnothing$ LET $A=\operatorname{INT}\left(2 \not \varnothing^{*} \operatorname{RND}(1)\right)$
33. Careful on this one! Change line 220 so that the value of $B$ is a random inreger from 10 to 20 , inclusive.

```
22\varnothing LET B =
```

$\qquad$

```
- - - - - - - - - - 
22.6 LET B=INT(11*RND(1))+10
```

That gives us 10 to 20 inclusive, eleven numbers in all.

$$
\begin{array}{r}
0 \text { to } 10 \\
+10 \quad+10 \\
\hline 10 \text { to } 20
\end{array}
$$

We changed lines 210 and 220 of the program in frame 32 to look like the answer to frame 32 , and ran the modified program. Remember, a RUN on your computer will probably show different numbers in the problems. These are random numbers, after all.

RUN

```
    16 + 14 =? 30
RIGHT ON...GOOD WORK!!!
    16 + 15 =? 31
RIGHT ON...GOOD WORK!!!
    4+1\varnothing =? 15
HMMM...I GET A DIFFERENT ANSWER.
    4+1\varnothing =? 14
RIGHT ON...GOOD WORK!!!
6 + 16 =? And so on.
```

34. When the learner's answer is correct, the computer always prints: RIGHT ON . . . GOOD WORK!!! To relieve the monotony, let's modify the program so that the computer selects at random from three possible replies to a correct answer. The changes are in the portion of the program beginning at line 600.
```
6øD REM***ANSWER IS CORRECT
61\varnothing LET R=INT(3*RND(1))+1 « Note the +1.
62\varnothing IF R=1 THEN 630
621 IF R=2 THEN 65\varnothing
6 2 2 ~ I F ~ R = 3 ~ T H E N ~ 6 7 \varnothing ~
63ø PRINT "RIGHT ON...GOOD WORK!!!"
64\emptyset GOTO 21\varnothing
650 PRINT "YOU GOT IT! TRY ANOTHER."
660 GOTO 21\varnothing
67\varnothing PRINT "THAT'S GREAT! KEEP IT UP!"
68\emptyset GOTO 21\varnothing
```

The possible values of R are $\qquad$ , and $\qquad$ .

1,2 , and 3 (Not 0,1 , and 2 , because we added +1 at the end of line 610.)
35. So, we see, R can be 1 or 2 or 3 .
(a) If $\mathrm{R}=1$, the computer will print $\qquad$
(b) If $\mathrm{R}=3$, the computer will print $\qquad$
(c) If $\mathrm{R}=2$, the computer will print $\qquad$

-     -         -             -                 -                     -                         -                             - 

(a) RIGHT ON...GOOD WORK!!!
(b) THAT'S GREAT! KEEP IT UP!
(c) YOU GOT.IT! TRY ANOTHER.
36. We made the changes in response (frame 34) from the original program (frame 32) and ran the modified program. Here is what happened.

```
RUN
    9+7=? 16
THAT'S GREAT! KEEP IT UP!
    6+3=? 9
YOU GOT IT! TRY ANOTHER.
    8+2=? 1\varnothing
THAT'S GREAT! KEEP IT UP!
    5 + 9 =? 14
RIGHT ON...GOOD WORK!!!
    0+7=? 7
RIGHT ON...GOOD WORK!!!
    8+5 =? 14
HMMM...I GET A DIFFERENT ANSWER.
    8+5=?
```

If the learner's answer is incorrect, the computer always prints: HMMM . . . I GET A DIFFERENT ANSWER. Modify the program in frame 32 so that, for an incorrect response, the computer selects randomly one of the two following responses.

```
    HMMM...I GET A DIFFERENT ANSWER
    TRY A DIFFERENT ANSWER. GOOD LUCK!
500 REM***ANSWER IS NOT CORRECT
51% LET R=
52.0 IF
```

```
530 IF
540 PRINT
55ø GOTO 31\varnothing
560
57\varnothing GOTO 31\varnothing
- - - - - - - - - 
5\varnothing\varnothing REM***ANSWER IS NOT CORRECT
51\varnothing LET R=INT(2*RND(1))+1
52\varnothing IF R=1 THEN 54\varnothing
53\varnothing IF R=2 THEN 56\varnothing
54\varnothing PRINT "HMMM...I GET A DIFFERENT ANSWER."
55\varnothing GOTO 31\varnothing
560 PRINT "TRY A DIFFERENT ANSWER. GOOD LUCK!"
57\varnothing GOTO 31\varnothing
```

Again, we are trying to make the computer seem friendly and helpful, instead of harsh and unforgiving.
37. The three statements: 628 IF $\mathrm{R}=1$ THEN 638
621 IF $R=2$ THEN $65 \%$
622 IF R=3 THEN $67 \varnothing$
can be replaced by a single statement.


With this change, the program segment in frame 34 can be rewritten as follows.

```
6\emptyset\emptyset REM***ANSWER IS CORRECT
610 LET R=INT(3*RND(1))+1
620 ON R GOTO 630,650,670
63\varnothing PRINT "RIGHT ON...GOOD WORK!"
640 GOTO 21\varnothing
650 PRINT "YOU GOT IT! TRY ANOTHER."
660 GOTO 21\varnothing
67\varnothing PRINT "THAT'S GREAT! KEEP IT UP!"
68D GOTO 21\varnothing
```

(a) Look at line 610. What are the possible values of R?
(b) Suppose, during a RUN, the random number generated by RND (1) in line 610 is .34319 . What value will $R$ have?
(c) In this case, which line will the ON R GOTO statement send the computer to? $\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

(a) $1,2,3$
(b) $2, \operatorname{INT}\left(3^{*} .34319\right)+1=\operatorname{INT}(1.02957)+1=1+1=2$
(c) line 650
38. In general, the ON . . . GOTO statement has the following form.

ON $e$ GOTO $\ell_{1}, \ell_{2}, \ell_{3}, \ldots, \ell_{n}$
Where $e$ can be any BASIC expression and $\ell_{1}, \ell_{2}, \ell_{3}, \ldots, \ell_{n}$ are line numbers. Valid values for $e$ are integers 1,2,3 .., $n$. If $e=1$, the computer goes to line $\ell_{1}$. If $e=2$, the computer goes to $\ell_{2}$. And so on.

Use an ON . . . GOTO to replace the two IF statements (lines 520 and 530) in our solution to frame 36.

```
5\varnothing\varnothing REM***ANSWER IS NOT CORRECT
51\varnothing LET R=INT(2*RND(1))+1
52\varnothing ON
54\varnothing PRINT "HMMM...I GET A DIFFERENT ANSWER."
55\varnothing GOTO 31\varnothing
56\varnothing PRINT "TRY A DIFFERENT ANSWER. GOOD LUCK:"
57\varnothing GOTO 31\varnothing
```

$52 \varnothing$ ON R GOTO 54』,56ø
39. And now, a wonderful space saving method! Here is the first part of our addition practice program, featuring multiple statements per line.

```
1ø\varnothing REM***ADDITION PRACTICE PROGRAM
2\varnothing\varnothing REM***GENERATE RANDOM NUMBERS, A AND B
210 LET A=INT(20*RND(1))
22\varnothing LET B=INT(11*RND(1))+1\varnothing
3ø\varnothing REM***PRINT PROBLEM AND ASK FOR ANSWER
31\varnothing PRINT : PRINT A; " + " ; B; " = " ; : INPUT C
4\emptyset\emptyset REM***IS THE ANSWER CORRECT?
41\varnothing IF C=A+B THEN 6\varnothing\varnothing
5\emptyset\emptyset REM***ANSWER IS NOT CORRECT
51\varnothing LET R=INT(2*RND(1))+1
52\varnothing ON R GOTO 54\varnothing,56\varnothing
54\emptyset PRINT "HMMM...I GET A DIFFERENT ANSWER." : GOTO 31\varnothing
56\varnothing PRINT "TRY A DIFFERENT ANSWER. GOOD LUCK!": GOTO 31\varnothing
```

Lines 540 and 560 each have 2 statements per line.

In the program, line 310 contains three statements, and lines 540 and 560 each contain two statements. In a line that contains more than one statement, what symbol, or character, is used between statements? $\qquad$

a colon (:)

40. For readability, we usually put a space on each side of the colon. However, this is not necessary. For example, we could have typed line 310 as shown below.

```
31\varnothing PRINT:PRINT A; " + "; B; " = ";:INPUT C
```

However, we will include spaces to make the statements easier to read. The computer understands either way.

We didn't show you the entire program in the last frame, because we want you to rewrite the part of the program beginning with line 600 as shown in frame 37, using multiple statements in those lines where it makes sense to group statements to work together.

```
6ø』 REM***ANSWER IS CORRECT
610 LET R=INT(3*RND(1))+1
62\varnothing ON R GOTO 630,64%,65\emptyset
630
640
650
------
630 PRINT "RIGHT ON...GOOD WORK!!!" : GOTO 21ø
64@ PRINT "YOU GOT IT! TRY ANOTHER." : GOTO 210
650 PRINT "THAT'S GREAT! KEEP IT UP!" : GOTO 21ø
```

41．Here is the computer game we promised you earlier in the chapter．Note the use of multiple statements per line in lines $150,160,170$ ，and 180.

```
1\varnothing\varnothing REM***GUESS MY NUMBER - A COMPUTER GAME
11\varnothing LET X=INT(1\varnothing凤*RND(1))+1
12\emptyset PRINT
13\varnothing PRINT "I'M THINKING OF A NUMBER FROM 1 TO 1\varnothing\varnothing"
14\varnothing PRINT "GUESS MY NUMBER!"
150 PRINT : PRINT "YOUR GUESS" ; : INPUT G
16\varnothing IF G < X THEN PRINT "TRY A BIGGER NUMBER." : GOTO 15\varnothing
17\varnothing IF G > X THEN PRINT "TRY A SMALLER NUMBER." : GOTO 15@
18\varnothing IF G = X THEN PRINT "THAT'S IT! YOU GUESSED MY NUMBER!" : GOTO 11\varnothing
RUN
I'M THINKING OF A NUMBER FROM A TO 1\varnothing\varnothing.
GUESS MY NUMBER!
YOUR GUESS? 5%
TRY A BIGGER NUMBER.
YOUR GUESS? }7
TRY A SMALLER NUMBER.
YOUR GUESS? 68
TRY A BIGGER NUMBER.
YOUR GUESS? }7
TRY A BIGGER NUMBER.
YOUR GUESS? }7
THAT'S IT! YOU GUESSED MY NUMBER!
I'M THINKING OF A NUMBER FROM 1 TO 1\varnothing\varnothing.
GUESS MY NUMBER!
YOUR GUESS?
And so on．
```

Line 110 tells the computer to generate a random number and store it in variable X ．This number will be $\mathrm{a}(\mathrm{n})$ $\qquad$ from $\qquad$ to $\qquad$ ＿．
－ーー———————
integer（or whole number）；1； 100

42．Multiple statements per line give us another nice shortcut．You＇ll recall that if the comparison in an IF－THEN statement is false，the computer skips the rest of the statement and goes on to the next line in the program in line number order．The nice thing is that the computer will also skip any statements that follow a false IF－THEN comparison if they are on the same multiple statement line．The rest of the statements on a line will be executed if the IF－THEN com－ parison is true．Therefore，in one line，you can have the computer do more than one thing if an IF－THEN comparison is true．Consider line 170 as it is shown on the following page．The computer will both PRINT and GOTO if the condition
is true, but it won't do either if the condition is false.


The condition is: $\mathrm{G}>\mathrm{X}$
(a) Suppose $G=90$ and $X=73$. Is the condition TRUE or FALSE? $\qquad$
(b) Suppose $\mathrm{G}=70$ and $\mathrm{X}=73$. Is the condition TRUE or FALSE? $\qquad$
(c) Suppose $\mathrm{G}=73$ and $\mathrm{X}=73$. Is the condition TRUE or FALSE? $\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

(a) TRUE; (b) FALSE; (c) FALSE
43. Line 150 causes the computer to print YOUR GUESS? When the player types a guess, the computer stores it in variable G. Lines 160, 170, and 180 compare the guess G with the random number X. Let's look at line 160.

```
16\varnothing IF G < X THEN PRINT "TRY A BIGGER NUMBER.": GOTO 15\varnothing
```

If the guess $G$ is less than the number $X$, the computer will print the message TRY A BIGGER NUMBER and will then GOTO line 150 to ask for another guess. However, if G is greater than X or equal to X , neither the PRINT nor the GOTO will be done. Here is another way to "picture" that idea.


So, if $\mathrm{G}<\mathrm{X}$ is FALSE, the computer goes on to line 170 . Describe what happens when the computer executes line 170.

```
17\varnothing IF G > X THEN PRINT "TRY A SMALLER NUMBER." : GOTO 15\varnothing
```

(a) If $G$ is greater than $X(G>X$ is TRUE), then $\qquad$ .
(b) However, if G is not greater than $\mathrm{X}(\mathrm{G}>\mathrm{X}$ is FALSE$)$, then $\qquad$
$\qquad$ _.
(a) the computer will print the message TRY A SMALLER NUMBER and then GOTO line 150 for another guess
(b) neither the PRINT nor the GOTO will be done
44. If $\mathrm{G}<\mathrm{X}$ is FALSE and $\mathrm{G}>\mathrm{X}$ is FALSE, the computer will finally arrive at line 180 . Here is a picture of the entire process of arriving at line 180.

$\qquad$
$\qquad$
$\qquad$
_ _ _ - - _ _ _ - -
The computer prints the message THAT'S IT! YOU GUESSED MY NUMBER, then goes to line 110, where it is directed to "think of" a new number and start the game again.
45. For very young children, we may wish to reduce the range of integers generated by the statement that uses the RND functions (line 110). For example, instead of generating a number from 1 to 100 , we may wish a number from 1 to 25. Conversely, advanced players may prefer a larger range, say 1 to 1000.
(a) Modify lines 110 and 130 so that the range is 1 to 25 . 110 $\qquad$ 130 $\qquad$
(b) Modify lines 110 and 130 so that the range is 1 to 1000 .

110
130

(a) $11 \varnothing$ LET $\mathrm{X}=\mathrm{INT}\left(25^{*} \operatorname{RND}(1)\right)+1$

130 PRINT "I'M THINKING OF A NUMBER,FROM 1 TO 25"
(b) $11 \varnothing$ LET $X=\operatorname{INT}(1 \varnothing \varnothing \varnothing$ *RND (1)) +1
$13 \varnothing$ PRINT "I'M THINKING OF A NUMBER FROM 1 TO $1 \varnothing \varnothing \varnothing . "$
46. Here is a convenient way to make it easy to change the range.

```
1\varnothing\varnothing REM***GUESS MY NUMBER - A COMPUTER GAME
1ø5 LET R=1\varnothing\emptyset
110 LET X=INT(R*RND(1))+1
120 PRINT
130 PRINT "I'M THINKING OF A NUMBER FROM 1 TO " ; R
```

Now the range is 1 to $R$, where $R$ is assigned a value in line 105 , then used in lines 110 and 130 . So, to change the range, you simply change line 105 . Suppose you want the range to be 1 to 500 . What do you write for line 105 ? 105 $\qquad$
$\qquad$
$1 \varnothing 5$ LET $R=5 \varnothing \varnothing$ or simply $105 \mathrm{R}=5 \varnothing \varnothing$
47. Using IF-THEN statements and multiple statements per line, modify and rewrite your NUMBER SIZE PROGRAM from frame 14 so that it will RUN like the one on the following page.

```
RUN
INPUT A NUMBER AND I WILL TELL YOU IF
IT IS LESS THAN 1\varnothing\varnothing, BETWEEN 1\varnothing\varnothing AND
1ø\varnothing\varnothing, OR OVER 1øøø.
YOUR NUMBER? }9
YOUR NO. IS LESS THAN 1\varnothing\varnothing
YOUR NUMBER? 1øø
YOUR NO. IS BETWEEN 1\varnothing\varnothing AND 1\varnothing\varnothing\varnothing.
YOUR NUMBER? }99
YOUR NO. IS BETWEEN 1\varnothing\varnothing AND 1\varnothing\varnothing\varnothing.
YOUR NUMBER? 10ø\varnothing
YOUR NO. IS BETWEEN 1\varnothing\varnothing AND 1\varnothing\varnothing\varnothing.
YOUR NUMBER? 1øø1
YOUR NO. IS OVER 1ø\varnothing\varnothing.
YOUR NUMBER?
```

```
1\varnothing\varnothing REM***NEW NUMBER SIZE PROGRAM
11\varnothing PRINT "INPUT A NUMBER AND I WILL TELL YOU IF"
12\varnothing. PRINT "IT IS LESS THAN 1\varnothing\varnothing. BETWEEN 1\varnothing\varnothing AND"
125 PRINT "1\varnothing\varnothing\varnothing, OR OVER 1\varnothing\varnothing\varnothing."
130 PRINT : PRINT "YOUR NUMBER"; : INPUT N
14\varnothing IF N<1\varnothing\varnothing THEN PRINT "YOUR NO. IS LESS THAN 1\emptyset\varnothing.": GOTO 13\varnothing
15\varnothing IF N<=1\varnothing\varnothing\varnothing THEN PRINT "YOUR NO. IS BETWEEN 1øø AND 1\varnothing\varnothing\varnothing.": GOTO 13\varnothing
16\varnothing IF N>1\varnothing\varnothing\varnothing THEN PRINT "YOUR NO. IS OVER 1\varnothing\varnothing\varnothing.": GOTO 13\varnothing
```

48. Now we want you to put your accumulated knowledge of BASIC to work and write a program to provide practice for a person learning or reviewing the "times table," that is, multiplication from 0 times 0 to 12 times 12 . Of course, we are calling this program COMPASSIONATE MULTIPLICATION PRACTICE. Study the RUN and our notes, then build your program. If you have a computer handy to use, check your own program before looking at our way of doing it.

Generate a problem, using random numbers from 0 to 12 . Print the problem and ask for an answer. Compare the player's answer with the correct answer.

If the answer is smaller than the correct answer, print TRY A BIGGER NUMBER and repeat the problem.

If the answer is bigger than the correct answer, print TRY A SMALLER NUMBER and repeat the problem.

If the answer is correct, tell the player that she or he has typed the correct answer.

Our program uses three different replies to a correct answer. These are chosen at random from the following three possibilities.

## THAT'S IT!

CORRECT ANSWER
GOOD WORK! KEEP IT UP

```
RUN
    2 人 4 =? 8
GOOD WORK! KEEP IT UP!
    2 2 =? 4
GOOD WORK! KEEP IT UP!
    2 }\times8=?1
TRY A BIGGER NUMBER.
    2 * 8=? 16
CORRECT ANSWER!
    1\varnothing\times1 =? 1\varnothing
CORRECT ANSWER!
    1\varnothing }\times9=?1\varnothing
TRY A SMALLER NUMBER.
    1\varnothing}\times9=? 9\varnothing
GOOD WORK! KEEP IT UP!
    11\times7=?
```

```
1\varnothing\varnothing REM***COMPASSIONATE MULTIPLICATION PRACTICE
110 LET A=INT(12*RND(1))+1 : LET B=INT(12*RND(1))+1
12\emptyset PRINT:PRINT A; "X" " B; " = " ; : INPUT C
13ø IF C<A*B THEN PRINT "TRY A BIGGER NUMBER." : GOTO 12ø
14\varnothing IF C>A*B THEN PRINT "TRY A SMALLER NUMBER.": GOTO 12\emptyset
15\varnothing LET R=INT(3*RND(1))+1:ON R GOTO 16\varnothing,17\varnothing,18\varnothing
160 PRINT "THAT'S IT!": GOTO 11\varnothing
17\varnothing PRINT "CORRECT ANSWER!": GOTO 11\varnothing
180 PRINT "GOOD WORK! KEEP IT UP!" : GOTO 11\varnothing
```

49. We mentioned in Chapter 2 that some of the older versions of BASIC required an END statement as the last statement in a program. Most versions of BASIC for home computers do not need this final END. However, the END statement, and its relative, the STOP statement, can be handy for terminating a program in some place other than the last line-numbered statement.

It is often handy to be able to end or stop a program as a result of an IF-THEN decision. END or STOP can be the condition to fulfill after THEN if the condition is TRUE. Examples:

```
2\varnothing IF }X=1\varnothing\mathrm{ THEN STOP
2\varnothing IF }X=1\varnothing\mathrm{ THEN END
```

With ATARI BASIC, using STOP will cause the computer to type a message, as shown below, giving the line number where the STOP statement was encountered and the RUN ended.

STOPPED AT $2 \varnothing$

However, a RUN that ends when an END statement is encountered just gives the standard READY.

In a multiple-statement line with IF-THEN, END or STOP could be used as below:

```
12\varnothing IF Y * Q = 1\varnothing\varnothing THEN PRINT "THAT'S ALL, FOLKS" : END
12\varnothing IF Y * Q = 1\varnothing\varnothing THEN PRINT "THAT'S ALL, FOLKS" : STOP
```

At the end of a math drill or game playing program, you could use the following approach.

```
31\varnothing PRINT "ANOTHER GAME (YES OR NO)"; : INPUT A$
32\varnothing IF A$ = "NO" THEN END
33\varnothing GOTO 1\varnothing\varnothing
```

In a counting loop program, insert a line to tell the computer to quit counting when $F$ is greater than 6.

```
1\varnothing LET F = 1
2\varnothing
3@ PRINT "F ="; F
4\varnothing LET F = F + 1
50 GOTO 2ø
```

$2 \emptyset$ IF $F>6$ THEN END
$2 \emptyset$ IF F>6 THEN STOP

## SELF-TEST

Try this Self-Test, so you can evaluate how much you have learned in Chapter 4.

1. Give the BASIC symbols for each of the following comparisons.
$\qquad$ is equal to
$\qquad$ is less than
$\qquad$ is greater than
$\qquad$ is less than or equal to
$\qquad$ is greater than or equal to
$\qquad$ is not equal to
2. Describe each IF-THEN statement in words. That is, describe what the statement tells the computer to do.
(a) IF G $=\times$ THEN 200
(b) IF $X>=\varnothing$ THEN $C=C+1$
$\qquad$
$\qquad$
(c) IF $N$ <> INT(N) THEN PRINT "N IS NOT AN INTEGER." : GOTO $21 \varnothing$
$\qquad$
$\qquad$
$\qquad$
(d) IF $A^{\wedge} 2+B^{\wedge} 2=C^{\wedge} 2$ then PRINT "YES, IT is A RIGHT TRIANGLE."
$\qquad$
$\qquad$
$\qquad$
3. For each description, write an IF-THEN statement.
(a) If the value of N is less than or equal to 7 , go to line 15 .
(b) If A is less than $2 * \mathrm{P}$, then increase the value of N by 1 and go to line 180.
(c) If $\mathrm{M} / \mathrm{N}$ is equal to $\operatorname{INT}(\mathrm{M} / \mathrm{N})$, then print the message M IS EVENLY DIVISIBLE BY N.
4. Complete the following program to tell how many years are needed to "double your money." Use multiple statements in line 190.
```
1\varnothing\varnothing REM***HOW MANY YEARS TO DOUBLE YOUR MONEY
11\varnothing PRINT "IF YOU TYPE THE AMOUNT OF PRINCIPAL"
12\varnothing PRINT "AND THE INTEREST RATE PER YEAR, I"
130 PRINT "WILL SHOW YOU HOW MANY YEARS TO"
135 PRINT "dOUBLE YOUR MONEY."
140 PRINT
150 PRINT "PRINCIPAL" ; : INPUT P
160 PRINT "INTEREST RATE" ; : INPUT R
17\varnothing LET N=1
18\varnothing LET A=P*(1+R/1\varnothing\varnothing) \N
200 PRINT
21\varnothing PRINT "YEARS TO DOUBLE YOUR MONEY:"; N
22ø PRINT "THE ACTUAL AMOUNT WILL BE $": A
RUN
IF YOU TYPE THE AMOUNT OF PRINCIPAL AND THE
INTEREST RATE PER YEAR, I WILL SHOW YOU HOW
MANY YEARS TO DOUBLE YOUR MONEY.
MRINCIPAL? 10\varnothing\varnothing 
YEARS TO DOUBLE YOUR MONEY: 12
THE ACTUAL AMOUNT WILL BE $ 2ø12.2
                                    2012.19638
```

This is $19 \varnothing$
a loop
5. What will be the result of running the following program? Show the RUN.

```
1\varnothing LET K=1
20 PRINT K
3ø LET K=K+1
4\varnothing IF K<=5 THEN 2\varnothing
RUN
```

6. What will the RUN look like for this program?
$1 \varnothing$ LET K=1
$2 \emptyset$ IF $K<5$ THEN $K=K+1$ : GOTO $2 \varnothing$ 3ø PRINTK
7. Describe the random numbers generated by each of the following expressions.
(a) $\mathrm{RND}(1)$
(b) $\quad 2 * \mathrm{RND}(1)$
(c) $\quad \mathrm{INT}(2 * \mathrm{RND}(1))$
(d) $\operatorname{INT}(2 * \mathrm{RND}(1))+1$
(e) $\operatorname{INT}(3 * \mathrm{RND}(1))-1$ $\qquad$
(f) $3.14159 *$ RND(1) $\qquad$
$\qquad$
8. Here is an incomplete program to simulate (imitate) flipping a coin. Please complete the program. (Hint: C should be 0 or 1, at random.)
```
1\varnothing\varnothing REM***COIN FLIPPER
11\varnothing LET C =
12\varnothing IF C=\varnothing THEN PRINT "TAILS" : GOTO 11\varnothing
13\varnothing IF C=1 THEN PRINT "HEADS" : GOTO 110
RUN
HEADS
HEADS
TAILS
TAILS
HEADS
HEADS
HEADS
HEADS
TAILS
HEADS
TAILS
TAILS
HEADS
HEADS
```


## Answers to Self-Test

The frame numbers in parentheses refer to the frames in the chapter where the topic is discussed. You may wish to refer to these for quick review.

1. $=$ is equal to
$<$ is less than
$>$ is greater than
$<=$ is less than or equal to
$>=$ is greater than or equal to
$<>$ is not equal to
(frame 7)
2. (a) If the value of $G$ is equal to the value of $X$, go to line 200. Otherwise ( $\mathrm{G}=\mathrm{X}$ is FALSE), continue in the usual line number order. (frames 1-8)
(b) If the value of X is greater than or equal to zero, increase the value of $C$ by 1 . Otherwise ( $\mathrm{X}>=0$ is FALSE ), do not execute the LET portion. In either case, continue in regular line number order. (frame 10)
(c) If $\mathrm{N}<>\operatorname{INT}(\mathrm{N})$ is TRUE, this means that the value of N is not an integer. In this case, print the string N IS NOT AN INTEGER and then go to line 210 . However, if N is an integer, $\mathrm{N}<>\operatorname{INT}(\mathrm{N})$ will be FALSE. In this case, neither the PRINT nor the GOTO will be executed and the computer will simply continue in regular line number order. (frames 1-8, 20-23, 42)
(d) If the value of $A$ squared plus $B$ squared is equal to the value of $C$ squared, print the string YES, IT IS A RIGHT TRIANGLE.

Otherwise $(\mathrm{A} \uparrow 2+\mathrm{B} \uparrow 2=\mathrm{C} \uparrow 2$ is FALSE), don't print the string. In either case, continue in regular line number order. (frames 1-8)
3. (a) IF $\mathrm{N}<=7$ THEN GOTO 15
(b) IF A<2*P THEN LET $N=N+1$ : GOTO 180
(c) IF M/N = INT(M/N) THEN PRINT "M IS EVENLY DIVISIbLE BY N"
(frames 1-10)
4. 19ø IF A<2*P THEN LET $N=N+1$ : GOTO $18 \varnothing$

In other words, if the newly computed amount $\mathbf{A}$ is still less than twice the original principal P, increase the year N by 1 , and go back to line 180 to compute a new amount A. (frames 9-10)
5. Run The PRINT statement is inside the loop. Therefore, it is done 1 every time.
(frame 8)
6. Run This time, the PRINT statement is outside the loop. It is done 5 only once, after the loop has been completed. (frame 8)
7. (a) Numbers between 0 and 1. Each random number is greater than zero, but less than one. This answer is also acceptable: $0<\mathrm{RND}(1)<1$. (frames 16,17 )
(b) Numbers between 0 and 2. Each random number will be greater than 0 , but less than 2. Also: $0<2 * R N D(1)<2$. (frames $17-19$ )
(c) 0 or 1 No other values are possible. (frames 20, 23-26)
(c) 1 or 2 (frames 20, 23-26)
(e) $-1,0$, or 1 (frames 20, 23-26)
(f) Numbers between 0 and 3.14159. Each random number is greater than 0 , but less than 3.14159 . Also: $0<3.14159 * \operatorname{RND}(1)<3.14159$. Since 3.14159 is an approximation to $\pi$, we might also say, although somewhat imprecisely, that these numbers are between 0 and $\pi$. (frames 20, 23-26)
8. $11 \varnothing \operatorname{LET} \mathrm{C}=\operatorname{INT}(2 * \operatorname{RND}(1)) \quad$ (frames 26,27)

## CHAPTER FIVE

## READ and DATA Work Together

This chapter is designed to give you practice using the BASIC statements and programming skills you have learned so far and to add to your bag of programming tricks. You will be able to extend your understanding of the capabilities of the PRINT statement, in order to better control the output of your programs and write more efficient instructions or programming code. In addition, you will learn two frequently used statements that always work together to assign values to variables: the READ and DATA statements. When you finish this chapter, you will be able to:

- use READ statements to assign values or strings to one or more variables at a time, from items in DATA statements;
- control the spacing of output through the use of commas and semicolons separating items in PRINT statements;
- identify the standard print positions in printout and write PRINT statements using comma spacing;

1. You've seen how LET statements and INPUT statements can be used to assign values to variables. (We hope that you have used them on your computer, too.) A third method uses two statements in combination, READ and DATA, to assign values to variables.
```
1% READ X
2\varnothing PRINT "THIS TIME THROUGH THE LOOP, }x=|"
3\varnothing GOTO 1\varnothing
4\varnothing DATA 1\varnothing, 15, 7, 3.25, 11
RUN 「
THIS TIME THROUGH THE LOOP, }x=1
THIS TIME THROUGH THE LOOP, }X=1
THIS TIME THROUGH THE LOOP, }x=
THIS TIME THROUGH THE LOOP, }x=3.2
THIS TIME THROUGH THE LODP, }x=1
ERROR- 6 AT LINE 1\varnothing
```

This statement 10 READ X tells the computer to READ one value from the DATA statement, and assign the value to the variable X. Every time the READ statement is executed (each time through the loop), the computer reads the next value from the DATA statement, and assigns the new value to the variable X . The computer keeps track of each value as it is read out, in effect, moving a pointer across the items in the DATA statement, one notch at a time.

How many values are in the DATA statement? $\qquad$

## 5

2. As the computer executed the program, each time through the loop it read and printed one value from the DATA statement. Then on the sixth trip through the loop, it tried to find still another number. Since it couldn't find another number to read from the DATA statement, the computer printed ERROR- 6 IN LINE 10 which means "Out of Data error in line 10." It isn't really an error. It just informs you that the computer has used up all the available data, tried to find more, but couldn't.

When the program in frame 1 was RUN, how many times was a new value assigned to the READ variable?

5 values were assigned
3. Look at the format for DATA statements.


No comma here

DATA statements may contain whole numbers, numbers with decimal fractions (such as 3.25 above), numbers in floating point or " $E$ " notation, or negative numbers.

DATA statements may not contain variables, arithmetic operations, other functions, or fractions.

This is OK: $\quad 90$ DATA $3,8,2.5$
This is NOT OK: 95 data $2+3,1 / 4,2 / 5,7 * 8$
Write a DATA statement for these values.

| 342 | 60.25 |
| :--- | :--- |
| 1256 | -412 |
| 205 | $2.05 E 8$ |

- ——————————

60 DATA $342,1256,2 \varnothing 5,60.25,-412,2, \varnothing 5 E 8$

Your line number may be different. And remember, no commas can be used in large numbers, such as 1256 above. However, floating point or ' $E$ "' notation may be used.
4. Data statements may be placed anywhere in the program.

```
1\varnothing READ N 10 DATA 123
2\emptyset PRINT N 2\varnothing READ N
30 DATA 123 30 PRINT N
RUN RUN
    123
    123
```

Can the DATA statement be placed as shown in the following program?

```
1\varnothing READ N
20 DATA 123
30 PRINT N
_-_-_-_-_-_
```

yes
5. These DATA statements are not written in correct BASIC. Tell what is wrong with each one.
(a) 20 DATA, $15,32,85,66$
(b) $3 \varnothing$ DATA 22.3; 81.1; $66.66 ; 43.22$
$-\infty-\infty-\infty-\infty$
(a) should not have comma after DATA
(b) should use commas instead of semicolons to separate values in a DATA statement
6. This program converts inches to centimeters. One inch $=2.54$ centimeters. When the program is RUN, the computer prints the value in inches on one line, and the equivalent in centimeters on the next. Fill in the missing statement (line 20).

```
1\varnothing REM***CONVERT INCHES TO CENTIMETERS
20
30 PRINT
4\varnothing PRINT "INCHES = ";I
5\varnothing PRINT "CENTIMETERS = ";2.54*I
6\varnothing GOTO 2\varnothing
90 DATA 1, 8, 12
RUN
INCHES = 1
CENTIMETERS = 2.54
INCHES = 8
CENTIMETERS = 20.32
INCHES = 12
CENTIMETERS = 30.48
ERROR- 6 AT LINE 2\emptyset
20 READ I
```

7. Now you write a program to convert ounces to grams. One ounce $=28.35$ grams (rounded to two decimal places). Use a DATA statement to hold the values in ounces that you want converted to grams. Here is what your program should print when it is RUN.
```
RUN
OUNCES = 1
GRAMS = 28.35
OUNCES = 13
GRAMS = 368.55
OUNCES = 16
GRAMS = 453.6
ERROR- 6 AT LINE 2%
```



```
1\varnothing REM***}\mathrm{ CONVERT OUNCES TO GRAMS
2ø READ Z
3@ PRINT
40 PRINT "OUNCES = " ; Z
5@ PRINT "GRAMS = " ; 28.35*Z
6\varnothing GOTO 2ø
90 DATA 1, 13, 16
```

We used Z to represent ounces because O (oh) can be confused with 0 (zero).
8. Write a "World's Most Expensive Adding Machine" program (from Chapter 3, frame 45) using READ and DATA statements instead of an INPUT statement so that a RUN of the program will look like the one below. Examine the RUN to determine the values in the DATA statement.

```
RUN
X = 12
TOTAL SO FAR IS 12
X=43
TOTAL SO FAR IS 55
x = 33
TOTAL SO FAR IS 88
X = 92
TOTAL SO FAR IS 18\varnothing
x = 76.25
TOTAL SO FAR IS 256.25
ERROR- 6 AT LINE 12\varnothing
```

```
1ø\varnothing REM***WORLD'S MOST EXPENSIVE ADDING MACHINE
11\varnothing LET T=\varnothing
12\varnothing READ X
130 LET T=T+X
140 PRINT "x = " : x
15ø PRINT "TOTAL SO FAR IS " ; T
160 PRINT
170 GOTO 12ø
180 DATA 12,43,33,92,76.25
```

Your line numbers may be different.
9. Do you remember our program to compute the mean, or average, of a group of numbers? If not, review Chapter 4, frame 12. Below is a rewrite of that program, using READ and DATA statements. We use lots of REMs
(REMARKS) to explain what is happening.

```
1øめ REM***A FRIENDLY 'MEAN' PROGRAM
11\varnothing REM***INITIALIZE T (FOR TOTAL) AND N (FOR NUMBER OF NUMBERS)
12% T=\varnothing:N=\varnothing
130 REM***READ A NUMBER, X. IF IT IS THE FLAG 1E97
14% REM***GOTO PRINTOUT. OTHERWISE, UPDATE T AND }
15% READ }X\mathrm{ : IF }X=1E97 THEN 18%
160 T=T+X :N=N+1 : GOTO 15%
170 REM***PRINT ANSWERS
18\varnothing PRINT "N = " :N
19\varnothing PRINT "TOTAL = " : T
20% PRINT "MEAN = " : T/N
9ø』 REM***DATA FOLLOWS
910 DATA 10,3,-9,-15,-23,-25,-30,1E97<< The flag
RUN
N=7
TOTAL = -89
MEAN = -12.71428571
```

To RUN this program for a different set of data, simply replace line 910 by one or more DATA statements containing the new data and the flag 1E97. (You'll recall from Chapter 3 that to replace a statement, just type the new statement using the old line number.) For example, suppose we wish to use this data: $63,72,50,55,75,67,59,61,64$. Write the DATA statement.

```
91\varnothing DATA
```

$\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

910 DATA $63,72,50,55,75,67,59,61,64,1 \mathrm{E97}$

10. The following program causes the computer to read numbers from a DATA statement and print only the numbers that are positive (greater than zero). Numbers that are less than zero or equal to zero are not printed.

```
10 READ X
2\emptyset IF }X>\varnothing\mathrm{ THEN PRINT "X = " ; }
3\varnothing GOTO 1\varnothing
4\varnothing DATA 3,7,\varnothing,-2,5,-1,7,8,\varnothing,-3
RUN
x = 3
x=7 Note:7 is printed twice because it occurs twice in the DATA
x=7 statement.
X=8
ERROR- 6 AT LINE 1\varnothing
```

Look at the numbers in the DATA statement.
(a) For which numbers is the condition $\mathrm{X}>0$ TRUE? $\qquad$
(b) When $\mathrm{X}>0$ is TRUE, what does line 20 cause the computer to do?
(c) For which numbers is the condition $\mathrm{X}>0$ FALSE?
(d) When $\mathrm{X}>0$ is FALSE, what happens in line 20 ?
(a) $3,7,5,7,8$
(b) print the message $\mathrm{X}=$ followed by the value of X
(c) $0,-2,-1,0,-3$
(d) Nothing. The PRINT portion of line 20 is not executed and the computer goes on to line 30 .
11. What will the RUN look like for this program?

```
1% READ X
2% IF }x<\varnothing\mathrm{ THEN PRINT " }\textrm{X}=|=
30 GOTO 1\varnothing
4ø DATA 3,7,\varnothing,-2,5,-1,7,8,\varnothing,-3
RUN
```

```
RUN
x = -2
x = -1
x=-3
ERROR- 6 AT LINE 1\varnothing< Did you remember this?
```

12. Complete the following program so that the RUN will occur as shown.
```
1\varnothing READ X
20
3\varnothing GOTO 1\varnothing
40 DATA 3, 7, 0, -2, 5, -1, 7, 8, &, -3
RUN
x=\varnothing
x = D
ERROR- 6 AT LINE 1』 the DATA statement.
```

$2 \varnothing$ IF $x=\varnothing$ THEN PRINT " $x=" ; x$
13. For more practice, do each of the following. If possible, try each one on your computer.
(a) Complete line 20 so that only nonzero numbers are printed. $2 \otimes$ IF $\qquad$ THEN PRINT " $x=$ " $x$
(b) Complete line 20 so that the computer prints numbers that are greater than or equal to zero.
28 IF $\qquad$ THEN PRINT " $\mathrm{x}=\mathrm{l}$ : x
(c) Complete line 20 so that the computer prints numbers that are less than or equal to 3 .
26 IF _ THEN PRINT " $x=$ " $x$
(a) $x<>$ (THE COMPUTER WILL PRINT $3,7,-2,5,-1,7,8$, AND -3.)
(b) $x>=\varnothing$ (THE COMPUTER WILL PRINT $3,7,0,5,7,8$, AND 0.)
(c) $x<=3$ (THE COMPUTER WILL PRINT $3,0,-2,-1,0$, AND -3. )

If you need review, see Chapter 4, frame 7.
14. In BASIC you may have more than one variable following a READ instruction. On the following page is an example. Use commas to separate the variables.


This will cause the computer to take two values from the DATA statement and assign them in order to the three READ variables.

Complete the RUN of this program (fill in blanks).

```
1\varnothing READ X,Y
2\varnothing PRINT }X,
3\varnothing GOTO 1\varnothing
4\varnothing DATA 1\varnothing, 2\varnothing, 3\varnothing, 4\varnothing
RUN
    1\varnothing 2\varnothing
ERROR- 6 AT LINE 1D
```



```
    30
    4ø
```

The second time through the loop, these values were assigned to X and Y and printed by line 20. (We'll discuss the spacing of items in PRINT statements later on.)
15. Fill in the blank spaces in the program and in the RUN.

```
1\varnothing
2\emptyset PRINT A + B
3\emptyset GOTO 1\varnothing
4\emptyset DATA 3,5,6,4,7,9
RUN
    8
ERROR- 6 ATLINE 1\varnothing
10 READ A,B
RUN
    8
    10
    16
```

16. You may have more than one READ statement in a program. However, all READ statements assign values to their variable(s) from the same DATA statement. An item from DATA is assigned to a READ variable in the order that the computer comes to READ statements when the program is RUN.
```
1\varnothing READ P
2\emptyset READ Q
3\varnothing PRINT P
4\varnothing PRINT Q
5\varnothing GOTO 1\varnothing
60 DATA 3,5,6,4,7,9
RUN
    3 First data item assigned to P, second assigned to Q.
    7_ Second trip through the loop: third data item is assigned to P, fourth
        to Q.
ERROR- 6 AT LINE
```

For the third trip through the loop, what value is assigned to P ? $\qquad$ What value is assigned to Q ? $\qquad$
_ - - - - - - - -
7; 9
17. Write a program that:
uses three READ statements to assign values to three different READ variables $\mathrm{X}, \mathrm{Y}$, and Z ;
then prints the sum of $X+Y+Z$;
then loops back to repeat the process until the data are all used up.
Show what the computer will print when your program is RUN. Here are the data for the DATA statement: $3,5,6,4,7,9,2,5,2$.

```
1% READ X
2ø READ Y
30 READ Z
4\varnothing PRINT X + Y + Z
5ø GOTO 1ø
60 DATA 3,5,6,4,7,9,2,5,2
RUN
    14
    2ø
    9
ERROR- 6 AT LINE 1ø
```

18. Here is a questionnaire we gave to 50 people.

## DOES YOUR COMPUTER UNDERSTAND YOU?

1. YES
2. NO

Each of the 50 responses was either 1 (YES) or $2(\mathrm{NO})$. The responses are shown below in five DATA statements. The last response is followed by -1 , the flag signalling end of data.

```
9ø\varnothing REM***DATA* 1=YES, 2=NO, - 1=END OF DATA
91ø DATA 1,2,2,2,1,2,1,2,1,2
92ø DATA 2,1,1,1,2,1,2,2,2,1
930 DATA 2,2,2,1,2,1,2,2,1,2
94ø DATA 1,1,1,1,2,1,2,2,1,1
950 DATA 2,2,2,2,1,1,1,2,1,2,-1
```

How many YES answers? $\qquad$
How many NO answers? $\qquad$
Write the number of YES answers in the box labeled ' Y ', and the number of NO answers in the box labeled "N."
$\square$

N $\square$

19. Here is a program to read the answers from the DATA statements and count the number of YES answers and NO answers. The variable Y is used to count YES answers. The variable N is used to count NO answers.

```
1\varnothing\varnothing REM***QUESTIONNAIRE ANALYSIS PROGRAM
11\varnothing REM***INITIALIZE: SET COUNTING VARIABLES TO ZERO
12\varnothing Y=\varnothing : N=\varnothing
2ø\varnothing REM***READ AND COUNT VOTES
21\varnothing READ A : IF A=-1 THEN 41\varnothing
22\varnothing IF A=1 THEN LET }Y=Y+1 : GOTO 21\varnothing
23\varnothing IF A=2 THEN LET N=N+1 : GOTO 21\varnothing
4\varnothing\varnothing REM***PRINT THE RESULTS Note the multiple statements in
4 1 \varnothing ~ P R I N T ~ l i n e s ~ 1 2 0 , 2 1 0 , 2 2 0 , ~ a n d ~ 2 3 0 . ~
420 PRINT "YES: " ; Y
430 PRINT " NO: " ; N
9\varnothing\varnothing REM***DATA* 1=YES, 2=NO, - 1=END OF DATA
91ø DATA 1,2,2,2,1,2,1,2,1,2
920 DATA 2,1,1,1,2,1,2,2,2,1
93@ DATA 2, 2, 2,1,2,1,2,2,1,2
94ø DATA 1,1,1,1,2,1,2,2,1,1
95ø DATA 2,2,2,2,1,1,1,2,1,2,-1
RUN
YES: 23
    NO: 27
```

(a) Which section of the program is a loop that is repeated for each value in the DATA statements? Lines $\qquad$ to $\qquad$ .
(b) Which statement reads a value corresponding to one vote and puts it into box A? $\qquad$
(c) Which line determines whether a vote is YES and, if it is, increases the YES count by one? $\qquad$
(d) Which line determines whether a vote is NO and, if it is, increases the NO count by one? $\qquad$
(a) lines 210 to 230; (b) line 210; (c) line 220; (d) line 230
20. Now look at this new questionnaire.

## DOES YOUR COMPUTER UNDERSTAND YOU?

1. YES
2. NO
3. SOMETIMES

Modify the program in frame 19 so that the computer counts the YES, NO, and SOMETIMES answers. Use the variable Y to count YES answers. Use the variable N to count NO answers. Use the variable S to count SOMETIMES answers. Use the following data.

$$
2,1,3,2,3,3,1,3,3,2,1,2,1,2,1,1,3,3,-1
$$

Using this data, the results when the program is RUN should be printed as follows.

```
YES: 6
    NO: 5
SOMETIMES: 7
```

Here are our changes.

```
12\varnothing Y=\varnothing : N=\varnothing : S=\varnothing
24ø IF A=3 THEN LET S=S+1 : GOTO 21\varnothing
440 PRINT "SOMETIMES: " ; S
9øø REM***DATA: 1=YES, 2=NO, 3=SOMETIMES, -1=END OF DATA
91ø DATA 2,1,3,2,3,3,1,3,3,2,1,2,1,2,1,1,3,3,-1
920
930
940
950
```

We deleted lines 920, 930, 940, and 950 from the program of frame 19. If the program is in the computer, we can do this by typing the line number and pressing RETURN. If you have a computer handy, LIST the program to show the modifications and to prove that the deleted lines have disappeared from the computer's memory. On the following page is our listing.

```
1\varnothing\varnothing REM***QUESTIONNAIRE ANALYSIS PROGRAM
11\varnothing REM***INITIALIZE: SET COUNTING VARIABLES TO ZERO
12\emptyset Y=\varnothing : N=\varnothing : S=\varnothing
2ø\varnothing REM***READ AND COUNT VOTES
21ø READ A : IF A=-1 THEN 41ø
22\varnothing IF A=1 THEN LET Y=Y+1 : GOTO 21\varnothing
230 IF A=2 THEN LET N=N+1 : GOTO 210
24ø IF A=3 THEN LET S=S+1 : GOTO 21ø
4ø\varnothing REM***PRINT THE RESULTS \
410 PRINT
42\emptyset PRINT "YES : " ; Y
400 PRINT " NO : " ; N
44\varnothing PRINT "SOMETIMES : " ; S
9ø\varnothing REM***DATA: 1=YES, 2=NO, 3=SOMETIMES, - 1=END OF DATA
910 DATA 2,1,3,2,3,3,1,3,3,2,1,2,1,2,1,1,3,3,-1
```

21. Back in Chapter 2, we used PRINT statements in the following form.

PRINT $e$
where $e$ is a numerical expression

For example:
PRINT 7+5
$\underbrace{7+5}$
numerical expression
A PRINT statement of this form tells the computer to compute and evalute (do the arithmetic of) the numerical expression and then print the result.

The following PRINT statement tells the computer to evaluate four numerical expressions and print the four results.

We type: PRINT $7+5,7-5,7 * 5,7 / 5$
It types: 122

In the above, draw arrows connecting each numerical expression with its computed and printed value. We have drawn the first arrow, connecting the expression, $7+5$, with its printed result, 12 .

22. If a PRINT statement has more than one expression, then the expressions are separated by commas.


The following PRINT statement directs the computer to compute and print the values of $2+3,2-3,2 * 3$, and $2 / 3$. However, we forgot to put in commas. Please insert commas in the correct BASIC form.

```
PRINT 2+3 2-3 2*3 2/3
```

-     -         -             -                 -                     -                         -                             -                                 - 

PRINT $2+3,2-3,2 * 3,2 / 3$

Note: No comma following PRINT and no comma following 2/3. A comma following PRINT will cause an ERROR message. A comma following $2 / 3$ (at the very end of the PRINT statement) has a special purpose which we will discuss later.
23. Complete the following. (Remember, for direct statements, you do not need a line number and you only have to press RETURN to have the computer execute the statement.)

We type: PRINT 3*3; 5*5, 7*7
It types: $\qquad$
$\qquad$

We type: PRINT $2 * 3+4 * 5,(2+3) *(4+5)$
It types: $\qquad$ -

| - | - | $-\infty$ |
| :--- | :--- | :--- |
| 9 | 25 | 49 |
| 26 | 45 |  |

24. Your turn. Let's go back to our three bicycles, with wheels of 20-, 24- and 26 -inch diameters. You want to find out, for each bike, how far it travels during one turn of the wheel. In other words, you want to evaluate the following three expressions.

| 20-inch wheel: | $3.14^{*} 20$ | First expression |
| :--- | :--- | :--- |
| 24-inch wheel: | $3.14^{*} 24$ | Second expression |
| 26-inch wheel: | $3.14^{*} 26$ | Third expression |

Write a PRINT statement to tell the computer to evaluate the three expressions and PRINT the results.

You type:
It types: $62.8 \quad 75.36 \quad 81.64$

-     -         -             -                 -                     -                         -                             -                                 - 

RRINT 3.14*20, 3.14*24, 3.14*26
25. ATARI BASIC has four standard print positions. A comma in a PRINT statement causes the cursor to move to the next available standard print position. Look at the example below and fill in the blanks.

We type: PRINT 1,2,3,4
It types:


Position 1 Position 2 Position $\qquad$ Position
$\qquad$

3; 4
26. Positive numbers, or zero, are printed without an explicit plus sign (+). Watch what happens when negative numbers are printed.

We type: PRINT - $1,-2,-3,-4$


How does the printing of negative numbers differ from that of positive numbers? $\qquad$

-     -         -             -                 -                     -                         -                             - 

Negative numbers are printed with a minus sign (-) followed by the digits of the number.
27. What happens if there are more than four items in a PRINT statement? Look at the direct statement below and also at how the computer executed it.

We type: PRINT $1,2,3,4,5,6,7$

It types: 1 | 3 |
| :--- | :--- | :--- |

7

Describe what happened. $\qquad$
———————————

The computer printed the 7 numbers on 2 lines, with 4 numbers on the first line and 3 numbers on the second line.
28. Following the rules for items or expressions separated by commas, show what the computer will print in response to the following PRINT statement.

We type: PRINT $1,2,3,4,5,6,7,8,9,1 \varnothing$
It types:

| $-\cdots-\cdots$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 1 | 2 | 3 | 4 |
| 5 | 6 | 7 | 8 |
| 9 | 10 |  |  |

29. Instead of commas, we can also use semicolons as separators in a PRINT statement. Watch what happens.

We type: PRINT-1;-2;-3;-4;-5;-6;-7
It types: -1-2-3-4-5-6-7
We type: PRINT 1:2:3:4;5
It types:, 12345
Semicolon spacing catenates numbers. That is, it directs the computer to print numbers close together, in a linked series. Comma spacing causes numbers to be printed in predetermined print positions. So, to print results close together, use $\qquad$ .
30. The screen can hold up to 38 characters on each line. That is, it has 38 character positions, numbered from 0 on the left to 37 on the right. Complete the following diagram of character positions on the screen.


32: 37
31. The four standard print positions, used in comma spacing, begin at character position 0 . We've marked print positions 1 and 2 ; you circle print positions 3 and 4 on the following diagram.

1111111111222222222233333333
$\varnothing 123456789 \varnothing 123456789 \varnothing 123456789 \varnothing 1234567$


Print Print
position 1 position 2


Note: A standard print position is 10 character positions wide. For example, print position 1 occupies character positions 0 through 9 , or 10 character positions in all. Print position 2 occupies character positions 10 through 19, and so on.
32. Now watch what happens when we put a comma at the end of a PRINT statement.

```
1\varnothing LET N=1
2\varnothing PRINT N,
30 LET N=N+1
4\varnothing GOTO 2\varnothing
RUN
\begin{tabular}{llll}
1 & 2 & 3 & 4 \\
5 & 6 & 7 & 8 \\
9 & 18 & 11 &
\end{tabular}
STOPPED AT LINE 2%
```

We pressed BREAK here to terminate the RUN.
Remember what the comma does. It tells the computer to move to the next standard print position. So, after printing number 1, the computer moves to print position 2; after print 2 , the computer moves to standard print position 3 , and so on. After printing something in standard print position 4, it continues printing on the next line.

Show the first 7 items printed by the following program.

```
10 LET N=1
2\emptyset PRINT N,
30 LET N=N+2
4\varnothing GOTO 2\emptyset
RUN
```

| $-\cdots-\infty-\infty$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 1 | 3 | 5 | 7 |
| 9 | 11 | 13 | 7 |

33. Now, what do you suppose happens if we put a semicolon at the end of a PRINT statement? As always with computers, if we don't know, we EXPERIMENT. Let's try it.
```
10 LET N=1
```

28 PRINT N:
38 LET $N=N+1$
40 GOTO $2 \%$
RUN 1234567891 W111213141516171819 (Bet you weren't
$1234567891 \varnothing 111213141516171819$ this quick!)
STOPPED AT LINE $2 \varnothing \quad$ then

Rewrite line 20 so that the computer puts a space after each number it prints.


It you want to put a space before each number, do it like this:
$2 \varnothing$ PRINT " "; N; The space between quotes, is before the number ( N ).
34. We have spent some time with comma spacing and semicolon spacing with numbers. Next, let's try strings.
PRINT "A", "b", "C", "D"

| Print |  |  |  |
| :--- | :--- | :--- | :--- |
| position 1 | Print | position 2 | Print |
| position 3 | Print |  |  |
| position 4 |  |  |  |

Your turn. Complete the output for this direct statement the way the computer would do it.

```
PRINT "A", "B", "C", "D", "E", "F", "G"
```

| $----\infty-\infty-\infty$ |  |  |  |
| :---: | :---: | :---: | :---: |
| $A$ | $B$ | $C$ | $D$ |

With strings, as with numbers, the comma causes the computer to move to the next standard print position.
35. Comma spacing is useful for printing headings. For example, here is a rewrite of our inches to centimeters program in frame 6.

```
1\varnothing REM***INCHES VERSUS CENTIMETERS TABLE
20 PRINT "INCHES","CENTIMETERS"
30 READ I
40 PRINT I,2,54*I
50 GOTO 30
90 DATA 1,8,12
RUN
INCHES CENTIMETERS
1 2.54
8 20.32
12 30.48
ERROR- 6 IN 3\varnothing
```

Note the use of comma spacing in lines 20 and 40 . The numerical values printed by line 40 line up nicely under the headings printed by line 20.

Your turn. Rewrite the ounces to grams program (frame 7), so that a RUN looks like the one on the following page.

| RUN |  |  |
| :--- | :--- | :--- |
| OUNCES |  | GRAMS |
| 1 | 28.35 |  |
| 13 | 368.55 |  |
| 13 | 453.6 |  |
| 16 | 6 | $4 T$ LINE 36 |

```
1\varnothing REM***OUNCES TO GRAMS TABLE
2\varnothing PRINT "OUNCES","GRAMS"
3\varnothing READ Z
4\varnothing PRINT Z,28.35*Z
5\varnothing GOTO 3\varnothing
9\varnothing DATA 1,13,16
```

38. Now, let's look at semicolon spacing with strings.
```
PRINT "A"; "B"; "C"; "D"; "E"
ABCDE
```

Semicolon spacing causes the computer to catenate strings, that is, to print them one after the other with no spaces.

Show what happens when the computer executes the following PRINT statement.

```
PRINT "THIS"; "IS"; "COMPUTER"; "PROGRAMMING?"
```

-     -         -             -                 -                     -                         -                             -                                 - 

THISISCOMPUTERPROGRAMMING?
39. The output in frame 38 is rather crowded and hard to read. If you want spaces between strings, you must put them where you want them. For example:


Show what the computer will print this time.

THIS IS COMPUTER PROGRAMMING?
40. Let's try a program that causes strings stored by string variables to print information.

```
5 DIM A$(2\varnothing),B$(2\varnothing),C$(2\varnothing)
1\varnothing LET A$="COMPUTERS "
2ø LET B$="ARE"
3\varnothing LET C$=" INTERESTING."
4ø PRINT A$;B$;C$
50 PRINT A$,B$,C$
```

First, we make room for the strings.
Note the spaces inside the quotation marks in lines 10 and 30.

Show what the computer will print when the program is RUN.

## RUN

```
-- - - - - - - - 
RUN
COMPUTERS ARE INTERESTING.
COMPUTERS ARE INTERESTING.
        4
    Position 2 Position 3
```

41. You may have guessed by now that a READ statement may also be used to assign strings to string variables. Show how you think the RUN for the following program to print the names of computer club members will look.
```
    5 DIM M$(2\varnothing)
1\varnothing READ M$
2\varnothing PRINT M$
3\varnothing GOTO 1\varnothing
4| DATA JERRY,BOBBY,MARY,DANNY
5\varnothing DATA MIMI,KARL,DOUG,SCOTT
```

```
RUN
JERRY
BOBEY
MARY
DANNY
MIMI
KARL
DOUG
SCOTT
ERROR- 6 AT LINE 1\varnothing
```

Well, we could go on like this for a long time. But, there are other things for you to know. So, EXPERIMENT! What happens if??? Try it and find out. Try short strings, long strings (what if a string is more than 10 characters). Mix up strings and numbers. Try strings with leading spaces; trailing space. Aha! You and your friendly ATARI computer can do it all.

And now, it's your turn again to write a program. You have probably used dice before, either on 'board"' games or other games. We want you to apply your accumulated knowledge of BASIC to write a program that simulates (imitates) the roll of a die. (A "die" is one "dice.") Below is a RUN of our program. Examine it and use it as a guide to writing a program that will produce a RUN similar to this one. Use standard print positions. Take your time, and try your solution on a computer before looking at ours, if possible.

```
RUN
HOW MANY ROLLS? 7
\begin{tabular}{llll} 
ONE & THREE & THREE & SIX \\
FOUR & FIVE & TWO &
\end{tabular}
HOW MANY ROLLS? 2
ONE SIX
HOW MANY ROLLS? And so on.
```

Don't look at the answer until you have written your program.

```
1\varnothing\varnothing REM***DIE ROLLER
11\varnothing PRINT : PRINT "HOW MANY ROLLS": : INPUT R
12\varnothing K=1 : PRINT
2ø\varnothing REM***'ROLL THE DIE' R TIMES
21\varnothingS=INT(5*RND(1))+1
22\varnothing ON S GOTO 23\varnothing,24\emptyset,25\emptyset,26\emptyset,27\emptyset,28\emptyset
230 PRINT "ONE", : GOTO 290
24\varnothing PRINT "TWO", : GOTO 29\emptyset
25@ PRINT "THREE", : GOTO 29@
260 PRINT "FOUR", : GOTO 29\varnothing
27\varnothing PRINT "FIVE", : GOTO 29@
280 PRINT "SIX",
290 IF K<R THEN LET K=K+1 : GOTO 21\varnothing
3\varnothing\varnothing PRINT : PRINT : GOTO 11\varnothing
```

Why two PRINTs in line 300? Try it with just one.


## SELF-TEST

Try this Self-Test, so you can evaluate how much you have learned so far.

1. Pretend that you are the computer and complete each RUN.
(a) 10 READ A $2 \varnothing$ PRINT A $3 \varnothing$ DATA 27 RUN
(b) $1 \varnothing$ READ A
$2 \varnothing$ READ B
$3 \varnothing$ PRINT A-B
$4 \varnothing$ DATA 27,15
RUN
(c) $1 \varnothing$ READ $A, B$ $2 \varnothing$ PRINT $A-B$ 3甲 DATA 27,15 RUN
(d) $1 \varnothing$ READ $A, B$ $2 \varnothing$ PRINT A-B 30 DATA 27 $4 \varnothing$ DATA 15 RUN
2. Show the RUNs for the following programs.
(a) $1 \varnothing$ READ $X$ $2 \varnothing$ PRINT $x$, Comma at end of PRINT statement $3 \varnothing$ GOTO $1 \varnothing$ $4 \varnothing$ DATA $3,7, \varnothing,-2,5,-1,7,8, \varnothing,-3$ RUN
(b) $1 \varnothing$ READ $x$ 2ø PRINT $x ; " \quad " ;$ Semicolon at end of PRINT statement $3 \varnothing$ GOTO $1 \varnothing$ 4ø DATA $3,7, \varnothing,-2,5,-1,7,8, \varnothing,-3$ RUN
3. Complete each RUN as if you were the computer.
(a) 10 READ $x$

$$
\begin{aligned}
& \text { 2 } \varnothing \text { IF } x>=\varnothing \text { THEN PRINT } " x=" ; x, \longleftarrow \text { Comma } \\
& 3 \varnothing \text { GOTO } 1 \varnothing \\
& 48 \text { DATA } 3,7, \varnothing,-2,5,-1,7,8, \varnothing,-3 \\
& \text { RUN }
\end{aligned}
$$

(b) 10 READ $\times$

$$
\begin{aligned}
& \text { 1ø READ } X \\
& 2 \varnothing \text { IF } x>=\varnothing \text { THEN PRINT " } \mathrm{X}=" ; \mathrm{X} \text {; Semicolon } \\
& 3 \varnothing \text { GOTO } 1 \varnothing \\
& 4 \varnothing \text { DATA } 3,7, \varnothing,-2,5,-1,7,8, \varnothing,-3 \\
& \text { RUN }
\end{aligned}
$$

4. Show the results if we RUN the following short program.
```
42ø PRINT "ANSWER","NO. OF","PERCENT OF"
430 PRINT "(Y OR N)","ANSWERS","TOTAL"
```

5. Modify the questionnaire analysis program beginning in frame 19 so that the results are printed as follows.

| ANSWER | NO. OF | PERCENT |
| :--- | :--- | :--- |
| $(Y O R N)$ | ANSWERS | OF TOTAL |
|  |  |  |
| YES | 23 | 46 |
| NO | 27 | 54 |
| TOTAL | $5 \emptyset$ | $1 \varnothing \varnothing$ |

Hint: Rewrite beginning with line 420 . The required information is printed in three columns, occupying the first three standard print positions.
6. Write a program, using READ and DATA statements, to compute the distance traveled in one turn of the rear wheel for bicycles with various wheel diameters. Use the following DATA statement with the line number of your choice.


On the following page is a run of our program.

7. Write a program to simulate coin flipping. The program should direct the computer to do the following steps. Type H for HEADS and T for TAILS across the page as shown in the RUN below. Also ask how many flips the user wants and do exactly that many, then stop. In other words, count the flips, and, when the count has reached the number requested, stop. Here are two RUNs of our program.


The first RUN of our program on our computer produced 9 heads (H) and 11 tails (T). The second RUN produced 53 heads (H) and 47 tails (T). Your computer may give quite different results.
8. Why not let the computer count the number of heads and the number of tails? Modify your program for question 7 so that the computer counts the number of heads and tails. Use the variable $H$ to keep track of the number of heads and the variable T to keep track of the number of tails. Two RUNs of the modified program are shown below.

9. Write a program to count the numbers in all the DATA statements in a program. Do not count the flag! For example, if the following DATA statements are in the program, the computer should dutifully tell us that there are 25 numbers.

```
150 DATA 2,3,5,7,11,13,17,19,23,29,31,37,41
160 DATA 43,47,53,59,61,67,71,73,79,83,89,97,1E97
```

The flag
Our program RUNs like this.


RUN
there are 25 Items of data.
10. Now write a program that will print a pattern of asterisks according to a plan entered as DATA statement values. This might be a way of laying a pattern of floor tiles, or loom weaving patterns, or just "computer art." Use a flag to avoid an out-of-data error message. Shown on the following page are our DATA statement values and the pattern produced by our program. Our program prints five different lines of asterisks and spaces.

```
3,4,4,5,1,5,1,5,1,5,2,2,2,5,1,5,1,5,1,5,4,4,3<<< DATA values
RUN
```



```
Hint: The pattern consists of five different types of lines. The first and last lines are "type 3 " lines. The first and last numbers in the DATA statement are 3 . Got the idea?
```


## Answers to Self-Test

The frame numbers in parentheses refer to the frames in the chapter where the topic is discussed. You may wish to refer to these for quick review.
1.
(a) $\begin{aligned} & \mathrm{RUN} \\ & 27\end{aligned}$
(b) $\underset{12}{R U N}$
(c) ${ }_{12}^{\mathrm{RUN}}$
(d) $\underset{12}{\mathrm{RuN}}$
(frames 1-6)
2. (a) RUN

| 3 |  |  | $\varnothing$ | -2 |
| :--- | :--- | :--- | :--- | :--- |
| 5 | -1 | 7 | 8 |  |
| $\varnothing$ | -3 |  |  |  |
| ERROR- | 6 | AT | LINE | $1 \varnothing$ |

(b) RUN
$\begin{array}{llllllllll}3 & 7 & \varnothing & -2 & 5 & -1 & 7 & 8 & \varnothing & -3\end{array}$ ERROR- 6 AT LINE $1 \varnothing$
(frames 1-5)
3. (a) RUN

| $x=3$ | $x=7$ | $x=\varnothing$ | $x=5$ |
| :--- | :---: | ---: | ---: |
| $x=7$ | $x=8$ | $x=\varnothing$ |  |
| ERROR- | 6 AT LINE $1 \varnothing$ |  |  |

（b）RUN
$X=3 X=7 X=5 X=7 X=8 X=\varnothing$
ERROR－$\quad{ }_{6}$ AT LINE $1 \varnothing$

How would you rewrite line 20 in order to provide more space between items？ For example： $\mathrm{X}=3 \mathrm{X}=7 \mathrm{etc}$ ．
（frames 32－33）
4．RUN

| ANSWER | NO．OF | PERCENT OF |
| :--- | :--- | :--- |
| （Y OR N $)$ | ANSWERS | TOTAL |

（frame 35）
5． $42 \emptyset$ PRINT＂ANSWER＂，＂No．OF＂，＂PERCENT OF＂
$43 \varnothing$ PRINT＂（Y OR N）＂，＂ANSWERS＂，＂TOTAL＂
$44 \varnothing$ PRINT
450 LET $T=Y+N$
$46 \varnothing$ PRINT＂YES＂，Y，10日＊Y／T
$47 \varnothing$ PRINT＂NO＂，N，1ø日＊N／T
$48 \varnothing$ PRINT＂TOTAL＂，T，1øø
In the above program segment，we have used T to compute the Total number of votes $(\mathrm{T}=\mathrm{Y}+\mathrm{N})$ ．Then，in lines 460 and 470 ，the expressions $100^{*} \mathrm{Y} / \mathrm{T}$ and $100 * \mathrm{~N} / \mathrm{T}$ are the percent Yes votes and No votes．
（frame 18－20，35）
6．1øø REM＊＊＊DIStance in one turn of a wheel
110 READ D
120 PRINT
130 PRINT＂wheel diameter：＂；D
14ヵ PRINT＂DISTANCE IN ONE TURN：＂；3．14＊D
150 GOTO $11 \varnothing$
$16 \varnothing$ DATA $16,28,24,26,27$
（frame 1）
7． $1 \varnothing \varnothing$ REM＊＊＊COIN FLIPPER
110 PRINT ：PRINT＂HOW MANY FLIPS＂；：infut N
$12 \varnothing$ IF $\mathrm{N}<1$ THEN END
130 REM＊＊＊FIP COIN N TIMES
$14 \varnothing \mathrm{~K}=\varnothing$ ：PRINT
15も $\mathrm{C}=\mathrm{INT}\left(\right.$ 2＊$^{*}$ RND（1））
168 IF $\mathrm{C}=\varnothing$ THEN PRINT＂ T ＂；
170 IF C＝I THEN PRINT＇ H ＂；
$18 \varnothing \mathrm{~K}=\mathrm{K}+1$
190 IF K＜N THEN $15 \varnothing$
200 END
There is more than one way to write this program．In ours，we use the variable K to count the number of times the coin has been flipped．In line 140，we set K to zero．Then，each time through the loop，we increase K by 1 （line 180）and compare K with N （line 190）．If K is still less than N ，we increase K by 1 and go around again．If N is less than one，no flips are done－this is checked by line 120 ．Your program may be entirely different． If it works，you have solved the problem！（frames 37，42）
8. We modified our program of question 7. The complete program is shown below. The variable T is used to count the number of tails and the variable H to count the number of heads. Look for T and H in lines $140,160,170$, and 210.

```
1ø\varnothing REM***COIN FLIPPER
11\varnothing PRINT : PRINT "HOW MANY FLIPS";:INPUT N
120 IF N<1 THEN END
130 REM***FLIP COIN N TIMES
14\varnothing K=\varnothing : T=\varnothing : H=\varnothing : PRINT
15ø C=INT(2*RND(1))
160 IF C=\varnothing THEN PRINT "T "; : T=T+1
17\varnothing IF C=1 THEN PRINT "H "; : H=H+1
180 K=K+1
19\varnothing IF K<N THEN 150
2ø\varnothing PRINT : PRINT
21\varnothing PRINT H:" HEADS AND ";T;" TAILS"
220 END
```

(frames 33, 37, 42)
9. $1 \varnothing \varnothing$ REM***COUNT ITEMS IN DATA STATEMENTS, EXCEPT FLAG
$110 \mathrm{~K}=\varnothing$
120 READ N
130 IF N<>1E97 THEN LET $K=K+1$ : GOTO $12 \varnothing$
14 ø IF $N=1 E 97$ THEN PRINT "THERE ARE" ;K;"ITEMS OF DATA."
150 DATA $2,3,5,7,11,13,17,19,23,29,31,37,41$
160 DATA $43,47,53,59,61,67,71,73,79,83,89,97,1 E 97$
999 END
Do you recognize the numbers in the DATA statements? They are all the prime numbers (those numbers with themselves and 1 as their only factors) less than 100. (frames $10,11,19$ )
10. $1 \varnothing \varnothing$ REM***PATTERN PRINTING PROGRAM
$11 \varnothing$ READ $X$ : IF $X=-1$ THEN END
$12 \varnothing$ ON X GOTO $21 \varnothing, 22 \varnothing, 23 \varnothing, 24 \varnothing, 25 \varnothing$
$2 \varnothing \varnothing$ REM***PATTERN LINES
$21 \varnothing$ PRINT "******* *** *******": GOTO $11 \varnothing$
$22 \varnothing$ PRINT "*** ***** ***** ***": GOTO $11 \varnothing$
$23 \varnothing$ PRINT "*********************" : GOTD $11 \varnothing$ $24 \varnothing$ PRINT $" * * * * * * * * * * * ": ~ G O T O ~ 11 \varnothing$ $25 \varnothing$ PRINT "*** *** *** ***": GOTO $11 \varnothing$
3øø REM*** DATA TO MAKE A RUG DESIGN
$31 \varnothing$ DATA $3,4,4,5,1,5,1,5,1,5,2,2,2,5,1,5,1,5,1,5,4,4,3,-1$ RUN
*********************


Here is another way to do it.

```
1\varnothing REMARK PATTERN PRINTING PROGRAM
2\varnothing READ X
30 IF }X=-1\mathrm{ THEN END
4\varnothing IF }X=1\mathrm{ THEN 1øø
5\varnothing IF X=2 THEN 12\varnothing
60 IF X=3 THEN 14\varnothing
70 IF }X=4\mathrm{ THEN 16ø
8\varnothing IF X=5 THEN 18\varnothing
9\varnothing GOTO 2\varnothing
1\varnothing\varnothing PRINT '
11\varnothing GOTO 2\varnothing
12\varnothing PRINT "*** ****** ***** **** "
13\varnothing GOTO 2\varnothing
14\varnothing PRINT "*********************** "
15\varnothing GOTO 2\varnothing
16\varnothing PRINT " * * * * * * * * * * * "
17\varnothing,GOTO 2\varnothing
18\varnothing PRINT " *** *** *** *** "
19\varnothing GOTO 2\varnothing
9ø\varnothing DATA 3,4,4,5,1,5,1,5,1,5,2,2
91\varnothing DATA 2,5,1,5,1,5,1,5,4,4,3,-1
```

(frames 18, 19)

## CHAPTER SIX

## FOR-NEXT Loops

In this chapter we introduce another important computer programming concept: the FOR-NEXT loop. The IF-THEN statement and the FOR-NEXT loop greatly extend the usefulness of the computer as a tool. Close attention to the explanation and problems in this chapter will help you understand the functions of these statements in BASIC and will open a new dimension in your computer programming capability. When you complete this chapter you will be able to:

- use the FOR and NEXT statements;
- use the STEP clause in FOR statements.

1. The Loop Demonstration Program on the following page is a counting program that prints the value for $F$ as we increase $F$ from 1 through 6 . Line 10 merely initializes $F$ at 1 . To initialize, remember, means to assign the first value to a variable. Line 20 prints the current value for $F$. Line 30 increases $F$ by 1 each time through the program.

Line 40 is an IF statement that tests the value of $F$. As long as $F$ is less than or equal to 6 , line 40 sends the computer back to line 20 to print the value of $F$. Once $F$ exceeds 6 , the program will stop since there are no more statements in the program. Just for practice, rewrite the program on the following page using multiple statements in one line. But think carefully: Can you do the entire program in just one line?

```
5 REM***LOOP DEMONSTRATION
1\varnothing LET F=1
2\varnothing PRINT "F = ": F
30 LET F=F+1
4\varnothing IF F <= 6 THEN 2\varnothing
RUN
F = 1
F=2
F=3
F=4
F=5
F=6
1\varnothing LET F = 1
2ø PRINT "F= "; F : LET F=F+1 : IF F <= 6 THEN 2\varnothing
RUN
F=1 This means go back and start executing line 20 again
F=2 (only if the comparison is true, of course). Notice that
```



```
F=5 would get "initialized" back to 1 every time the state-
F=6
ment was executed. So we could not put the entire
program in just one line.
```

2. The space-saving, time-saving FOR-NEXT loop accomplishes a given number of iterations or repetitions more easily. Look at the FOR-NEXT loop below. Instead of IF-THEN, this time we use the FOR and NEXT statements to tell the computer how many times to go through the loop.
```
5 REM***FOR-NEXT LOOP DEMONSTRATION
10 FOR F=1 TO 6
2\varnothing PRINT "F = "; F
30 NEXT F
RUN
F = 1
F=2
F=3
F = 4
F=5
F=6
```

In every FOR-NEXT loop, the FOR statement is the beginning point of the loop and the NEXT statement is always the last statement in the loop. The statement or statements between FOR and NEXT are executed, in order, over and over again, with the FOR statement indicating to the computer how many times the loop is to be executed.
(a) You can see from the RUN of the FOR-NEXT loop that each time through the loop the value of $F$ is automatically increased by
(b) How many times did the computer go through the loop? $\qquad$
(c) Why did the computer stop after going through the loop the above number of times? $\qquad$
(d) What other statement must you have?

-     -         -             -                 -                     -                         -                             - 

(a) 1
(b) 6
(c) because the FOR statement told it to go from 1 to 6.
(d) a NEXT statement
3. As you can see in the program below, the computer will continue with the rest of the program when it has completed the loop as specified by the FOR statement.

```
5 REM***ANOTHER FOR-NEXT LOOP
10 FOR D=5 TO 10< Note that the loop doesn't have to
2ø PRINT "D = "; D
30 NEXT D
4\varnothing PRINT
50 PRINT "AHA! OUT OF THE LOOP BECAUSE"
6\emptyset PRINT "D = "; D: "WHICH EXCEEDS 1\varnothing."
RUN
D = 5
D=6
D = 7
D = 8
D = 9
D = 1\varnothing
```

AHA! OUT OF the LOOP because
$D=11$ WHICH EXCEEDS $1 \varnothing$

In the program, the FOR-NEXT loop occupies which lines? $\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

lines 10,20 , and 30
4. How does the FOR-NEXT loop work? Follow the arrows.


In line $10, \mathrm{~N}$ is set equal to 1 .

In line $30, \mathrm{~N}$ is increased by one, and the computer compares the increased value of N to the upper limit for N indicated in the FOR statement.

Let's look at the FOR statement.
When N goes past this value, the computer stops executing the loop and continues on with the rest of the program past the FOR-NEXT loop (if there is more to the program). We call this the limit of N , or
$1 \varnothing$ FOR N = 1 TO 3


This is the FOR-NEXT loop control variable. the limit of the FOR variable.

This is the
first value N will have.

Here is a RUN of the program above.

```
FOR N=1 TO 3
PRINT N
NEXT N
RUN
```

1
1
3
3
3

Each time the computer comes to a NEXT N statement, it increases the value of N by one, and checks the new value against the limit for N . In this case, the limit is 3 , because the FOR statement reads: FOR $\mathrm{N}=1$ TO 3 . When the value of N is greater than 3 , the computer continues on to the next statement after the NEXT statement, if there is one. If not, the computer has finished executing the program and stops. Got that? Let's see.

Statement 10 means that for the first time through the loop, $\mathbf{N}=1$. The second time through, $\mathrm{N}=\mathrm{N}+1=1+1=2$. The third time through, $\mathrm{N}=$
$\qquad$ = $\qquad$ $=$ $\qquad$ -.
$\mathrm{N}=\mathrm{N}+1=2+1=3$
5. Write a program with three statements that will print the word LOOP six times. Use a FOR-NEXT loop, and use C as the FOR-NEXT loop control variable. Show what your program will print when it is RUN.

```
1\varnothing FOR C = 1 TO 6
2\varnothing PRINT "LOOP"
30 NEXT C
RUN
LOOP
LOOP
LOOP
LOOP
LOOP
LOOP
```

6. FOR-NEXT statements can be used in a multiple statement line. Here is a FOR-NEXT program, all on one line. Follow the arrows.


When the computer had finished the FOR-NEXT loop and had made its exit from the loop, what was the value for N ? $\qquad$

## 6

Notice that the value for N after loop exit is one more than the upper limit for N as given in the FOR statement. That is how the computer recognized that it had performed the proper number of loops and was ready to go on to the next statement in the program beyond the FOR-NEXT loop.
7. Let's say you enter the following multiple-statement line.
$1 \varnothing$ PRINT "TESTING "; : FOR $X=1$ TO 4 : PRINT $x$ : " ": $:$ NEXT $x$
What will your computer print when you type RUN? $\qquad$

-     -         -             -                 -                     -                         -                             -                                 -                                     - 

TESTING 1234
8. Finish writing this program so that the computer will produce the RUN shown. Use a FOR-NEXT loop with Y as the control variable.

```
1\varnothing PRINT "THIS YEAR CATHY IS 10 YEARS OLD"
2ø
3\varnothing
4\varnothing
RUN
THIS YEAR CATHY IS 1\varnothing YEARS OLD
AND THE NEXT YEAR SHE WILL BE 11
AND THE NEXT YEAR SHE WILL BE 12
AND THE NEXT YEAR SHE WILL BE 13
AND THE NEXT YEAR SHE WILL BE 14
2\varnothing FOR Y = 11 TO 14
3ø PRINT "AND THE NEXT YEAR SHE WILL BE "; Y
4\varnothing NEXT Y
```

9. Another thing to notice about FOR-NEXT loops is that variables may be used instead of numbers, providing, of course, that the variables have been assigned values earlier in the program. In the example below, values are assigned by LET statements. Values could also have been assigned by INPUT or READ statements.
```
1\varnothing A=3:B=8
20 FOR C=A TO B
30 PRINT " "; C ;
4\varnothing NEXT C
RUN
    3}4
```

Rewrite the FOR statement (line 20), substituting numerical values for variables A and B . Use the values that were assigned by the program above.

20 $\qquad$
$-\ldots-\ldots-\ldots-\infty$
$2 \varnothing$ FOR C $=3$ TO 8
10. Play computer and show the RUN for this FOR-NEXT demonstration program.

```
1\varnothing X=\varnothing : Y=4
2\varnothing FOR Z=X TO Y
4\varnothing PRINT " "; Z
50 NEXT Z
RUN
```

$-\ldots-\ldots-\ldots-\ldots$
RUN
$\begin{array}{lllll}0 & 1 & 2 & 3 & 4\end{array}$
11. Now you write a program where variables are used to set the initial and upper limits of the FOR-NEXT loop control variable. Have your program READ the values to be used for the initial and upper limits from a DATA statement.

Use Z for the control variable, and use X and Y for the variables that set the initial and upper limits. Select your DATA statement values so that your program will produce the following RUN.

## RUN

$1 \varnothing \varnothing 1 \varnothing 1 \quad 1 \varnothing 2 \quad 1 \varnothing 3 \quad 1 \varnothing 4 \quad 1 \varnothing 5$

```
READ X
2ø READ Y
30 FOR Z=X TO Y
4\varnothing PRINT " "; Z
50 NEXT Z
60 DATA 1\varnothing\varnothing,1\varnothing5
```

Statements 10 and 20 could be combined in one statement: 10 READ X, Y.
12. In this next program, an INPUT value (line 40) is used to establish the upper limit of the FOR statement (line 100), which tells the computer how many times to repeat " $\mathrm{X}=$ ?" When the program is RUN, the PRINT statements in lines $10-80$ tell the user how to use the program.

```
5 REM***FRIENDLY MEAN FROM INPUT VALUES
1\varnothing PRINT "FOR MY NEXT ENCDRE I WILL COMPUTE"
2\emptyset PRINT "THE MEAN OF A LIST OF NUMBERS."
3\varnothing PRINT
4\varnothing PRINT "HOW MANY NUMBERS IN THE LIST"; : INPUT N
50 PRINT
60 PRINT "EACH TIME I TYPE 'X =?' YOU TYPE IN"
70 PRINT "ONE NUMBER AND THEN PRESS RETURN."
8@ PRINT
9@ T=\varnothing
1øø FOR K=1 TO N
11\varnothing PRINT " }x="\mathrm{ ; : INPUT }
120 T=T+X
130 NEXT K
14\varnothing M=T/N
150 PRINT
16\emptyset PRINT "TOTAL = "; T
170 PRINT "MEAN = "; M
```

(a) In the program above, the FOR-NEXT loop occupies lines
$\qquad$
(b) What is the FOR-NEXT loop control variable? $\qquad$
(c) The upper limit for the control variable is determined by the value assigned to which other variable? $\qquad$
(a) $100,110,120,130$
(b) K
(c) N
13. In the program of frame 12, which line in the FOR-NEXT loop will keep a running tally of the values entered for line 110 ? $\qquad$

-     -         -             -                 -                     -                         -                             - 

$12 \varnothing \mathrm{~T}=\mathrm{T}+\mathrm{X}$
14. This is a RUN of the program in frame 12.

```
RUN
FOR MY NEXT ENCORE, I WILL COMPUTE
THE MEAN OF A LIST OF NUMBERS.
HOW MANY NUMBERS IN THE LIST? 5
EACH TIME I TYPE 'X =?' YOU TYPE IN
ONE NUMBER AND THEN PRESS RETURN.
x =? 16
x =? 46
x =? 38 \ Values entered by user.
X =? 112
x=? 23
TOTAL = 235
MEAN = 47
```

Show the numerical values in the FOR statement for the above RUN.

1øø FOR K = $\qquad$ то $\qquad$

-     -         -             -                 -                     -                         -                             - 

1 то 5 (The value entered for INPUT N was 5. .)
15. Here is the beginning of another RUN of the same program.

```
RUN
FOR MY NEXT ENCORE, I WILL COMPUTE
THE MEAN OF A LIST OF NUMBERS.
```

HOW MANY NUMBERS IN THE LIST: $4 \longleftrightarrow$ Value entered by user.
How many times will ' $\mathrm{X}=$ ?'' be printed? $\qquad$ How many times will the statements between the FOR-NEXT statements be executed? $\qquad$

## 4; 4

Just to prove it to you, this is the rest of the same RUN.

```
EACH TIME I TYPE 'X =?' YOU TYPE IN
ONE NUMBER AND THEN PRESS RETURN.
x =? 2
x=? 4
x =? 6
x =? 8
TOTAL = 2ø
MEAN = 5
```

16. Complete the following program to compute the product $(\mathrm{P})$ of N numbers. Think carefully about the effect of your statements when the program is RUN.
```
5 ~ R E M * * * P R O D U C T ~ C A L C U L A T E D ~ F R O M ~ A ~ L I S T ~ O F ~ N U M B E R S ~
1\varnothing PRINT "YOU WANT ANOTHER ENCORE? I'LL COMPUTE"
2ø PRINT "THE PRODUCT OF A LIST OF NUMBERS."
3@ PRINT
4\varnothing PRINT "HOW MANY NUMBERS IN THE LIST"; : INPUT N
5@ PRINT
6ø PRINT "EACH TIME I TYPE 'X =?' YOU TYPE IN"
7\varnothing PRINT "ONE NUMBER AND THEN PRESS RETURN."
80 PRINT
1\propto\varnothing~<_ Initialize
11\varnothing
136 P=P*X
140
150 PRINT : PRINT "PRODUCT = "; P
RUN
YOU WANT ANOTHER ENCORE? I'LL COMPUTE
THE PRODUCT OF A LIST OF NUMBERS.
HOW MANY NUMBERS IN THE LIST? 5
EACH TIME I TYPE 'X =?' YOU TYPE IN
ONE NUMBER AND THEN PRESS RETURN.
x =? 7
x =? 12
x =? 4
x =? 3
x =? 19
PRODUCT = 19152
1\varnothing\varnothing LET P=1
110 FOR K=1 TO N
140 NEXT K
```

17. Any BASIC expression may be used to set both the initial and the maximum value of a FOR-NEXT loop control variable. The computer evaluates these expressions (that is, does the arithmetic) before the loop is executed the first time, and does not recompute these values each time through the loop.

Look at the FOR statement in this next program, and then decide whether the computer executed the loop the proper number of times.

```
1. Q=4
2\varnothing FOR P=Q TO 2*Q-1
3\varnothing PRINT " "; P;
40 NEXT P
RUN
    4 6 7 The computer was right!
```

In the following program, fill in the blanks in line 20 with expressions using the variable Q , so that when the program is RUN , it will produce the printout shown below.

```
1\varnothingQ=4
2ø FOR P=
```

$\qquad$

``` TO
``` \(\qquad\)
```

3ø PRINT " "; P;
40 NEXT P
RUN
2 3
20 FOR P=Q/2 TO Q*3 OR 2\emptyset FOR P=Q-2 TO Q+8

```

Note: If your answer is different and you think it is correct, try it on your computer and see if you get the same RUN that we did.
18. In the FOR-NEXT loops you have seen so far, the FOR-NEXT loop control variable takes the first value given in the FOR statement, and keeps that value until the computer comes to the NEXT statement. Then the FOR variable increases its value by one each time through the loop until it reaches the maximum value allowed by the FOR statement.

\[
X=5 \text {, then } 6 \text {, then } 7 \text {, then } 8 \text {, then } 9 \text {, and then } 10
\]

However, you can write a FOR statement that causes the value of the FOR-NEXT loop control variable to increase by multiples of other than one, or
by frational increments. You can also have the value of the FOR-NEXT variable decrease each time through the loop.
```

1\varnothing FOR }X=1\mathrm{ TO 1ø STEP 2

```

Tells the computer to increase the value of X by 2 every time through the FOR-NEXT loop, until X is greater than 10.


Tells the computer to increase the value of Y by 1.5 every time through the FOR-NEXT loop, until Y is greater than 6.


Note that Z will start at \(\mathrm{Z}=10\) and go to \(Z=5\)

Tells the computer to decrease the value of \(Z\) by 1 each time through the FOR-NEXT loop, until Z is less than 5 .

Some demonstration programs will show the effects of STEP in action.
```

1\varnothing FOR B=1 TO 1\varnothing STEP 2
2\emptyset PRINT " "; B;
30 NEXT B
4\varnothing PRINT
50 PRINT
60 PRINT "LOOP TERMINATES BECAUSE"
7\emptyset PRINT "B = "; B; ", WHICH IS GREATER THAN 1\varnothing."
RUN
1
LOOP TERMINATES BECAUSE
B = 11, WHICH IS GREATER THAN 1\varnothing.

```

The PRINT statement in line 40 "bumps" the computer off the line where it is held by the semicolon at the end of line 20. The PRINT statement in line 50 causes the space before line 60 is printed.

Note that the loop starts with the first value in the FOR statement (1) and increases by increments of 2 , until the value of \(B=11\) which exceeds the maximum value allowed (10). At that point, the computer terminates the loop and continues running the rest of the program.

Play computer again, and fill in the RUN for this program.
```

lø D=3 : FOR F=D TO 4*D STEP D : PRINT " "; F; : NEXT F

```
19. In this example, the STEP in the FOR statement is followed by a negative number. STEP may be used to decrease the value of the FOR variable in any size step, going from a large value to a smaller one.
```

1ø FOR J=1\varnothing\varnothing TO 1\varnothing STEP - 1\varnothing
2\varnothing PRINT " "; J;
30 NEXT J
RUN
1\varnothing\varnothing 9\varnothing 8\varnothing 7\varnothing 6\varnothing 50 4\varnothing 3\varnothing 2\varnothing 1\varnothing

```

Now you write one where the FOR-NEXT loop control variable E decreases in steps of 3 from 27 to 18 . Show the program and the RUN.
```

1\varnothing FOR E = 27 TO 18 STEP - 3
2ø PRINT " "; E;
30 NEXT E
RUN
27 24 21 18

```
20. As we mentioned, the steps in a FOR-NEXT loop can be fractional values, as in the following example.
```

1\varnothing FOR X = 5 TO 7.5 STEP . }2
2g PRINT " "; x;
3ø NEXT X
RUN
5 5.25 5.5 5.75 6 6.25 6.5 6.75 7 7.25 7.5

```

Show the RUN for this program if we changed line 10 to the following.
```

1』 FOR X = 5 TO 7.5 STEP . }
RUN

```
```

RUN
5 5.5 6 6.5 7 7.5

```
21. The FOR-NEXT loop is useful for such things as repeated calculations, counting or keeping tallies, and dealing with cyclical or recurring events.

One such recurring event is the monthly compounding of interest on a savings account. In the following program, monthly interest (I) is calculated in line 180 by multiplying the initial amount of money ( P for Principal) by the Rate of interest (R).

The rate of interest is converted to a decimal fraction: \(\mathrm{R}=5\) percent \(=\) \(5 / 100=.05\)

Since 5 percent is the yearly rate of interest, only \(1 / 12\) of the calculated amount of interest is added to the principal each month.
```

1øø REM***MONTHLY INTEREST COMPOUNDING
110 PRINT "PRINCIPAL" ; : INPUT P
120 PRINT "YEARLY INTEREST RATE (IN %)"; : INPUT R
130 PRINT "HOW MANY MONTHS"; : INPUT M
140 PRINT
15% PRINT "MONTH", "AMOUNT"
160 FOR K=1 TO M
17@ PRINT K, P
18\varnothing I=(P* (R/1\emptyset\emptyset))/12
190 P=P+I
20. NEXT K
RUN
PRINCIPAL? 20|
YEARLY INTEREST RATE (IN %)? 5
HOW MANY MONTHS? }
MONTH AMOUNT
1 20ø
3 201.670138
4 202.51043
5 203.354223
6 204.201532

```

This table shows the amount of money in the account at the beginning of each month.
(a) Which lines are included in the FOR-NEXT loop?
(b) Which variable keeps track of and is used to print the number corresponding to the month for each line in the table?
(c) Line 150 prints the column headings for the table. The words used in the headings are separated by commas. In line 170, the values to be printed under the headings are also separated by commas, so that the spacing of headings and the numbers that go under headings match up. What would happen if the statement that prints the heading were included in the FOR-
NEXT loop?
(b) Which variable keeps the ther cormpond headings are separated by
(d) Which line keeps a running tally of Principal plus Interest? \(\qquad\)
- - - - - - - - -
(a) \(160,170,180,190,200\)
(b) the FOR variable K
(c) The heading would be printed every time through the loop, between each line of the table.
(d) 190

Note: If you want to brush up on your business math, a useful book would be Locke, Business Mathematics (a Self-Teaching Guide), John Wiley \& Sons, New York, 1972.
22. Yes, we admit, it is rather strange to see a "dollars and cents" answer printed as 200.833333 or 201.670138 . Fortunately, BASIC has a nifty way for rounding off numbers to a desired number of decimal places.

Recall how the INT function works (Chapter 4, Frame 20). The INT function chops off a number at the decimal point, keeps the integer part and discards the decimal fraction part. For example,
```

INT (200.833333) = 20ø

```

However, when dealing with dollars and cents, we don't want to lose the cents! So, we do it like this.
(1) Multiply by 100 .
\(100 * 200.833333=20083.333\)
(2) Add .5 .
\(20083.333+.5=20083.8333\)
(3) Keep the integer part.
\(\operatorname{INT}(20083.8333)=20083\).
(4) Divide by 100 .
\(20083 / 100=200.83\)

Your turn. Use the above procedure to round \(\$ 123.45678\) to the nearest penny.
(1) Multiply by 100 .
\(100 * 123.45678=\) \(\qquad\)
(2) Add .5 .
(3) Keep the integer part.
(4) Divide by 100 .
(1) \(100 * 123.456789=12345.678\)
(2) \(12345.678+.5=12346.178\)
(3) \(\operatorname{INT}(12346.178)=12346\).
(4) \(12346 / 100=123.46\)
23. The following program is a step by step demonstration of the rounding method shown in the previous frame.
```

1%% REM**STEP BY STEP DEMONSTRATION OF ROUNDING
11\varnothing PRINT "NUMBER TO BE ROUNDED"; INPUT A
12\varnothing PRINT "START WITH YOUR NUMBER, A = ";A
130}A=100%
14\varnothing PRINT "(1) MULTIPLY BY 1\varnothing\varnothing, A = ";A
15\varnothing A = A +.5
160 PRINT "(2) ADD .5, A = ";A
17% A = INT(A)
18% PRINT "(3) KEEP INTEGER PART, A = ":A
19\varnothing A = A/10\varnothing
20ø PRINT "(4) DIVIDE BY 10ø, A= ";A
210 PRINT "A IS NOW ROUNDED TO 2 DECIMAL PLACES"
220 PRINT
230 GOTO 11\varnothing
RUN
NUMBER TO BE ROUNDED? 123.45678
START WITH YOUR NUMBER, A = 123.45678
(1) MULTIPLY BY 1øø, A = 12345.678
(2) ADD . 5, A = 12346.178
(3) KEEP INTEGER PART, A = 12346.
(4) DIVIDE BY 1\varnothing\varnothing, A = 123.46
A IS NOW ROUNDED TO 2 DECIMAL PLACES

```

One more example. You fill in the values of A. (Try using our program on your Atari!)

NUMBER TO BE ROUNDED. 203.7249
START WITH YOUR NUMBER, \(A=\) \(\qquad\)
(1) MULTIPLY BY \(1 \varnothing \varnothing\) 。 \(A=\) \(\qquad\)
(2) ADD . 5, \(A=\) \(\qquad\)
(3) KEEP INTEGER PART, \(A=\) \(\qquad\)
(4) DIVIDE BY \(1 \varnothing \varnothing\).
\(A=\) \(\qquad\)
A IS NOW ROUNDED TO 2 DECIMAL PLACES
24. In our rounding program, the actual work of rounding is done by lines 130 , 150,170 and 190 . We can combine these four lines into a single statement to round a number, as follows.

(2) Add .5
(3) Keep the integer part

Remember, the above statement rounds the value of A to two decimal places.
(1) Write a statement to round the value of P to two decimal places.
(2) Write a statement to round the value of X to one decimal place.
(3) Write a statement to round the value of B to three decimal places.
(1) \(P=\operatorname{INT}\left(10 \varnothing^{*} P+.5\right) / 1 \varnothing \varnothing\)
(2) \(X=\operatorname{INT}\left(1 \varnothing^{*} x+.5\right) / 1 \varnothing\)
(3) \(B=\operatorname{INT}(1 \varnothing \varnothing \varnothing * B+.5) / 1 \varnothing \varnothing \varnothing\)

Try this. Add the statement \(195 \mathrm{P}=\mathrm{INT}\left(100^{*} \mathrm{P}+.5\right) / 100\) to the MONTHLY INTEREST COMPOUNDING program in frame 21. This should cause the numbers under AMOUNT to be rounded to the nearest penny. A RUN will look like this.

\section*{RUN}

PRINCIPAL?2øø
YEARLY INTEREST RATE (IN \%)? 5
HOW MANY MONTHS?6
\begin{tabular}{ll} 
MONTH & AMOUNT \\
1 & \(2 \varnothing \varnothing\) \\
2 & \(2 \varnothing \varnothing .83\) \\
3 & \(2 \varnothing 1.67\) \\
4 & \(2 \varnothing 2.51\) \\
5 & \(2 \varnothing 3.35\) \\
.6 & \(2 \varnothing 4.2\)
\end{tabular}
25. Can you have a FOR-NEXT inside another FOR-NEXT loop? Absolutely. It is called nested FOR-NEXT loops and is perfectly 'legal'" provided you follow the rule illustrated below.
```

10 FOR X = 1 TO 5
2\varnothing FOR Y = 1 TO 6
30 PRINT"*";
4\varnothing NEXT Y
50 NEXT X

```
RUN

This inside loop must be completely inside the other or outside loop. Otherwise you'll get an error message.

Count the stars. How many are there? Do you see any relationship between the number of stars printed and the numbers 5 and 6 which appear in the two FOR statements?

A loop within a loop is called a \(\qquad\) FOR-NEXT loop. The inside loop must be \(\qquad\) the outside loop.
```

_ - - - - - _ -

```
nested; inside
26. Here are two programs using nested FOR-NEXT loops.
5 REM*** PROGRAM A
5 REM*** PROGRAM A
1\varnothing FOR N=1 TO 4
1\varnothing FOR N=1 TO 4
20 FOR L=1 TO 3
20 FOR L=1 TO 3
30 PRINT "NESTED"
30 PRINT "NESTED"
4\varnothing NEXT L
4\varnothing NEXT L
5\varnothing PRINT" LOOP"
5\varnothing PRINT" LOOP"
60 NEXT N
60 NEXT N
5 REM***PROGRAM B
5 REM***PROGRAM B
1\varnothing FOR N=1 TO 4
1\varnothing FOR N=1 TO 4
20 FOR L= TO 3
20 FOR L= TO 3
3\varnothing PRINT "NESTED"
3\varnothing PRINT "NESTED"
4\varnothing NEXT N
4\varnothing NEXT N
5\emptyset PRINT " LOOP"
5\emptyset PRINT " LOOP"
60 NEXT L
60 NEXT L

Which program (A or B) has correctly nested FOR-NEXT loops? \(\qquad\)
- - - - - - - -
program A
27. Program A in frame 26 produces a repeated pattern of printout. Look at the program closely and then show what the computer will print when the program is RUN.
```

_ - - - - - - - -
RUN
NESTED
NESTED
NESTED
LOOP
NESTED
NESTED
NESTED
LOOP
NESTED
NESTED
NESTED
LOOP
NESTED
NESTED
NESTED
LDOP

```
28. The following program uses nested loops to print a rectangular pattern of "stars."
10 FOR R \(=1\) TO \(3 \quad\) This inner loop causes the computer to
\(2 \varnothing\) FOR \(C=1\) TO 7 print one row of seven stars.
\(3 \varnothing\) PRINT "*";
\(4 \varnothing\) NEXT C
50 PRINT
60 NEXT R
RUN
*******
** * * * *
*******
(1) What is the purpose of the empty PRINT statement in line 50 ?
(2) Why does the computer print 3 rows of stars? \(\qquad\) -
\(\qquad\)
\(\qquad\)
(1) It moves the cursor to the beginning of the next line after a row of stars has been printed by the inside loop.
(2) The outer loop, controlled by lines 10 and 60, causes the inner loop to be executed for \(\mathrm{R}=1,2\), and 3 . Each time, a row of stars is printed.
29. Show what will be printed if we run the following program.
\(1 \varnothing\) FOR A=1 TO 4
20 FOR B=1 TO 3
36 PRINT "?";
48 NEXT B
\(5 \varnothing\) PRINT
6ヵ NEXT A
RUN
??? The computer will print four (4) rows, each with three (3) ques-
? ? ?
? ? ? tion marks.
30. Write a program to print 7 rows with 12 dollars signs (\$) in each row. A RUN should look like the following.
```

RUN

\$\$\$\$\$\$\$\$\$\$\$\$

\$\$\$\$\$\$\$\$\$\$\$\$

\$\$\$\$\$\$\$\$\$\$\$\$

\$\$\$\$\$\$\$\$\$\$\$\$

\$\$\$\$\$\$\$\$\$\$\$\$

\$\$\$\$\$\$\$\$\$\$\$\$

\$\$\$\$\$\$\$\$\$\$\$\$
```
$1 \varnothing$ FOR $A=1$ TO 7
20 FOR Z=1 TO 12
30 PRINT "\$";
40 NEXT $Z$
$5 \emptyset$ PRINT
60 NEXT A

## SELF-TEST

Now that you have completed Chapter 6, you have acquired enough understanding of computer programming to be able to learn a lot more by experimenting at a computer terminal. As you look at our demonstration programs, you may see some possibilities that we do not specifically deal with. Build on your knowledge by trying out your own ideas.

But right now, find out if you really know how to use FOR-NEXT loops by doing the following programs.

1. Show what will be printed if we RUN the following program.
```
1\varnothing S=\varnothing
2\varnothing FOR K=1 TO 4
3\varnothing S=S+K
40 NEXT K
50 PRINT S
RUN
```

2. Show what will be printed if we RUN the following program.
```
1\varnothing P=1 : FOR K=1 TO 4 : P=P*K : NEXT K : PRINT P
RUN
```

3. Examine this program. Which of the three RUNs was produced by the program? $\qquad$
```
1\varnothingN=1
2\emptyset FOR K=1 TO N
3\varnothing PRINT "*";
4\varnothing NEXT K
5\emptyset PRINT
6\emptyset N=N+1
7\emptyset IF N>1\emptyset THEN END
8\varnothing GOTO 2\emptyset
```

RUN 1
RUN 2
RUN 3

4. Write a program to print a table of $\mathrm{N}, \mathrm{N}^{2}$, and $\mathrm{N}^{3}$. Use INPUT statements to indicate what list of numbers you wish included in the table. A RUN should look like this.

```
RUN
FIRST NUMBER? 4\varnothing
LAST NUMBER? 45
\begin{tabular}{lll}
\(N\) & \(N-S Q U A R E D\) & \(N-C U B E D\) \\
\(4 \varnothing\) & \(16 \varnothing \varnothing\) & \(64 \varnothing \varnothing \varnothing\) \\
41 & 1681 & 68921 \\
42 & 1764 & \(74 \varnothing 88\) \\
43 & 1849 & \(795 \varnothing 7\) \\
44 & 1936 & 85184 \\
45 & \(2 \varnothing 25\) & 91125
\end{tabular}
```

5. Show what will be printed if we RUN the following program.
```
1\varnothing S=\varnothing
2\varnothing FOR K=1 TO }7\mathrm{ STEP 2
3\varnothing S=S +K
4\varnothing NEXT K
5\emptyset PRINT S
RUN
```

6. On the following page, complete this program to print a table projecting growth rate of a population at specified intervals over a given time period (years). The formula for population growth is:

$$
\mathrm{Q}=\mathrm{P}(1+\mathrm{R} / 100)^{\mathrm{N}}
$$

where N is the number of years.

We want the population rounded to the nearest whole number.
$1 \varnothing \varnothing$ REM***REQUEST DATA AND PRINT HEADING
$11 \varnothing$ PRINT "INITIAL POPULATION"; : INPUT $P$
$12 \varnothing$ PRINT "GROWTH RATE": INPUT R
$13 \varnothing$ PRINT "INITIAL VALUE OF $N$ "; : INPUT A
$14 \varnothing$ PRINT "FINAL VALUE OF $N$ "; : INPUT $B$
150 PRINT "STEP SIZE"; : INPUT H
$16 \varnothing$ PRINT: PRINT "N", "POPULATION" : PRINT
2øø REM***COMPUTE AND PRINT TABLE
210
220
230
240
RUN
INITIAL POPULATION? $23 \varnothing$
GROWTH RATE? 1
INITIAL VALUE OF N? $\varnothing$
FINAL VALUE OF N? $1 \varnothing \varnothing$
STEP SIZE? 25

| $N$ | POPULATION |
| :--- | :--- |
| $\varnothing$ | $23 \varnothing$ |
| 25 | 295 |
| $5 \varnothing$ | 378 |
| 75 | 485 |
| $1 \varnothing \varnothing$ | 622 |

RUN
INITIAL POPULATION? $2 \varnothing 5$
GROWTH RATE? 1
INITIAL VALUE OF N? $\varnothing$
FINAL VALUE OF N? $1 \varnothing \varnothing$
STEP SIZE? $1 \varnothing$

| $N$ | POPULATION |
| :--- | :--- |
| $\varnothing$ | $2 \varnothing 5$ |
| $1 \varnothing$ | 226 |
| $2 \varnothing$ | $25 \varnothing$ |
| $3 \varnothing$ | 276 |
| $4 \varnothing$ | $3 \varnothing 5$ |
| $5 \varnothing$ | 337 |
| $6 \varnothing$ | 372 |
| $7 \varnothing$ | 411 |
| $8 \varnothing$ | 454 |
| $9 \varnothing$ | $5 \varnothing 2$ |
| $1 \varnothing \varnothing$ | 554 |

For U.S.A., 1970 (in millions of people).

Results are expressed in millions, rounded to the nearest million.
7. Write a program to compute and print the sum of whole numbers from 1 to N where the value of N is supplied in response to an INPUT statement. A RUN might look like the one on the following page.

```
RUN
GIVE ME A NUMBER (N) AND I WILL COMPUTE
THE SUM OF THE NUMBERS FROM 1 TO N.
WHAT IS N? 3
THE SUM IS 6 Because 1+2+3=6
WHAT IS N? 5
THE SUM IS 15
WHAT IS N? And so on.
```

8. Look back at the simple number guessing game in Chapter 1, frame 9. Use a FOR-NEXT loop to modify the program so that the user has only eight chances to guess the number. If he fails in eight guesses print an appropriate message before starting over again.
9. What will soon appear on the screen if we store and run the following program?
```
100 FOR R=1 TO 23
110 FOR C=1 TO 37
12\varnothing S=INT(6*RND(1)) + 1
138 IF S=1 PRINT "*";
14% IF S>1 PRINT " ";
150 NEXT C
160 PRINT
17% NEXT R
180 GOTO 180
```


## Answers to Self-Test

The frame numbers in parentheses refer to the frames in the chapter where the topic is discussed. You may wish to refer back to these for a quick review.

1. RUN

10
The answer is the sum of the values of K defined by the FOR statement ( $\mathrm{K}=1,2,3$, and 4). (frames 1-7)
2. RUN

24
The answer is the product of the values of K defined by the FOR statement ( $\mathrm{K}=1,2,3$, and 4). (frames 1-6, 16)
3. RUN 3. The FOR-NEXT loop (lines $20,30,40$ ) causes the computer to print a row of N stars. The loop is done for $\mathrm{N}=1,2,3, \ldots 10$.
(frames 1-6, 28)
4. $1 \varnothing$ INPUT "FIRST NUMBER"; A
$2 \varnothing$ INPUT "LAST NUMBER"; B
$3 \varnothing$ PRINT
$4 \varnothing$ PRINT "N", "N-SQUARED", "N-CUBED"
$5 \emptyset$ FOR $N=A$ TO B
$6 \varnothing$ PRINT $N, N \uparrow 2, N \uparrow 3$
$7 \varnothing$ NEXT N
(frames 9, 21)
5. RUN

16
Similar to question 1, but this time the values of $K$ defined by the FOR statement are $K=1,3,5$, and 7. (frame 18)
6. 200 REM***COMPUTE AND PRINT TABLE

210 FOR N=A TO B STEP H
220 LET $Q=P^{*}(1+R / 1 \varnothing \varnothing) \uparrow N$
$23 \varnothing$ PRINT N, INT( $Q+.5$ )
$24 \varnothing$ NEXT $N$, (frames 18-24) whole number.
7. $1 \varnothing$ PRINT "Give me a NUMber ( $N$ ) and i will compute"
$2 \varnothing$ PRINT "THE SUM OF THE NUMBERS FROM 1 TO N."
$3 \varnothing$ PRINT
$4 \varnothing$ PRINT "WHAT IS N";
50 INPUT $N$
If you wish, you can put these on one
55 LET $\mathrm{S}=\varnothing$
60 FOR $W=1$ TO $N$
$7 \varnothing$ LET S=S+W
$8 \varnothing$ 'NEXT W
$9 \varnothing$ PRINT "THE SUM IS";
$1 \varnothing 0$ GOTO 30
8. $1 \varnothing \varnothing$ REMARK***THIS IS A SIMPLE COMPUTER GAME $11 \varnothing$ LET X=INT ( $1 \varnothing \varnothing$ *RND (1) ) +1 $12 \emptyset$ PRINT
$13 \varnothing$ PRINT "I'M THINKING OF A NUMBER FROM 1 TO $1 \varnothing \varnothing$ "
$14 \varnothing$ PRINT "GUESS MY NUMBER!!!"
150 FOR $A=1$ TO 8 : PRINT "YOUR GUESS"; : INPUT G
$16 \varnothing$ IF G<X THEN PRINT "TRY A BIGGER NUMBER": GO TO $19 \varnothing$
$17 \varnothing$ IF G>X THEN PRINT "TRY A SMALLER NUMBER" : GO TO $19 \varnothing$
$18 \varnothing$ IF G=X THEN PRINT "THAT'S IT!!! YOU GUESSED MY NUMBER." : GO TO $11 \varnothing$ $19 \varnothing$ NEXT A : PRINT "TOO MANY GUESSES. THE NUMBER WAS" ; $X$ : GO TO $11 \varnothing$ (frames 2, 4)
9. The 'stars'" will come out. About $1 / 6$ of the screen will show stars; the other $5 / 6$ will be "blanks." The stars and blanks are selected at random by lines 120,130 , and 140 . Happy stargazing!

## CHAPTER SEVEN

## Subscripted Variables

In Chapters 7 and 8 we will present another useful tool, the subscripted variable. First we will discuss BASIC variables with a single subscript.

You will learn, for example, how to count votes from a survey and how to accumulate or count dollars and assign them to different groupings. And you will get lots more practice using FOR-NEXT loops.

Many new programming ideas are introduced in this chapter. Read the chapter slowly and carefully. Experiment on your computer; you will find that these new techniques give you much more range and flexibility. When you complete this chapter, you will be able to:

- recognize and use subscripted variables with a single (one) subscript;
- assign values to subscripted variables;
- use subscripted variables with variables for subscripts;
- use one-dimensional arrays to store the values of subscripted variables;
- use the DIM statement to tell the computer the maximum size of the array(s) used by a program.

1. The concept we discuss here will require your close attention. Take it slowly, and read carefully as we enter the mysterious realm of subscripted variables.

Until now, we have used only simple BASIC variables. A simple variable consists of a letter (any letter A to Z) or a letter followed by a single digit (any digit 0 to 9 ). For example, the following are simple variables.

```
P
```

Now we want to introduce a new type of variable, called a subscripted variable.


Say it: "P sub 5"
A subscripted variable consists of a letter (any letter A to Z) followed by a subscript enclosed in parentheses. $\mathrm{P}(3)$ is a subscripted variable; P 3 is not a subscripted variable.

Which of the following are subscripted variables? Circle the answer(s).

```
X(1) X X1 C(23) D
```

$\mathrm{X}(1) ; \mathrm{C}(23)$
Note: X, X1, and X(1) are three distinct variables. All three can appear in the same program. They may confuse $y o u$, but the computer will recognize them as three different variables.
2. A subscripted variable (like the simple variables we have been using) names a memory location inside the computer. You can think of it as a box, a place to store a number.


A set of subscripted variables is also called an array. This set of subscripted variables is a one-dimensional array, also known as a vector. In Chapter 8, we will discuss two-dimensional arrays.

Pretend you are the computer, and LET $\mathrm{P}(2)=36$. In other words use your pencil or pen and write the number 36 in the box labeled $\mathrm{P}(2)$ in the drawing above. Then LET $P(3)=12$. (Do it.) Now LET $P(7)=P(2)+P(3)$. Check yourself by looking at our answer following the dashed line.

| $\mathrm{P}(0)$ |  |
| :---: | :---: |
| $\mathrm{P}(1)$ |  |
| $\mathrm{P}(2)$ | 36 |
| $\mathrm{P}(3)$ | 12 |
| $\mathrm{P}(4)$ |  |
| $\mathrm{P}(5)$ |  |
| $\mathrm{P}(6)$ |  |
| $\mathrm{P}(7)$ | 48 |
| $\mathrm{P}(8)$ |  |

3. Subscripted variables can have variables for subscripts. The subscripted variable, $\mathrm{Y}(\mathrm{J})$, has the variable J for a subscript.

If $\mathrm{J}=1$ then $\mathrm{Y}(\mathrm{J})$ is $\mathrm{Y}(1)$
If $\mathrm{J}=2$ then $\mathrm{Y}(\mathrm{J})$ is $\mathrm{Y}(2)$
If $\mathrm{J}=7$ then $\mathrm{Y}(\mathrm{J})$ is $\mathrm{Y}(7)$
Let us assume that the values (in the boxes below) have been assigned to the corresponding variables. Note that both simple and subscripted variables are shown here.

A


Write the value of each variable below.

| $Y(1)=$ |  |  |
| :---: | :---: | :---: |
| $\mathrm{Y}(2)=$ |  |  |
| $\mathrm{Y}(\mathrm{C})=$ |  |  |
| $\mathrm{Z}(\mathrm{A})=$ |  |  |
| 4 | 1 | 4 |
| -3 | 2 | -3 |
| 5 | 2 | 3 |
| 4.7 | 9.2 | 6 |

$\mathrm{A}=$ $\qquad$
$\mathrm{Y}(\mathrm{A})=$ $\qquad$
$B=$ $\qquad$

$$
\mathrm{Y}(\mathrm{~B})=
$$

$\qquad$
$\mathrm{Y}(\mathrm{C})=$ $\qquad$
$\qquad$ $X(B)=$ $\qquad$
$Z(A)=$
$Z(B)=$ $\qquad$
$Y(D)=$ $\qquad$
4. So far we have only used single variables as subscripts. However, the subscript can be more complex. Below are two examples, still using the variables and values in the boxes in frame 3.

$$
\begin{aligned}
& Y(A+1)=Y(1+1)=Y(2)=-3 \\
& Y(2 * B)=Y(2 * 2)=Y(4)=6
\end{aligned}
$$

Notice that the expressions inside the subscript parentheses are computed using the same rules for BASIC arithmetic as an expression in a PRINT statement, or inside a function parentheses.

Now you complete some examples as we did above, showing both the value calculated for the subscript and the value assigned to the subscripted variable with that subscript. (Refer to the boxes in frame 3.)

$$
\begin{aligned}
& Y(A+2)= \\
& Y\left(2^{*} A-1\right)= \\
& Y(A+B)= \\
& Y\left(B^{*} C-D\right)= \\
& Y(A+3)= \\
& Y(D-3)= \\
& Y(D-C+A)= \\
& Y((C+D)-(A+B))=------ \\
& -----1) \\
& Y(A+2)=Y(1+2)=Y(3)=5 \\
& Y(2 * A-1)=Y(2 * 1-1)=Y(2-1)=Y(1)=4 \\
& Y(A+B)=Y(1+2)=Y(3)=5 \\
& Y(B * C-D)=Y(2 * 3-4)=Y(6-4)=Y(2)=-3 \\
& Y(A+3)=Y(1+3)=Y(4)=6 \\
& Y(D-3)=Y(4-3)=Y(1)=4 \\
& Y(D-C+A)=Y(4-3+1)=Y(1+1)=Y(2)=-3 \\
& Y((C+D)-(A+B))=Y((3+4)-(1+2))=Y(7-3)=Y(4)=6
\end{aligned}
$$

5. You will recall that previously you had to tell the computer how much space to reserve in its memory for the strings to be assigned to string variables in your program. In a similar fashion, you must also DIMension subscripted variables for the maximum number of values to be assigned to a particular subscripted variable. That is, you must tell the computer the largest subscript it is to permit for a subscripted variable by using a DIM statement. "DIM'" is the abbreviation for the "dimension" of an array of subscripted variables. The DIM statement(s) in your program must be placed so that they are executed before the subscripted variable(s) are actually used in the program, or an error message will result and the execution of the program will stop. The format for dimensioning an array is shown below. Note that it is similar to dimensioning a string variable.

Variable for which space is being reserved

Maximum subscript to be permitted

The above DIM statement specifies a subscripted variable which can have a maximum subscript of $\qquad$ —.
6. Suppose we wanted to specify that the maximum subscript is 50 . Write the DIM statement.

```
105
105 DIM X(50)
```

7. So how can subscripted variables contribute to the ease and versatility of programming in BASIC? One common use of subscripted variables is to store a list of numbers entered via INPUT or READ statements. This can be done with a FOR-NEXT loop. The control variable can also be used as the variable for the subscript in a subscripted variable, causing the subscript to increase by one each time through the loop. To illustrate, again we will turn to The World's Most Expensive Adding Machine.
```
1\varnothing\varnothing REM***WORLD'S MOST EXPENSIVE
1\varnothing5 REM***ADDING MACHINE (AGAIN)
11\varnothing DIM X(1\varnothing)
12\varnothing PRINT "HOW MANY NUMBERS";
13\varnothing INPUT N
14\varnothing PRINT
15\varnothing FOR K=1 TO N
160 PRINT "X=";
17\varnothing INPUT }
18\emptyset X (K)=X
19\varnothing NEXT K
2\varnothing\varnothing T=\varnothing
210 FOR K=1 TO N
220 LET T=T+X(K)
230 NEXT K
24\varnothing PRINT "THE TOTAL IS "; T
RUN
HOW MANY NUMBERS?5
```

$x=? 37$
$x=? 23$
$x=? 46$
$x=? 78$
$X=? 59$
THE TOTAL IS 243

For the RUN shown, N is 5 . Therefore, 5 numbers will be entered by the operator and stored in $\mathrm{X}(1)$ through $\qquad$ .
8. Notice especially lines 170 and 180 in the previous frame. First, the input value is assigned to the simple numeric variable X . Then the subscripted variable $\mathrm{X}(\mathrm{K})$ is assigned the same value by letting $\mathrm{X}(\mathrm{K})=\mathrm{X}$.

Now suppose the computer is running the program in frame 7. It has just completed the FOR-NEXT loop in lines 150 to 190 . The numbers entered by the user are now stored as follows.

| N | 5 |
| :---: | :---: |
| $\mathrm{X}(1)$ | 37 |
| X(2) | 23 |
| X(3) | 46 |
| X(4) | 78 |
| $\mathrm{X}(5)$ | 59 |

The computer is ready to proceed with line 200. This statement initializes the variable T, that is, gives T its first value. Show the value of T after line 200 has been executed.

T

9. Next, the computer will execute the FOR-NEXT loop in lines 210 to 230. How many times will the FOR-NEXT loop be executed?

5 times, because line 210 says $F O R \mathrm{~K}=1 \mathrm{TO} \mathrm{N}$ and N is equal to 5
10. The FOR-NEXT loop in lines 210 to 230 will be done 5 times, first for $\mathrm{K}=$ 1 , then for $K=2, K=3, K=4$, and finally for $K=5$. Let's look at line 220, where $K$ is used as a subscript.

```
22ø LET T=T+X(K)
```

This statement tells the computer to add the value of $\mathrm{X}(\mathrm{K})$ to the old value of T and then assign the results as the new value of T .

What is the value of T after line 220 has been executed for $\mathrm{K}=1$ ?
$\qquad$ For $K=2$ ? $\qquad$ For $\mathrm{K}=3$ ? $\qquad$ For $K=4$ ?
$\qquad$ For $K=5$ ? $\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

37; 60; 106; 184; 243
11. Let's use the World's Most Expensive Adding Machine to compute the sum of whole numbers, 1 through 12.

```
RUN
HOW MANY NUMBERS? 12
x =? 1
x=? 2
x =? 3
x =? 4
x =? 5
x =? 6
x =? 7
x=? 8
x =? 9
x =? 1ø
X=? 11
ERROR- AT LINE 18\varnothing
```

This time we got an error message telling us that we had a bad subscript. What was the largest subscript for $\mathrm{X}(\mathrm{K})$ that the computer would accept before it gave us an error message? $\qquad$

$1 \varnothing$
12. Change line 110 to allow us to input more numbers by substituting the following statement:

```
11\varnothingDIM X(1\varnothing\varnothing)
```

Now RUN the program again using the 12 numbers that gave us trouble before.

RUN
HOW MANY NUMBERS: 12
$x=$ ? 1
$x=3 \quad 2$
$x=$ ? 3
$x=$ ? 4
$x=$ ? 5
$x=$ ? 6
$x=$ ? 7
$x=$ ? 8
$x=$ ? 9
$x=$ ? $1 \varnothing$
$x=$ ? 11
$x=$ ? 12
THE TOTAL IS 78
Now the program can be used to compute the sum of at most how many numbers? $\qquad$

-     -         -             -                 -                     -                         -                             - 

100. If 100 numbers are entered they will be stored in $X(1)$ through $X(100)$, the limit specified by the DIM statement in line 110 . We can, of course, also use the program to compute the sum of fewer than 100 numbers.
101. A DIM statement may have its dimensions assigned by a variable. Look at the examples below.
```
DIM X(N)
DIM A(B)
DIM D \((Y+2)\)
```

You may only dimension an array once during the RUN of a program. The computer will give you an error message and stop executing the program if it comes to a DIM statement for the same array a second time and tries to redimension the array during the same RUN.

Look at the program segment below, and the beginning of the RUN. We have deleted line 110 and placed the DIM statement at the beginning of line 150.

```
.
12\emptyset PRINT "HOW MANY NUMBERS";
13ø INPUT N
14@ PRINT
15\varnothing DIM X(N) : FOR K=1 TO N
:
RUN
HOW MANY NUMBERS:8
```

What will be the dimensioned size of the array during this RUN of the program?

8 (the value assigned to N by the INPUT statement)
14. Where else in the program segment shown in frame 13 could DIM $X(N)$ be placed?

## - - -

In line 130 after INPUT N, or in line 140 either before or after PRINT. But notice that the DIM statement must be placed after the input value has been entered, but before the FOR-NEXT loop so that the array $\mathbf{X}(\mathrm{K})$ is dimensioned only once during the same RUN. The DIM X(N) statement could also be on a single line by itself, using a line number between 130 and 140 or between 140 and 150 .
15. Look at the first FOR-NEXT loop (lines $150-190$ ) in the program in frame 7. The first value assigned to $K$ is 1 , so the first subscripted variable $X(K)$ is $\mathrm{X}(1)$. Since the array could start with X(0), an array dimensioned as DIM X(100) can actually hold how many values? $\qquad$
Show how we could modify the FOR statement so that we could take advantage of every element (subscripted variable value) in the array for storing values, provided that $\mathrm{N}=100$.

```
----------
1\varnothing1
FOR K=\varnothing TO N
```

16. Instead of using an INPUT statement to get values for $\mathbf{X}(1), X(2)$, and so on, we can use READ and DATA statements. We'll put the value of $N$ and the values of $\mathrm{X}(1)$ through $\mathrm{X}(\mathrm{N})$ in a DATA statement, as follows.

DATA 5, 37, 23, 46, 78, 59
A A A A A
Value of $N$ Values of $X(1)$ through $X(5)$

```
1ø\varnothing REM ** WORLD'S MOST EXPENSIVE
1ø5 REM ** ADDING MACHINE YET AGAIN
110 DIM X(1\varnothing见)
208 REM ** READ N & }X(1) THRU X(N
210 READ N
22g FOR J=1 TO N
23\varnothing READ }X:X(J)=
24@ NEXT J
3ø\varnothing REM ** PRINT VALUE OF N & X ARRAY
310 PRINT "N="; N
32\emptyset PRINT "X(1) THRU X(";N;") ARE:"
330 FOR K=1 TO N
340 PRINT " "; x(K);
35@ NEXT K
36\varnothing PRINT
4\varnothing\varnothing REM ** TOTAL OF X ARRAY VALUES
41\varnothing T=\varnothing
4 2 0 ~ F O R ~ L = 1 ~ T O ~ N
430 T=T+X(L)
440 NEXT L
5ø凤 REM ** PRINT TOTAL: START AGAIN
510 PRINT "THE TOTAL IS "; T
52\emptyset PRINT
53@ GOTO 21ø
9\emptyset\varnothing REM ** HERE ARE TWO SETS OF DATA
910 DATA 5,37,23,46,78,59
920 DATA 12,1,2,3,4,5,6,7,8,9,1\varnothing,11,12
```

In the first FOR－NEXT loop（lines 220－240），we used J as the subscript． This choice was entirely arbitrary．What subscript did we use in lines 330 to 350 ？
$\qquad$ Lines 420 to 440 ？ $\qquad$

K；L

17．If we had wanted to，could we have used $\mathbf{J}$ as the subscript in all three places？ $\qquad$
ーーーーーーーーーー
Yes．These are three separate and distinct FOR－NEXT loops．We could have used any variable as the subscript except $\mathrm{N}, \mathrm{T}$ ，or X ．

18．The following questions refer back to the program in frame 16.
（a）For the second set of data，which statement assigns the first item in the
DATA statement to a variable？
（b）Which statements assign the rest of the data to a subscripted variable？
(c) Which statement prints values stored in an array instead of from the DATA statement?
(d) Which statement tallies or adds up all the values stored in the array?

-     -         -             -                 -                     -                         -                             -                                 - 

(a) $21 \varnothing$ READ $N$
(b) 230 READ $x: x(J)=x$
(c) $34 \varnothing$ PRINT $x(K)$;
(d) $43 \varnothing \mathrm{~T}=\mathrm{T}+\times(\mathrm{L})$

Note: Refer back to frame 8 for an explanation and suggestion regarding line 230.
19. Suppose we RUN the program in frame 16. Show what the RUN will look like. (Hint: Check all the PRINT statements.)

```
RUN
N=5
X(1) THRU X(5) ARE:
    37 23 46 78 59
THE TOTAL IS 243
N=12
x(1) THRU x(12) ARE:
    112
THE TOTAL IS 78
ERROR- 6 AT LINE 21%
```

20. So that you can better understand and use subscripted variables in your programming, here's a little more practice at doing what a computer does when dealing with subscripted variables.

For this segment of a computer program, fill in the boxes showing the values of $\mathrm{D}(\mathrm{G})$ at the affected locations after this FOR-NEXT loop has been run.

```
10 DIM D(3)
20 FOR G=1 TO 3
3\varnothing D(G)=2*G-1
4\varnothing NEXT G
```



D(2)

D(3) $\square$

| D(1) | 1 | For $\mathrm{G}=1,2 * \mathrm{G}-1=2 * 1-1=2-1=1$ |
| :---: | :---: | :---: |
| D(2) | 3 | For $\mathrm{G}=2,2 * \mathrm{G}-1=2 * 2-1=4-1=3$ |
| D(3) | 5 | For $\mathrm{G}=3,2 * \mathrm{G}-1=2 * 3-1=6-1=5$ |

21. For the following FOR-NEXT loop, fill in the boxes showing the values in $R(1)$ through $R(4)$ after the loop has been carried out.
```
1\varnothing DIM R(1\varnothing)
2g FOR R=1 TO 4
3\varnothing R(R)=R+2
4\varnothing NEXT R
4』 NEXT R
```

(Remember R and ( R ) are different variables.)


| R(1) | 3 | For $\mathrm{R}=1, \mathrm{R}+2=1+2=3$ |
| :---: | :---: | :---: |
| R(2) | 4 | For $\mathbf{R}=2, \mathrm{R}+2=2+2=4$ |
| R(3) | 5 | For $\mathrm{R}=3, \mathrm{R}+2=3+2=5$ |
| R(4) | 6 | For $\mathrm{R}=4, \mathrm{R}+2=4+2=6$ |

22. Let's do one more of these. Show what values will be in the boxes after this FOR-NEXT loop has been executed.
```
1\varnothing DIM P(1\varnothing)
2ø FOR N=1 TO 6
3ø P(N)=2*N
4| NEXT P
```



P(4)


P(6)


-     -         -             -                 -                     -                         -                             -                                 - 

P(1) $\square$ $P(2)$

$\square$ $P(5)$

$\mathrm{P}(6)$12
23. Next, assume that numbers are stored in $C(1)$ through $C(5)$, as follows:

$C(4) \quad 20$
C(5) $\square$

What will be printed if the following FOR-NEXT loop is carried out?

```
10\varnothing DIM C(1\varnothing)
11\varnothing FOR A=1 TO 5
12\varnothing PRINT " "; C(A);
13ø NEXT A
RUN
```

$-\ldots-\ldots-\ldots-\ldots-\ldots$
RUN
$\begin{array}{lllll}18 & 34 & 12 & 20 & 17\end{array}$
24. Suppose numbers are stored in $\mathrm{C}(1)$ through $\mathrm{C}(5)$ as shown in frame 23. What will be printed if the following FOR-NEXT loop is carried out?

```
10\varnothing DIM C(1\varnothing)
11\varnothing FOR A=5 TO 1 STEP - 1
120 PRINT " "; C(A);
130 NEXT A
RUN
```

RUN
$17 \quad 2 \varnothing 123418$

The values are printed in reverse order. If you missed this, review Chapter 6, frames 18 and 19.
25. Assume that an election is approaching and you have conducted a poll among your friends, using the following questionnaire.

Who will you vote for in the coming election? Circle the number to the left of your choice.

1. Sam Smoothe
2. Gabby Gruff

Let's write a program to count the votes each candidate received in the poll. You have 35 responses to your questionnaire, each response being either a " 1 " or a ' 2 ". First, record the votes in DATA statements.

```
91\varnothing DATA 1,1,2,2,2,1,1,2,2,2,1,1,1,2
920 DATA 1,2,1,1,2,2,1,1,1,2,1,2,2,2,
93ø DATA 1,1,2,1,-1
End-of-data flag (not a vote)
```

How many votes did Sam Smoothe receive? $\qquad$
26. How many votes did Gabby Gruff receive? $\qquad$ (Do your answers total 32?)

```
- - - - - - - - -
```

15
27. To answer those last two questions, you probably counted the 1 's in the DATA statements to find out how many votes Sam Smoothe received. Then you counted the 2 's to find out how many votes Gabby Gruff received.

Your computer can count votes by using subscripted variables to keep a running total of the 1's and 2's read from the DATA statements. When it comes to the end-of-data flag ( -1 ) it stops counting and prints the results. Here is a program to count the votes.

```
1\varnothing\varnothing REM***VOTE COUNTING PROGRAM
11\varnothing REM***INITIALIZE
12ø DIM C(2):C(1)=\varnothing : C(2)=\varnothing
2g\varnothing REM***READ AND COUNT VOTES
210 READ V
22ø IF V=-1 THEN 31\varnothing
23ø C(v)=c(v)+1 Crucial vote-counting statement.
240 GOTO 210
3øø REM***PRINT RESULTS
31ø PRINT "SAM SMOOTHE:"; C(1)
32ø PRINT "GABBY GRUFF:"; C(2)
910 DATA 1,1,2,2,2,1,1,2,2,2,1,1,1,2
920 DATA 1,2,1,1,2,2,1,1,1,2,1,2,2,2
930 DATA 1,1,2,1,-1
RUN
SAM SMOOTHE:17
GABBY GRUFF:15
```

Is the DIM statement really necessary? Why or why not? $\qquad$

Yes, arrays must always be DIMensioned.
28. After the computer executes line 120 , what are the values of $C(1)$ and $C(2)$ ?

C(1) $\square$

C(2)


Both have a value of 0 . These are the initial values prior to counting votes. We call the process initializing as shown in the REMark statement in line 110.
29. When your programs get so long that they start exceeding the computer's memory capacity, delete the REMarks to save memory space, as well as to save you time in typing in the programs you don't intend to store for later use.

To save memory space, which statements could be deleted from the program and still have it RUN as shown in frame 27? $\qquad$
$1 \varnothing \varnothing, 11 \varnothing, 2 \varnothing \varnothing$, AND $3 \varnothing \varnothing$
30. Look again at the crucial vote-counting statement from frame 27.

```
230 LET C(V)=C(V)+1
```

It is the subscripted variable equivalent of a similar statement which has been used in earlier programs to keep count, such as this one:

```
LET N=N+1
```

Note how the variable subscript of C is used to determine whether either the value of $\mathrm{C}(1)$ is increased by one, or the value of $\mathrm{C}(2)$ is increased by one. Since V can have only two values, either 1 or 2 , line 230 is actually a doublepurpose line. Depending on the value of V , line 230 is actually equivalent to:

```
LET C(1)=C(1)+1, Or LET C(2)=C(2)+1
```

When the preceding program is RUN, what values will the computer have stored for $\mathrm{C}(1)$ and $\mathrm{C}(2)$ after the first vote has been read and processed? (That is, lines 210 through 230 have been done for the first vote in the first DATA statement.)
C(1)

C(2)


What values will be stored for $\mathrm{C}(1)$ and $\mathrm{C}(2)$ after the second vote has been read and processed?
C(1)

C(2)


What values will be stored in $\mathrm{C}(1)$ and $\mathrm{C}(2)$ after the third vote has been read and processed?

$C(1) \square$
$C(2) \quad 0$
C(1)

C(2)

C(1)

C(2)

31. In the program we have been discussing (frame 27), line 220 checks for the end-of-data flag with the following statement.

```
IF V=-1 THEN 31\varnothing
```

If we switch lines 220 and 230 , this section of the program would look like this:

```
21\varnothing READ V
220 LET C(V)=C(V)+1
23\emptyset IF V=-1 THEN 31\varnothing
24\varnothing GOTO 210
```

(a) What would be the last value assigned to V from the DATA statement?
(b) If the computer used this value for V in line 220, what would the subscripted variable look like? $\qquad$
(c) Since negative subscripts are not allowed, what error message would our computer print? $\qquad$
(a) -1
(b) $\mathrm{C}(-1)$
(c) ERROR-a bad subscript. Moral: Beware of where you place the test for the end-of-data flag. The best place is usually right after the READ or INPUT statement where the flag might appear.
32. Suppose the following poll is conducted.

Which candidate will you vote for in the coming election? Circle the number to the left of your choice.

1. Sam Smoothe
2. Gabby Gruff
3. No opinion

The results of this poll are shown below.

$$
\begin{aligned}
& 2,2,2,1,2,1,1,2,1,1,3,2,1,3 \\
& 2,1,1,3,1,3,2,2,1,1,3,2,1,3 \\
& 1,1,2,1,2,1,1
\end{aligned}
$$

Modify the vote-counting program from frame 27 to process this data. You will have to add a line to set $\mathrm{C}(3)$ to zero and a PRINT statement to print the NO OPINION total. You will also have to change the DATA statements for the new data, as well as the DIM statement. Here is how it should RUN.

```
RUN
SAM SMOOTHE:17
GABBY GRUFF:12
NO OPINION:6
```

Write your program below.

```
1øø REM ** VOTE COUNTING PROGRAM
11ø REM ** INITIALIZE
120 DIM C(3)
13\varnothingC(1)=\varnothing:C(2)=\varnothing:C(3)=\varnothing
2\emptysetø REM ** READ AND COUNT VOTES
210 READ V
22ø IF V=-1 THEN 31\varnothing
230 C(V)=C(V)+1
24\varnothing GOTO 21\varnothing
3\varnothing\varnothing REM ** PRINT RESULTS
31\varnothing PRINT "SAM SMOOTHE:"; C(1)
320 PRINT "GABBY GRUFF:":C(2)
330 PRINT "NO OPINION:"; C(3)
91ø DATA 2,2,2,1,2,1,1,2,1,1,3,2,1,3
92ø DATA 2,1,1,3,1,3,2,2,1,1,3,2,1,3
93ø DATA 1,1,2,1,2,1,1,-1
\uparrow
```

Did you remember the flag?
33. Suppose we have a questionnaire with 4 possible answers, or 5 or 6 . Instead of writing a separate program for each, let's write one program to count votes for a questionnaire with N possible answers. The value of N will appear in a DATA statement prior to the actual answers, or votes. For example, the data for the questionnaire in frame 25 would look like this.

```
9\varnothing\varnothing REM ** THE DATA
901 REM ** FIRST DATA IS NUMBER-OF
902 REM ** POSSIBLE CHOICES
910 DATA 2
92ø DATA 1,1,2,2,2,1,1,2,2,2,1,1,1,2
93\varnothing DATA 1,2,1,1,2,2,1,1,1,2,1,2,2,2
940 DATA 1,1,2,1,-1
```

Line 910 is the value of N . In this case, N is 2 and possible votes are 1 or 2. How would the data for the questionnaire in frame 32 be placed in DATA statements?

```
9øø REM ** THE DATA
9ø1 REM ** FIRST DATA IS NUMBER OF
9ø2 REM ** POSSIBLE CHOICES
910 DATA
919 REM ** THE VOTES & THE FLAG (-1)
920
930
940
```

$\qquad$
$91 \varnothing$ DATA 3
920 DATA $2,2,2,1,2,1,1,2,1,1,3,2,1,3$
930 DATA $2,1,1,3,1,3,2,2,1,1,3,2,1,3$
940 DATA $1,1,2,1,2,1,1,-1$

This time $\mathrm{N}=3$ (line 910 ) and possible votes or 1,2 , or 3.
34. Your turn. Write a program to read and count votes for a questionnaire with N different possible answers (votes), where N is less than or equal to 20 . You will have to do the following things.
(1) DIMension for the maximum subscript for C . Remember, we said N is less than or equal to 20.
(2) Read the value of N .
(3) Set $\mathrm{C}(1)$ through $\mathrm{C}(\mathrm{N})$ to zero. (Use a FOR-NEXT loop.)
(4) Read and count votes until a flag is read.
(5) Print the results, as shown in the sample runs below.

Example: $\mathrm{N}=2$

## RUN

ANSWER \# 1 : 17 ANSWER \# 2 : 15

Example: $\mathrm{N}=5$
RUN
ANSWER * 1 : 12 ANSWER * $2: 7$ ANSWER * $3: 9$ ANSWER \# 4 : 9 ANSWER * $5: 1 \varnothing$

Here's a good opportunity to practice writing multiple statements per line. Our sample runs above were produced using these two sets of data.

```
910 DATA 2
92ø DATA 1,1,2,2,2,1,1,2,2,2,1,1,1,2
930 DATA 1,2,1,1,2,2,1,1,1,2,1,2,2,2
94\varnothing DATA 1,1,2,1,-1
91\varnothing DATA 5
92ø DATA 4,3,4,2,4,1,1,5,5,3,5,4,5,1
93@ DATA 3,2,5,5,4,4,5,1,2,3,3,3,5,2
94\varnothing DATA 2,3,1,5,4,1,1,1,2,3,1,4,1,5
95』 UATA 1,2,3,4,1,-1
```

Write your program below. (You need not show the DATA statements.)

```
- - - - - - - - - - 
1\varnothing\varnothing REM***VOTE COUNTING PROGRAM
11\varnothing REM***INITIALIZE
12\varnothing DIM C(2\emptyset) : READ N : FOR K=1 TO N:C(K)=\varnothing : NEXT K
2\emptyset\varnothing REM***READ AND COUNT VOTES
21\varnothing READ V : IF V <> -1 THEN LET C (V)=C(V)+1 : GOTO 21\varnothing
3\varnothing\varnothing REM***PRINT RESULTS
31\varnothing FOR K=1 TO N : PRINT "ANSWER #"; K; ":"; C(K) : NEXT K
```

35. The problems in frames $25-34$ dealt with counting votes. Each time through the loop that reads data (a data loop) you added one (1) to an array element $(\operatorname{LET~C}(\mathrm{V})=\mathrm{C}(\mathrm{V})+1)$. Almost any vote counting application you might want to try is going to be similar to the solutions in frame 34 . Now you can volunteer to be the official ballot counter for all the elections in your community-PTA, computer club, school class offices, chiurch groups, ad infinitum.

On to more serious business. A similar, but not identical application of simple one-dimension arrays deals with counting things or money, instead of votes.

Let's set the stage. You are the sponsor for the neighborhood computer club for eight local kids. The kids want to buy a new superduper color graphics terminal for the neighborhood computer system. It's only $\$ 1200$ in kit form. Raising funds is the problem. The kids agree to sell milk chocolate candy bars for $\$ 1.00$ each to raise money. (The club makes $55 \mathbb{C}$ profit per sale, not bad!). But you must do the recordkeeping. You assign each kid a number. Whenever a kid comes by for candy bars, you identify the kid, by number, and note how many bars were taken. The money will be turned in later.

Here are the ID numbers assigned to each club member.

1. Jerry
2. Karl
3. Bobby
4. Mimi
5. Mary
6. Doug
7. Danny
8. Scott

When Danny first takes 6 bars you note it as 4,6. The 4 is Danny's ID number for the computer, and 6 is the number of candy bars he took. When

Doug takes 12 bars, your note is $\qquad$
$\qquad$ . When Mary takes 6, the note is $\qquad$ -.

7,12; 3,6
36. After a few weeks of this, you've accumulated quite a pile of notes. It's time to tally and see how much money you've raised thus far. The information from your notes will be placed into DATA statements. (You could enter the information using INPUT, but it could take much too long!) Start at line 910 (a good place to put DATA assuming the rest of the program won't have line numbers past 900.)

```
9ø\emptyset REM ** DATA IN PAIRS: KID ID NO.
9@1 REM ** FOLLOWED BY QUANTITY
91\varnothing DATA 4,6,7,12,3,6,1,8,4,5,5,3,8,2\varnothing
```

This shows that Danny took another five candy bars.

```
920 2,4,3,8,6,6,5,10,7,12,8,4,1,3
Mary took another 8.
936 DATA -1,-1
```

(a) Each item of data has (how many?) $\qquad$ numbers.
(b) DATA 6,6 means $\qquad$ -.
(c) The end-of-data flag has (how many?) $\qquad$ numbers. Why? $\qquad$
(a) two
(b) Mimi took 6 bars
(c) Two. Each data element has two numbers. Two values will be read with one READ statement. An ERROR would result if there were only one (flag) value for the two variables in the READ statement.
37. Just as you complete entering the DATA, Bobby shows up to take another six bars. Show how you could add this data without changing any of the existing DATA statements. Use the highest line number permissible and still have the end-of-data flags as the last values read by the program.

```
- - - - - - - - 
929 DATA2,6
```

The line number cannot be larger than 929 , or the flags in line 930 will not be the last data item read by the program. Moral: Be careful where you add DATA into an existing program.
38. We need an array with eight elements. That means we need a subscripted variable with subscripts from 1 to 8 , to represent the eight members of the club. The value added to each element (or subscripted variable) in the array will be the number of candy bars each kid took. But first, initialize the array by writing one multiple-statement line that will dimension the array and assign a zero to each element. We will call this the A array and use $\mathrm{A}(\mathrm{X})$ for the subscripted variable.

```
1ø\emptyset REM***CANDY BAR COUNTER
11ø REM*** INITIALIZE
12ø DIM
```

-     -         -             -                 -                     -                         -                             -                                 -                                     - 

$12 \varnothing$ DIMA(8): FOR $X=1$ TO 8 : LET $A(X)=\varnothing$ : NEXT $X$ YOU could omit the LET.
39. Now let's read the data in pairs (two items at a time). Use K for kid and Q for quantity of candy bars, and test for end of DATA, all on one line. If we run out of data, have the program branch to line 310.

```
200 REM***READ DATA AND TALLY
```

210 $\qquad$

```
21\varnothing READ K,Q : IF K=-1 THEN 31\varnothing
```

40. Now the hard one! We must accumulate the number of bars in the correct array element corresponding to the kid who took them. Think of the subscript K in the subscripted variable $\mathrm{A}(\mathrm{K})$ as the kid's ID code.


If K (for kid) is 2 and Q (quantity) is 4, then line 220 will cause array element $\mathrm{A}\left(\_\right.$_ ) to increase by $\qquad$ .

## $A(2): 4$

41. If the array elements look like those on the left before, how will they look after reading and adding the additional DATA given here?

| $\mathrm{A}(1)=$ | 8 | $A(1)=$ |
| :---: | :---: | :---: |
| (2) $=$ | 4 | (2) $=$ |
| (3) $=$ | 6 | (3) $=$ |
| $(4)=$ | 4 | (4) $=$ |
| $(5)=$ | 3 | $(5)=$ |
| $(6)=$ | 2 | $(6)=$ |
| $(7)=$ | 12 | (7) $=$ |
| $(8)=$ | 7 | $(8)=$ |
|  | Befo |  |


| $\mathrm{A}(1)=$ | 8 |
| :---: | :---: |
| (2) $=$ | 4 |
| (3) $=$ | 14 |
| (4) $=$ | 13 |
| (5) $=$ | 3 |
| (6) $=$ | 8 |
| (7) $=$ | 14 |
| (8) $=$ | 7 |

42. Here's our program so far.
```
1\varnothing\varnothing REM ** CANDY BAR COUNTER
11\varnothing REM ** INITIALIZE
120 DIM A(8)
13\varnothing FOR X=1 TO 8:A(X)=\varnothing: NEXT X
2\varnothing\varnothing REM ** READ DATA AND TALLY
21ø READ K,Q : IF K=-1 THEN 31\varnothing
220 LET A(K)=A(K)+Q:GOTO 21ø
9\varnothing\varnothing REM ** DATA IN PAIRS: KID ID NO.
9ø1 REM ** FOLLOWED BY QUANTITY
91ø DATA 4,6,7,12,3,6,1,8,4,5,5,3,8,2\varnothing
92\emptyset DATA 2,4,3,8,6,6,5,1\varnothing,7,12,8,4,1,3
929 DATA 1,6
930 DATA -1,-1
```

It starts and it accumulates. Before it stops, we must have it print our report. Let's start the report with a heading.

```
3@\varnothing REM ** PRINT THE REPORT
31\varnothing PRINT "KID ID *", "QUANTITY"
```

Now we print the results using a FOR-NEXT loop.

```
32ø FOR X=1 TO 8
33\varnothing PRINT X, A(X)
34@ NEXT X
Or
32ø FOR }X=1\mathrm{ TO 8:PRINT }X,A(X):NEXT 
```

Using the data in the DATA statement, show below how the report will look after running our program.

| RUN |  |  |
| :--- | :--- | :--- | :--- |
| KID | ID $\#$ | QUANTITY |
| 1 |  | 17 |
| 2 |  | 4 |
| 3 |  | 14 |
| 4 |  | 11 |
| 5 |  | 13 |
| 6 |  | 6 |
| 7 |  | 24 |
| 8 |  | 24 |
| READY |  |  |

43. So far our report shows us who has what but doesn't give us names or totals or profits. With some help, the computer can do all those things.

Let's start with the total. In BASIC each array has an element we haven't used yet. It's the zero (0) element. Remember, when you DIMension an array of eight elements with a DIM statement, DIM A(8), you really get 9: $0,1,2,3,4,5$, 6,7 , and 8 .

Since we haven't assigned any kid the ID number 0 (zero), the "A array" element with the subscript 0 has not been used or assigned a value. So the $\mathrm{A}(0)$ element can be used for accumulating totals, although we could use some other variable. Look at statement 410, which accumulates the total number of bars sold in $A(0)$.

```
4\varnothing\varnothing REM ** TALLY TOTAL SALES & PROFIT
41\varnothing FOR X=1 TO 8:A(\varnothing)=A(\varnothing)+A(X):NEXT X
```

If the $A$ array starts at zero, we must remember to change the FOR statement in the initializing routine to start assigning zeros at $\mathrm{A}(0)$. Replace (rewrite) the initializing line for this program so that all the array elements are given the initial value of zero.

```
13\varnothing FOR K=\varnothing TO 8 : A(X)=\varnothing : NEXT X
```

44. The statement that tallies up all the candy sold by the club uses the $A(0)$ element in the A array to accumulate the value stored in $A(1)$ through $A(8)$. If the array looks as it did in frame 41 (after reading data), then what value will be stored in $\mathbf{A}(0)$ after one time through the loop in line 410 ? $\qquad$ After three times through the loop in 410 ? $\qquad$
45. Write lines 420 and 430 to print the total and the profit ( 55 c on each bar). Here is what we want line 420 to print:
```
TOTAL IS 113
PROFIT IS 62.15
420
430
```

```
42\emptyset PRINT "TOTAL IS ";A(\varnothing)
```

42\emptyset PRINT "TOTAL IS ";A(\varnothing)
43ø PRINT "PROFIT IS ";A(\varnothing)*\varnothing.55

```
43ø PRINT "PROFIT IS ";A(\varnothing)*\varnothing.55
```

46. Here is a complete list and run so far.
```
1\varnothing% REM ** CANDY BAR COUNTER
11\varnothing REM ** INITIALIZE
12\varnothing DIM A(8)
13\varnothing FOR X=\varnothing TO 8:A(X)=\varnothing:NEXT }
2ø\varnothing REM ** READ DATA & TALLY
21\varnothing READ K,Q:IF K=-1 THEN 31\varnothing
215 IF K=-1 THEN 31\varnothing
22\varnothing A(K)=A(K)+Q:GOTO 21\varnothing
3\varnothing\varnothing REM ** PRINT THE REPORT
31\varnothing PRINT "KID ID *","QUANTITY"
32\varnothing FOR X=1 TO 8:PRINT X,A(X):NEXT X
4\varnothing\varnothing REM ** TALLY TOTAL SALES & PROFIT
41\varnothing FOR X=1 TO 8:A(\varnothing)=A(\varnothing)+A(X):NEXT X
42\varnothing PRINT "TOTAL IS ";A(\varnothing)
43\emptyset PRINT "PROFIT IS ";A(\varnothing)*ø.55
9øø REM ** DATA IN PAIRS: KID ID NO.
9ø1 REM ** FOLLOWED BY QUANTITY
91\varnothing DATA 4,6,7,12,3,6,1,8,4,5,5,3,8,2\varnothing
92ø DATA 2,4,3,8,6,6,5,1\varnothing,7,12,8,4,1,3
9 2 9 ~ D A T A ~ 1 , 6
930 DATA -1,-1
RUN
KID ID # QUANTITY
        17
2 4
3 14
4 11
5 13
6 6
7 24
8 24
TOTAL IS 113
PROFIT IS 62.15
```

That's a nice report . . . but wait! In this day of impersonalization, wouldn't it be nice to print each kid's name instead of a number? How can we do it? Easily. We can have the computer READ the names from DATA statements.

String variables must be DIMensioned, just as an array must be DIMensioned. Just don't forget the properly placed \$ that identifies a string variable. You may prefer to DIMension each array in the same multiple-statement line where the array is first used or initialized.

Write a DIM statement to initialize $\mathrm{N} \$(\mathrm{X})$ for a string long enough to use for the longest name of any member of the computer club.

140


140 DIM $N \$(8)$ (Number in parentheses must be at least 5.)
47. Let's say that we have placed the club members' names in a DATA statement, in the same order as their ID numbers.

DATA JERRY, BOBBY, MARY, DANNY, KARL, MIMI, DOUG, SCOTT
(Note that on your video screen this line will "wrap around" to the next line. The computer doesn't care and will consider names or numbers that are "split" between the end of one display line and the beginning of the next as unbroken.)

Since our BASIC does not allow arrays of strings, only numeric arrays, we must tell the computer to READ and PRINT each name at the time that it is printing the report. Therefore, the statement that reads the names from the data statement must be inside the FOR-NEXT loop that prints the report (lines 320 and 340).

```
3ø\varnothing REM***PRINT THE REPORT
31\varnothing PRINT
32\varnothing PRINT "NAME", "QUANTITY'":PRINT
330 FOR }X=1\mathrm{ TO 8: READ N$
34\varnothing PRINT N$,A(X):NEXT X
```

Notice that no "end of data" flag is needed since the FOR-NEXT loop only goes around 8 times, and there are 8 names in the DATA statement.

There is now the touchy problem of where to place the DATA statement that contains the club members' names. Keep in mind that we want to avoid an error message just because a READ statement with a numeric variable came upon a DATA statement containing strings!

Where should the DATA statement with club members names be placed in the program? $\qquad$


At the end, since all numeric data is read earlier in the program.
48. Now here is the real test of your understanding. Ready to play computer? Show what a RUN of this program would look like.

```
1\varnothing\varnothing REM ** CANDY BAR COUNTER
11\varnothing REM ** INITIALIZE
12\emptyset DIM A(8)
13@ FOR Z=\varnothing TO B:A(X)=\varnothing:NEXT X
14\varnothing DIM N$(8)
2ø\emptyset REM ** READ DATA & TALLY
21\varnothing READ K,Q:IF K=-1 THEN 31ø
215 IF K=-1 THEN 31ø
22\varnothing A(K)=A(K)+Q:GOTO 21\varnothing
3ø\varnothing REM ** PRINT THE REPORT
31\varnothing PRINT
32\varnothing PRINT "NAME","QUANTITY"
330 FOR X=1 TO 8:READ N$
34\varnothing PRINT N$,A(X):NEXT X
4\varnothingD REM ** TALLY TOTAL SALES & PROFIT
41\varnothing FOR X=1 TO 8:A(\varnothing)=A(\varnothing)+A(X):NEXT X
42\varnothing PRINT "TOTAL IS ";A(\varnothing)
43\varnothing PRINT "PROFIT IS ";A(\varnothing)*\varnothing.55
9\varnothing\varnothing REM ** DATA IN PAIRS: KID ID NO.
901 REM ** FOLLOWED BY QUANTITY
91g DATA 4,6,7,12,3,6,1,8,4,5,5,3,8,2\varnothing
92ø DATA 2,4,3,8,6,6,5,1\varnothing,7,12,8,4,1,3
929 DATA 1,6
930 DATA -1,-1
94ø DATA JERRY, BOBBY, MARY, DANNY,KARL,MIM
I ,DOUG,SCOTT
```

RUN

| NAME | QUANTITY |
| :--- | :--- |
| JERRY | 17 |
| BOBBY | 4 |
| MARY | 14 |
| DANNY | 11 |
| KARL | 13 |
| MIMI | 6 |
| DOUG | 24 |
| SCOTT | 24 |
| TOTAL IS | 113 |
| PROFIT IS | 62.15 |

49. Let's look at one other application of singly-subscripted variables. This one neither counts votes nor accumulates anything.

No doubt you've read about computer dating. Ever wonder how it works? You answer a series of questions that are then stored in the computer; other people who wish to be matched do likewise. Then the responses are compared to test for "compatibility." Let's do a simplified version of a computer dating program which you can alter for your own uses.

We'll use a multiple-choice questionnaire with only five questions. (Ask anything you'd like!) Responses will be stored in DATA statements, with the name first, and the five responses following. My responses appear in line 910 on the next page.

```
9øø REM ** QUESTIDNAIRE RESPONSES
9ø1 REM ** NAME FOLLOWED BY ANSWERS
9ø2 REM ** 'HIS' IN LINE 910
91ø DATA LEROY,3,3,4,2,1
```

Now, you create DATA statements in lines 920-970 for these respondents, plus an end-of-data flag.

|  | Q1 | Q2 | Q3 | Q4 | Q5 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| JOAN | 1 | 4 | 2 | 2 | 1 |
| TONI | 2 | 2 | 2 | 3 | 3 |
| LAURA | 2 | 3 | 3 | 1 | 2 |
| MARY | 3 | 3 | 4 | 2 | 1 |
| IRENE | 3 | 1 | 4 | 2 | 1 |

```
920
930
94\varnothing
950__
960
97\varnothing DATA END
- - - - - - - - 
92ø DATA JOAN,1,4,2,2,1
93ø DATA TONI,2,2,2,3,3
940 DATA LAURA,2,3,3,1,2
950 DATA MARY,3,3,4,2,1
960 DATA IRENE,3,1,4,2,1
970 DATA END
```

50. Now, you write the rest of the program with some gentle supervision. First, you will need a DIM statement that will allow the program to compare "his" responses (stored in array C), with "her" responses (stored in array A). Also initialize string variable N\$ for "his" and H\$ for "her."
```
10\varnothing REM***COMPUTER DATING SIMULATION
1\varnothing5 REM***INITIALIZE
```

118
$\qquad$
$\rightarrow+\square^{-}$
$11 \varnothing$ DIMC(5),A(5),N\$(1ø),H\$(1ø)

Note: You can DIMension more than one array in one DIM statement.
51. Next, READ the first data statement which contains 'his" name, and READ "his" five responses. The responses should be read into array $C$ using the method shown in frames 8 and 18.

Then print "his" name and responses all on one line, so that later you can compare them with "hers."

```
2øø REM**'HIS' NAME & RESPONSES
```

```
- - - - - - - - -
21\varnothing READ N$
22ø FOR X=1 TO 5:READ C:C(X)=C:NEXT X
230 PRINT N$,
24ø FOR X=1 TO 5:PRINT C(X);" "; :NEXT X:
PRINT
Did you remember this PRINT statement? It returns the cursor to the beginning of the next line.
```

Note: You may have used more or less line numbers, but the statements must perform as indicated, probably the same order.
52. Next, READ one set of "her" names and responses into array A, and print "her" responses so you can visually compare the "his" responses with "her" responses. After you read "her'" name in line 310, check to see if it is the end-of-data flag (the word END). Use the string comparison IF H\$ = "END" THEN END. The output we want so far should look like this.

| RUN |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| LEROY | 3 | 3 | 4 | 2 | 1 |
| JOAN | 1 | 4 | 2 | 2 | 1 |

Complete the program segment to produce this output or printout.

```
3ø\varnothing REM ** 'HER' NAMES & RESPONSES
31\varnothing
320
33ø
```

$\qquad$

```
34%
```

```
31\varnothing READ H$:IF H$= "END" THEN END
32ø FOR X=1 TO 5:READ A:A (X)=A:NEXT X
330 PRINT H$,
34ø FOR X=1 TO 5:PRINT A(X);" "; :NEXT X:
PRINT
```

53. Now comes the crucial part. This is where you compare the contents of array $C$ with the contents of array $A$ and add the number of matches into variable M. Think about that and complete the program below, so that a RUN of the complete program looks like the one here.
```
RUN
LEROY 3
JOAN 1
    2 MATCHES
TONI 2 2 2 3 3
    | MATCHES
LAURA 2
    1 MATCHES
MARY }\begin{array}{llllll}{3}&{3}&{4}&{2}&{1}
    5 \text { MATCHES}
IRENE }\quad\begin{array}{llllll}{3}&{1}&{4}&{2}&{1}
    4 MATCHES
4\emptyset\emptyset REM ** COMPARE & COUNT 'MATCHES'
41\varnothing M=\varnothing
420 FOR X=1 TO 5
430 IF ___ THEN 450 ఒ Compare
440 LET M= _ _ Add matches
4 5 0 ~ ఒ ~ < ~ C l o s e ~ t h e ~ l o o p ~ t o ~ c o m p a r e ~ a n o t h e r ~
460 PRINT "MATCHES"
47@ PRINT
48\varnothing кото ___ Read another set of responses
410}M=
420 FOR }X=1\mathrm{ TO }
43\varnothing IF C(X)<>A(X) THEN 450
44\varnothing M=M+1
450 NEXT }
46\varnothing PRINT M; " MATCHES"'
47% PRINT
48ø GOTO 31ø
```

Following is a complete listing and RUN of our computer dating program.

```
1ø\varnothing REM ** COMPUTER DATING SIMULATION
105 REM ** INITIALIZE
11\varnothing DIM C(5),A(5),N$(1\varnothing),H$(1\varnothing)
2øø REM ** 'HIS' NAME & RESPONSES
21\varnothing READ N$
22ø FOR X=1 TO 5:READ C:C(X)=C:NEXT X
23\varnothing PRINT N$,
24\varnothing FOR X=1 TO 5:PRINT C(X);" ";:NEXT X:
PRINT
3ø\varnothing REM ** 'HER' NAMES & RESPONSES
31\varnothing READ HS:IF H$="END" THEN END
32ø FOR X=1 TO 5:READ A:A(X)=A:NEXT X
33\varnothing PRINT H$,
34@ FOR X=1 TO 5:PRINT A(X);" ";:NEXT X:
PRINT
4ø\varnothing REM ** COMPARE & COUNT 'MATCHES'
41\varnothing M=\varnothing
42\varnothing FOR X=1 TO 5
430 IF C }(x)<>A(X) THEN 45\emptyset
440 M=M+1
4 5 0 ~ N E X T ~ X ~
460 PRINT M;" MATCHES"
47\varnothing PRINT
48\varnothing GOTO 31\varnothing
9øø REM ** QUESTIONAIRE RESPONSES
9ø1 REM ** NAME FOLLOWED BY ANSWERS
9ø2 REM ** 'HIS' IN LINE 91\varnothing
910 DATA LEROY,3,3,4,2,1
92\emptyset DATA JOAN,1,4,2,2,1
930 DATA TONI,2,2,2,3,3
940 DATA LAURA, 2,3,3,1,2
950 DATA MARY, 3,3,4,2,1
960 DATA IRENE,3,1,4,2,1
970 DATA END
RUN
LEROY 3
JOAN 1 4 2 2 1
2 MATCHES
TONI 22 2 3 3
\varnothing MATCHES
LAURA 2 3 3 1 2
1 MATCHES
MARY 3 3 4 2 1
5 ~ M A T C H E S
IRENE 3 1 4 2 1
4 \text { MATCHES}
```


## SELF-TEST

If you can complete the Self-Test on subscripted variables, you will be ready for the next chapter, which will expand your programming ability to include the use of more complex subscripted variables. Therefore, it is important that you have the information in this chapter well in hand.

1. Indicate which of the following are legal BASIC subscripted variables.
$\qquad$ (a) X
(b) X 2
(c) $\mathrm{X}(2)$
$\qquad$ (d) $2(\mathrm{X})$
(e) $\mathrm{XX}(2)$
(f) $\mathrm{X}(\mathrm{K})$
$\qquad$ (g) $X_{2}$
(h) $\mathrm{X}(\mathrm{I}-\mathrm{J})$
2. Assume that values have been assigned to variables as shown below. Note that both simple and subscripted variables are shown.


Remember, A, A1, and A(1) are distinct variables. Write the value of each variable below.
(a) $\mathrm{A}(\mathrm{Q})$ $\qquad$
(b) $\mathrm{A}(\mathrm{A})$
(c) $\mathrm{A}(\mathrm{A} 1)$ $\qquad$
(d) $\mathrm{A}(\mathrm{A}(2))$ $\qquad$
(e) $\mathrm{A}(\mathrm{A}(\mathrm{Q}))$ $\qquad$
(f) $\mathrm{A}(\mathrm{A}-\mathrm{Q})$ $\qquad$
(g) $\mathrm{A}(\mathrm{A}+\mathrm{A} 1)$ $\qquad$
(h) $\mathrm{A}\left(2^{*} \mathrm{Q}\right)$ $\qquad$
3. What will be printed if we RUN the following program?

```
1\varnothing\varnothing REM ** MYSTERY PROGRAM
11\varnothing DIM X(1\varnothing)
120 READ N
13\varnothing FOR K=1 TO N
140 READ X: X(K)=X
150 NEXT K
160 FOR K=1 TO N
17\varnothing IF }X(K)<\varnothing\mathrm{ THEN 19ø
18\emptyset PRINT X(K);" ";
190 NEXT K
90\varnothing REM ** VALUES OF N AND X ARRAY
91\varnothing DATA'7
92ø DATA 23,-44,37,\varnothing,-12,-58,87
```

4. In the preceding program of question 3 , what is the largest value of N for which the program can be used? $\qquad$ What would happen if we tried to RUN the program using the following DATA?
```
91\varnothing DATA 12
92ø DATA 3,6,-2,ø,9,\varnothing,7,3,-5,4,-1,7
```

5. Modify the vote-counting program of frame 27 so that the total votes (for both candidates) are also printed. The printout might look like this.
```
RUN
SAM SMOOTHE: 19
GABBY GRUFF: 16
TOTAL VOTES: 35
```

6. Modify the vote-counting program of frame 27 so that the printout is $\%$ of total votes, rounded to the nearest whole number $\%$.

RUN
SAM SMOOTHE: 54\%
GABBY GRUFF: 46\%
7. You are selected chairman of the United Collection in your neighborhood. You have 5 people who collect money door-to-door and turn in the money to you at the end of each day. You record their names and dollar amounts collected on a form. This data is then entered into your computer for further processing. Write a BASIC program that will accumulate the current amount each person has collected and the total amount collected by all 5 people. Your report should show the names of each collector with the amounts collected.

```
RUN
NAME AMOUNT COLLECTED
FRED 125
JOANN 205
MARYJO 1.0
JERRY 1\varnothing\varnothing
BOB 2ø\varnothing
TOTAL 73\varnothing
```

8. Your computer club kids decide they want to find out who is the best programmer in their group. As club sponsor, you decide to give them a multiple choice test on the programming concepts and correct the test using the computer. The multiple choice answers will be the numbers $1,2,3,4$, or 5 . There are 10 questions on the test. You enter the 10 correct answers in the first DATA statements in the program. These are read into array K. In subsequent DATA statements, you first enter the name of the club member, followed by the 10 answers that person gave for the test. (Enter in array R.) Your task is to write a BASIC program that will correct the tests and print a report that looks similar to the one below.

| RUN |  |
| :--- | :---: |
| NAME | SCORE |
| DANNY | 5 |
| KARL | 5 |
| MIRIAM | 4 |
| SCOTT | 7 |

9. Are you curious about your chances of winning at any game using dice? If you developed a program to simulate the rolling of one die and counted how many times each side appeared, you would get a better idea of your chances of winning.

Write a BASIC program to simulate the roll of one die, 1000 times (or make that an input variable). After each simulated roll, accumulate or add to the correct array element one appearance or "vote." After 1000 rolls, print the contents of your array in report form showing how many times each die side appeared during the computer simulation. Your report should look like the one below. There is room to write your program on the next page.

```
RUN
HOW MANY SIMULATED ROLLS? 1øø\varnothing
DICE ROLL NO. OF OCCURENCES
    1 159
    2 152
    3 173
    4 142
    5 189
    6 185
```


## Answers to Self-Test

The frame numbers in parentheses refer to the frames in the chapter where the topic is discussed. You may wish to refer back to these for quick review.

1. (c), (f), and (h) are legal subscripted variables. Longer variable names such as item (e) may be legal on your computer. Check the reference manual for your computer. (frame 1)
2. (a) 4
(b) 23
(c) 37
(d) $19 \quad \mathrm{~A}(\mathrm{~A}(2))=\mathrm{A}(4)=19$
(e) $19 \quad \mathrm{~A}(\mathrm{~A}(\mathrm{Q}))=\mathrm{A}(\mathrm{A}(2))=\mathrm{A}(4)=19$
(f) $37 \mathrm{~A}(3-2)=\mathrm{A}(1)=37$
(g) $19 \mathrm{~A}(3+1)=\mathrm{A}(4)=19$
(h) $19 \quad \mathrm{~A}(2+2)=\mathrm{A}(4)=19$
(frame 4)
3. RUN
$23 \quad 37$ ø 87
(frames 7-8)
4. 10

The computer would print an error message.
(frames 11-12)
5. Add the following statements.

```
330 PRINT
34\varnothing PRINT "TOTAL VOTES:";C(1)+C(2)
```

(frames 43-46)
6. Beginning at line 310 , make these changes.

```
31\varnothing LET T=C(1)+C(2)
32ø LET S=INT(100*C(1)/T + .5)
33\varnothing LET G=INT(1\varnothing\mp@subsup{|}{}{*}C(2)/T + .5)
34\varnothing PRINT "SAM SMOOTHE:";S;"%"
35ø PRINT "GABBY GRUFF:";G;"%"
```

(frame 27 and Chapter 4)
7. $1 \varnothing$ REM

15 REM
$2 \varnothing$ DIM NS (1ø),T(5):G=ø:FOR $X=1$ TO 5:T(
$X)=\varnothing$ : NEXT $X$
25 REM
$3 \varnothing$ READ $P, D: I F P=-1$ THEN 6ø
$4 \varnothing T(P)=T(P)+D: G=G+D: G O T O \quad 3 \varnothing$
50 REM
$6 \varnothing$ PRINT "NAME","AMOUNT COLLECTED"
$7 \varnothing$ FOR $P=1$ TO 5:READ N\$:PRINT N\$,T(P):
NEXT P
$8 \varnothing$ PRINT "TOTAL:", G
$9 \varnothing \varnothing$ REM
$91 \varnothing$ DATA $2,45,1,75,3,25,4,10 \varnothing, 3,25$
$92 \varnothing$ DATA $5,125,3,5 \varnothing, 1,5 \varnothing, 2,12 \varnothing, 2,4 \varnothing$
930 DATA 5,75,-1,-1
940 DATA FRED, JOANN, MARYJO, JERRY, BOB
RUN
NAME
FRED
JOANN
MARYJO
JERRY
BOB
AMOUNT COLLECTED
125
205
205
108
100
tOTAL
200

READY
(frame 35-53)
8. $1 \varnothing$ REM
2. REM
$3 \varnothing$ DIMK(1ø),R(1ø),N\$(1ø)
40 REM
$5 \emptyset$ PRINT "NAME","SCORE" : PRINT
60 REM
$7 \varnothing$ FOR $X=1$ TO $1 \varnothing$
$8 \emptyset$ READ $K: K(X)=K$
$9 \varnothing$ NEXT K
$1 \varnothing \varnothing$ REM
$11 \varnothing$ READ N\$ : IF N\$="END" THEN END
$12 \varnothing$ FOR $X=1$ TO $1 \varnothing$
$13 \varnothing$ READ $R: R(X)=R$ : NEXT $X$
$14 \varnothing S=\varnothing$
$15 \varnothing$ REM
$16 \varnothing$ FOR $x=1$ TO $1 \varnothing$
$17 \varnothing$ IF $K(x)<>R(x)$ THEN $19 \varnothing$
18 @ $\mathrm{S}=\mathrm{S}+1$
$19 \varnothing$ NEXT
$2 \varnothing \varnothing$ PRINT N\$,S: GOTO $11 \varnothing$
$9 \varnothing \varnothing$ REM
910 DATA $3,4,3,3,5,1,2,3,2,1$
920 REM
930 DATA DANNY, 1, 2, 3, 4, 5, 1, 2, 3, 4,5
940 DATA KARL, 1, 3, 2, 4, 1, 2, 3, 2, 1
950 DATA MIRIAM,3,2,2,1,4,1,2,3,1,2
960 DATA SCOTT, 1, 2, 3, 3,5,1,2,3,2,2
$97 \varnothing$ DATA END

RUN
NAME SCORE
DANNY 5
KARL
MIRIAM 4
SCOTT 7
(frame 49-53)
9. $1 \varnothing$ REM
$2 \varnothing$ DIM D(6)
$3 \varnothing$ FOR $X=1$ TO 6 : $D(X)=\varnothing$ : NEXT $X$
$4 \varnothing$ PRINT "HOW MANY SIMULATED ROLLS";
50 INPUT R
$6 \varnothing$ FOR $X=1$ TO R
$7 \varnothing N=\operatorname{INT}\left(6^{*} \operatorname{RND}(1)\right)+1: D(N)=D(N)+1$
$8 \varnothing$ NEXT $X$
$9 \varnothing$ PRINT "SPOTS","* OF OCCURENCES"
180 REM
$11 \varnothing$ FOR $X=1$ TO 6
$12 \varnothing$ PRINT $X, D(X)$
130 NEXT $X$

## RUN

HOW MANY SIMULATED ROLLS? $1 \varnothing \varnothing \varnothing$
SPOTS \# OF OCCURENCES
$\begin{array}{ll}1 & 168 \\ 2 & 144\end{array}$
2144
$3 \quad 172$
$\begin{array}{ll}4 & 182 \\ 5 & 159\end{array}$
159
175
(frames 25-31)

## CHAPTER EIGHT

## Double Subscripts

In Chapter 7 you were introduced to singly-subscripted variables and their many applications. There are no new statements in this chapter, just some new uses and variations of what you already know.

In this chapter we'll extend your use of ATARI BASIC to variables with two subscripts, which we call doubly-subscripted variables. Doubly-subscripted variables are used with arrays of numbers which might require several columns and rows, such as in complex voter analysis problems, detailed dollar analysis problems, and a whole host of board game applications. When you complete this chapter, you will be able to:

- use variables with two subscripts;
- assign values to doubly-subscripted variables in a two-dimensional array (also called a table or matrix);
- use the DIM statement to tell the computer the dimensions of two-dimensional arrays.

1. In Chapter 7, we described subscripted variables such as $X(7)$ and $T(K)$. These are singly-subscripted variables. That is, each variable has exactly one subscript.


In this chapter, we will use doubly-subscripted variables, variables that have two subscripts.

> T(2,3) Two subscripts, separated by a comma
$\mathrm{T}(3)$ is a subscripted variable with how many subscripts? $\qquad$
$\mathrm{T}(7,5)$ is a subscripted variable with how many subscripts? $\qquad$

-     -         -             -                 -                     -                         -                             -                                 -                                     - 

1; 2
2. It is convenient to think of doubly-subscripted variables arranged in an array of rows and columns, as shown below.

Column $1 \quad$ Column $2 \quad$ Column $3 \quad$ Column 4

Row 1


Row 2


Row 3 $\square$
$\square$
$\square$ $A(3,4) \square$

The above array has $\qquad$ rows and $\qquad$ columns.

3; 4
3. With the arrangement shown in frame 2, we can relate subscripts to particular places (locations, or 'boxes'' for values) in rows and columns. These are called the elements in the array. For example:


Column
$\mathbf{A}(1,1)$ is in row 1 , column $1 . \mathbf{A}(1,2)$ is in row 1 , column 2 . What subscripted variable is in row 3 , column 2 ? $\qquad$

-     -         -             -                 -                     -                         -                             - 

A(3,2)
4. The rectangular arrangement of doubly-subscripted variables shown in frame 2 is called a table, matrix, or two-dimensional array.

In Chapter 7 we described arrays of singly-subscripted variables which are also called lists, vectors, or one-dimensional arrays.

| This is a list: | $\mathrm{X}(1)$ | $\mathrm{X}(2)$ | $\mathrm{X}(3)$ |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
| This is a table: | $\mathrm{C}(1,1)$ | $\mathrm{C}(1,2)$ | $\mathrm{C}(1,3)$ |
|  | $\mathrm{C}(2,1)$ | $\mathrm{C}(2,2)$ | $\mathrm{C}(2,3)$ |
|  | $\mathrm{C}(3,1)$ | $\mathrm{C}(3,2)$ | $\mathrm{C}(3,3)$ |

(a) A list is also called a $\qquad$ or a $\qquad$
(b) A table is also called a $\qquad$ or a $\qquad$ .
(a) vector, one-dimensional array (one subscript)
(b) matrix, two-dimensional array (two subscripts)
5. A doubly-subscripted variable is simply the name of a location in the computer. As with any other variable, you can think of it as the name for a box, a place to store a number. Here is a table of doubly-subscripted variables.


Pretend you are the computer and assign the value of 73 to variable $B(2,1)$. In other words, take pencil in hand and write the number 73 in the box labeled $B(2,1)$. Then do the same for the following.

```
\(\operatorname{LET} B(1,3)=\varnothing\)
LET \(B(1,1)=49\)
\(\operatorname{LET} B(2,3)=B(2,1)-B(1,1)\)
LET \(B(1,2)=2^{*} B(2,1)\)
\(\operatorname{LET} B(2,2)=\operatorname{INT}(B(2,1) / B(2,3))\)
```


6. As we learned in Chapter 7, subscripts can be variables. The subscripted variable $P(R, C)$ has variable subscripts.

If $\mathrm{R}=1$ and $\mathrm{C}=2$, then $\mathrm{P}(\mathrm{R}, \mathrm{C})$ is $\mathrm{P}(1,2)$.
If $R=4$ and $C=3$, then $P(R, C)$ is $P(4,3)$.
If $R=7$ and $C=5$, then $P(R, C)$ is $\qquad$ -.

-     -         -             -                 -                     -                         -                             - 

$P(7,5)$
7. Let's assume that the following values (in the boxes) have been assigned to the corresponding variables. Note that there are both simple and subscripted variables.

$T(1,1)$

B


Write the value of each variable below, and the value of subscripts.

| $\mathrm{T}(2,3)=$ | $\mathrm{T}(1,1)=$ |
| :--- | :--- |
| $\mathrm{R}=$ | $\mathrm{A}=$ |
| $\mathrm{C}=\square$ | $\mathrm{T}(\mathrm{A}, \mathrm{A})=$ |
| $\mathrm{T}(\mathrm{R}, \mathrm{C})=\square$ | $\mathrm{T}(\mathrm{B}, \mathrm{R})=$ |
| $\mathrm{T}(\mathrm{A}, \mathrm{B})=\square$ | $\mathrm{T}(\mathrm{R}, \mathrm{A})=$ |
|  | $\mathrm{T}(\mathrm{R}+1, \mathrm{C}-2)=$ |

$8 \quad 7$
21
37
85
$0 \quad 9$

$$
16 \mathrm{~T}(\mathrm{R}+1, \mathrm{C}-2)=\mathrm{T}(2+1,3-2)=\mathrm{T}(3,1)
$$

8. Election time again. (Before starting on this, you may wish to review the vote-counting application in Chapter 7.) The questionnaire below requires two answers.

Q1. Who will you vote for in the coming election? Circle the number to the left of your choice.

1. Sam Smoothe
2. Gabby Gruff
3. No opinion

Q2. What age group are you in? Circle the number to the left of your age group.

1. Under 30
2. 30 or over

Since there are two questions, each reply consists of two numbers: the answer to question 1 and the answer to question 2. We will use V (for Vote) to represent the answer to question 1 and A (for Age) to represent the answer to question 2.


Answer to question 1
Answer to question 2
The possible values of V are 1,2 , or 3 . What are the possible values of A ?

1 or 2
9. We sent out some questionnaires. Some typical replies are shown below.

Reply Meaning
1,1 one vote for Sam Smoothe, voter is under 30
1,2 one vote for Sam Smoothe, voter 30 or over
3,1 no opinion, voter is under 30
What does the reply 2,2 mean? $\qquad$
one vote for Gabby Gruff, voter is 30 or over
10. We want to write a program to summarize data for a two-question questionnaire. We will use subscripted variables to count votes as shown on the following page.


In other words, $\mathrm{C}(1,1)$ will hold the count for Sam Smoothe by people under 30. $\mathrm{C}(1,2)$ will hold the total for Sam Smoothe by people 30 or over. $C(2,1)$ will hold the total for $\qquad$ by people

What subscripted variable will hold the No opinion count for people 30 or over? $\qquad$

```
-- - - - - - - 
```

Gabby Gruff; under 30; $\mathrm{C}(3,2)$
11. Here are 29 replies to our questionnaire. Remember, each reply is a pair of numbers and represents one vote. The first number of each pair is the answer to question 1. The second number of each pair is the answer to question 2.

| 3,1 | 2,2 | 3,2 | 1,2 | 1,2 | 2,1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2,2 | 1,1 | 1,2 | 3,1 | 3,2 | 2,2 |
| 3,1 | 2,1 | 2,2 | 1,1 | 1,1 | 1,2 |
| 1,1 | 2,1 | 2,1 | 1,2 | 2,1 | 3,1 |
| 2,1 | 3,1 | 2,1 | 3,1 | 2,2 |  |

Write the appropriate count in each box below.
Under 30
Sam Smoothe $C(1,1) \square$
30 or over

Gabby Gruff $\quad C(2,1) \square$
$\mathrm{C}(1,2) \square$


No opinion

12. Naturally, we want the computer to do the counting. Below is the beginning of our program.

```
1\emptyset\emptyset REM***VOTE COUNTING, TWO QUESTIONS
11\varnothing DIMC(3,2)
```

The DIM statement (line 110) defines an array with at most 3 rows and 2 columns. That is, the DIM statement defines an array of doubly-subscripted variables in which the maximum value of the first subscript is 3 and the maximum value of the second subscript is 2 . You must always DIM doublysubscripted arrays or you'll get an error message.


Next, we want to set all counts to zero. That is, we want to assign zero to $C(1,1), C(1,2)$, and so on up to $C(3,2)$. Even though other versions of BASIC might do this automatically, it is good programming practice to initialize every program. You complete this part of the program.

Here are four ways to do it!

## Method 1

```
21\varnothing LET C (1,1)=\varnothing
22\varnothing LET C(1,2)=\varnothing
23\varnothing LET C(2,1)=\varnothing
24\varnothing LET C (2,2)=\varnothing
25\varnothing LET C (3,1)=\varnothing
26\varnothing LET C (3,2)=\varnothing
```

Method 2
$21 \varnothing$ FOR $K=1$ TD 3 $22 \emptyset$ LET $C(K, 1)=\varnothing$ $23 \varnothing$ LET $C(K, 2)=\varnothing$
240 NEXT K

## Method 3

```
21\varnothing FOR K=1 TO 3
22\emptyset FOR L=1 TO 2
23\varnothing LET C C K,L)=\varnothing
240 NEXT L
250 NEXT K
```

Method 4

```
21\varnothing FOR K=1 TO 3:FOR L=1 TO 2:LET C(K,L)=\varnothing : NEXT L : NEXT K
```

We will usually use Methods 3 and 4 because they are easily generalized to arrays of different sizes. Using Method 3, we can add more rows by changing line 210, more columns by changing line 220 . (Of course, we would also have to change the DIM statement.)
13. The array is now set up. Let's READ and count the votes.

```
3\varnothing\varnothing REM***READ AND COUNT VOTES
31\varnothing READ V,A : IF V=-1 THEN 41\varnothing
32\varnothing LET C(V,A)=C(V,A)+1:GOTO 31\varnothing
```

Line 320 is the crucial vote-counting statement. It adds 1 (vote) to the array element specified by V and A . Suppose this is the array before executing lines 310 and 320.

| C(1,1) | 0 | C(1,2) | 4 |
| :---: | :---: | :---: | :---: |
| C $(2,1)$ | 2 | $\mathrm{C}(2,2)$ | 7 |
| C(3,1) | 5 | C(3,2) | 0 |

Show how the array would look after this additional data was processed.

14. Since line 310 is a READ statement, some DATA statements must be given somewhere. Here they are, featuring the data from frame 11.

```
90. REM ** DATA IN PAIRS:
9\varnothing1 REM ** VOTE FOLLOWED BY AGE GROUP
91\varnothing DATA 3,1, 2,2, 3,2, 1,2, 1,2, 2,1
92ø DATA 2,2, 1,1, 1,2, 3,1, 3,2, 2,2
930 DATA 3,1, 2,1, 2,2, 1,1, 1,1, 1,2
94ø DATA 1,1, 2,1, 2,1, 1,2, 2,1, 3,1
950 DATA 2,1, 3,1, 2,1, 3,1, 2,2, -1,-1
```

Remember, each reply is a pair of numbers representing one vote. To emphasize this, we have typed a space after each reply (pair of values) in the DATA statements above. Why is the flag $-1,-1$ instead of just -1 ? $\qquad$
$\qquad$
$\qquad$
_ - - - - - - - -

If the computer could not find a value for READ variable A as well as variable V in line 310 , it would print a data error message and stop.
15. Only one task remains-print the results! For the data shown in frame 14, the results should look like the one on the following page when the program is RUN.

| RUN |  |  |
| :--- | :--- | :--- |
| CAND. | UNDER | $3 \varnothing$ |
|  |  | $3 \varnothing+$ |
| SMOOTHE | 4 |  |
| GRUFF | 7 | 5 |
| NO OPIN | 6 | 5 |

You do it. Complete the program segment to print the results- $\mathrm{C}(1,1)$, $\mathrm{C}(1,2)$, and so on-as shown above.
$4 \varnothing \varnothing$ REM***PRINT THE RESULTS

We did it like this.

```
4ø\emptyset REM ** PRINT THE RESULTS
41\varnothing PRINT "CAND.","UNDER 3\varnothing'","3\varnothing +"
42\varnothing PRINT
430 PRINT "SMOOTHE",C(1,1),C(1,2)
44\emptyset PRINT "GRUFF",C(2,1),C(2,2)
450 PRINT "NO OPIN",C(3,1),C(3,2)
```

16. Here's a listing of the complete vote-counting program.
```
1\varnothing\varnothing REM ** VOTE COUNTING, }2\mathrm{ QUESTIONS
11@ DIM C(3,2)
2ø\varnothing REM ** INITIALIZE
21\varnothing FOR K=1 TO 3:FOR L=1 TO 2
22\varnothingC(K,L)=\varnothing
23\varnothing NEXT L:NEXT K
3\varnothing\varnothing REM ** READ AND COUNT DATA
31\varnothing READ V,A:IF V=-1 THEN 41\varnothing
32\varnothingC(V,A)=C(V,A)+1:GOTO 31\varnothing
4ø\varnothing REM ** PRINT THE RESULTS
41\emptyset PRINT "CAND.","UNDER 3\emptyset","3\emptyset +"
420 PRINT
43\varnothing PRINT "SMOOTHE",C(1,1),C(1,2)
440 PRINT "GRUFF",C(2,1),C(2,2)
45ø PRINT. "NO OPIN",C(3,1),C(3,2)
9øø REM ** DATA IN PAIRS:
9ø1 REM ** VOTE FOLLOWED BY AGE GROUP
91D DATA 3,1,2,2,3,2,1,2,1,2,2,1
92ø DATA 2,2,1,1,1,2,3,1,3,2,2,2
930 DATA 3,1,2,1,2,2,1,1,1,1,1,2
94\varnothing DATA 1,1,2,1,2,1,1,2,2,1,3,1
950 DATA 2,1,3,1,2,1,3,1,2,2,-1,-1
```

Suppose the questionnaire had been the following.

Q1. Who will you vote for in the coming election? Circle the number to the left of your choice.

1. Sam Smoothe
2. Gabby Gruff
3. No opinion

Q2. What is your political affiliation? Circle the number to the left of your answer.

1. Democrat
2. Republican
3. Other

Modify the vote-counting program so that answers are counted as follows.

|  | Democrat | Republican | Other |
| :--- | :---: | :---: | :---: |
| Sam Smoothe | $\mathrm{C}(1,1)$ | $\mathrm{C}(1,2)$ | $\mathrm{C}(1,3)$ |
| Gabby Gruff | $\mathrm{C}(2,1)$ | $\mathrm{C}(2,2)$ | $\mathrm{C}(2,3)$ |
| No opinion | $\mathrm{C}(3,1)$ | $\mathrm{C}(3,2)$ | $\mathrm{C}(3,3)$ |

You will have to change lines $110,210,410,430,440$, and 450.
110 $\qquad$
210 $\qquad$
410 $\qquad$
430 $\qquad$
440 $\qquad$
450 $\qquad$

```
110 DIMC(3,3)
210 FOR K=1 TO 3:FOR L=1 TO 3
41\varnothing PRINT "CAND.","dEM.","repub.","Other"
420 PRINT
43\varnothing PRINT "SMOOTHE",C(1,1),C(1,2),C(1,3)
44\varnothing PRINT "GRUFF",C(2,1),C(2,2),C(2,3)
450 PRINT "NO OPIN.",C(3,1),C(3,2),C(3,3)
```

Note: Even though we changed the questionnaire, we didn't have to change the crucial vote-counting statement in line 320.
17. Here is a LISTing of the modified program and new DATA statements for the questionnaire in frame 16. You be the computer and print the output for the program when it is RUN.

```
1\varnothing\varnothing REM ** VOTE COUNTING, }2\mathrm{ QUESTIONS
11\varnothing DIM C (3,2)
2\varnothing\varnothing REM ** INITIALIZE
210 FOR K=1 TO 3:FOR L=1 TO 2
22\emptyset C(K,L)=\varnothing
23\varnothing NEXT L:NEXT K
3\varnothing\varnothing REM ** READ AND CDUNT DATA
31\varnothing READ V,A:IF V=-1 THEN 41\varnothing
32\varnothing C(V,A)=C(V,A)+1:GOTO 31\varnothing
4\varnothing\varnothing REM ** PRINT THE RESULTS
41\varnothing PRINT "CAND.","DEM.","REPUB.","OTHER"
42\emptyset PRINT
430 PRINT "SMOOTHE",C(1,1),C(1,2),C(1,3)
44ø PRINT "GRUFF",C(2,1),C(2,2),C(2,3)
450 PRINT "NO OPIN.",C(3,1),C(3,2),C(3,3)
9\varnothing\varnothing REM ** DATA IN PAIRS:
9\varnothing1 REM ** VOTE FOLLOWED BY POLITICAL AFFILIATION
91ø DATA 3,1,1,1,1,2,2,3,1,3,3,1,2,1
92ø DATA 2,2,3,2,3,3,1,1,2,3,1,2,2,1
930 DATA 3,3,3,2,3,2,2,2,1,1,1,1,3,2
94ø DATA 3,2,2,1,3,1,1,2,1,3,2,2,2,1
950 DATA 3,1,1,3,1,3,2,3,3,3,1,2,1,3
96@ DATA 2,3,2,1,3,1,1,2,3,3,2,3,2,1
97ø DATA 3,1,3,3,-1,-1
```

RUN

| CAND. | DEM. | REPUB. | OTHER |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
| SMOOTHE | 4 | 5 | 5 |
| GRUFF | 6 | 3 | 5 |
| NO OPIN. | 6 | 5 | 5 |

18. Look at this section of the program.
```
43ø PRINT "SMOOTHE",C(1,1),C(1,2),C(1,3)
440 PRINT "GRUFF",C(2,1),C(2,2),C(2,3)
45ø PRINT "NO OPIN.",C(3,1),C(3,2),C(3,3)
```

We have used the subscripted variables with the actual numerical values for the subscripts. Instead, we could have used a FOR-NEXT loop to print the results for each candidate and no opinion, and could do this using just three multiple-statement lines. Think about it carefully, then rewrite lines 430, 440, and 450 so that FOR-NEXT loops are used to print the values stored in the C array. The RUN should look exactly as it did before.

430 $\qquad$
440 $\qquad$
450

```
430 PRINT "SMOOTHE", : FOR X=1 TO 3 : PRINT C(1,X), : NEXT : PRINT
44\varnothing PRINT "GRUFF", : FOR X=1 TO 3 : PRINT C(2,X), : NEXT : PRINT
450 PRINT "NO OPIN", : FOR X=1 TO 3 : PRINT C(3,X), : NEXT
```

Note that a PRINT statement must end lines 430 and 440 . You must use PRINT to tell the computer to start a new line at character position 0 . Also, the above program lines will each occupy more than one line on your display.
19. Do you remember the problem on counting candy bars? You might want to review it in Chapter 7 before we go on.

Before, we were selling one chocolate candy bar for $\$ 1.00$, on which the profit was $\$ .55$. Now let's add another product-a bag of jelly beans which sells for $\$ .50$, on which we profit $\$ .30$. Our job is to re-program our computer to tabulate individual sales and overall profits. Here's the report we'd like to produce.

| RUN |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| KID ID $\#$ | TOTAL |  |  |  |
| 1 |  | $\varnothing$ | $C H O C$ | $J . B E A N S$ |
| 2 |  | 3 | $\varnothing$ | $\varnothing$ |
| 3 |  | $\varnothing$ | 3 | $\varnothing$ |
| 4 |  | 6 | $\varnothing$ | $\varnothing$ |
| 5 |  | $1 \varnothing$ | 3 | 6 |
| 6 |  | $\varnothing$ | 6 | 8 |
| 7 | $\varnothing$ | $\varnothing$ | $\varnothing$ |  |
| 8 |  | 12 | $\varnothing$ | $\varnothing$ |
| TOTALS: | 31 | 6 | 12 |  |
| PROFITS: | 17.7 | 9.9 | 7.8 |  |

(a) From the report above, who had the greatest overall dollar sales? $\qquad$
(b) Who sold the most chocolate bars? $\qquad$
(c) The most jelly beans? $\qquad$
(d) Can you tell who made us the most profit? $\qquad$
(a) 8
(c) 8
(b) 5 and 8
(d) not directly from the report. (It's number 8.)
20. For recordkeeping purposes we will prepare some preprinted forms to keep track of who takes what. Now, when one of the kids asks for candy we fill in a form like the one on the following page.

| Name | Danny |
| :--- | :--- | :--- |
| ID No. | 4 |
| 1. Milk  <br> 2. Jelly  | 3 |

This shows that Danny (number 4) took 3 chocolate bars and 6 bags of jelly beans. When we convert that into computer data we use this format.
kid number, candy number (1 or 2 ), quantity
Thus, to show the data on this one slip requires 6 data items.

DATA
$\begin{array}{cc}\text { Kid ID No. Quantity } & \text { Kid ID No. Quantity } \\ 4, \underset{\sim}{1}, 3,2,2,6 \\ \text { Chocolate } & 4,2 \\ \text { U } & \text { Jelly beans }\end{array}$
(Notice how we designed the form to conform to our system of data entry!)
From the three forms below, complete the DATA statements. Include end-of-data flags.

| ID No. 5 | ID No. 2 | ID No. 8 |
| :---: | :---: | :---: |
| 1.6 | 1. 3 | 1. 6 |
| 2. 8 | 2. 0 | 2. 12 |

```
9\varnothing\varnothing REM***KID ID NUMBER, CANDY ID NUMBER, QUANTITY
91\varnothing DATA 4,1,3, 4, 2,6
92\varnothing
930
```

$\qquad$


This data is not even necessary, since this kid didn't take any jelly beans to sell.

```
92\varnothing DATA 5,1,6, 5,2,8, 2,1,3, 2,2,\varnothing
93\emptyset DATA 8,1,6, 8,2,12, -1,-1,-1<
21. Our array will look like this.
\begin{tabular}{|c|c|}
\hline Array A. & 2 = jelly beans \\
\hline 1 = Jerry & \\
\hline \(2=\) Bobby & \\
\hline 3 = Mary & \\
\hline 4 = Danny & \\
\hline 5 = Karl & \\
\hline \(6=\mathrm{Mimi}\) & \\
\hline 7 = Doug & \\
\hline \(8=S \operatorname{cott}\) & \\
\hline
\end{tabular}

Here is another way to visualize the same A-array.


Kid ID No.

Your first task is to write the statement(s) to initialize the array and zero it out, that is, set the dimensions and set the values for all the variables to zero. Don't forget the zero element. We'll be using it, too!
```

1ø\varnothing REM***CANDY BAR \& JELLY BEAN COUNTER
11ø REM***INITIALIZE
12ø
13%

```
\(\qquad\)
```

14%

```
\(\qquad\)
```

15\varnothing

```
\(\qquad\)
```

-     -         -             -                 -                     -                         -                             -                                 - 

12ø DIM A(8,2)
13\varnothing FOR X=\varnothing TO 8:FOR Y=\varnothing TO 2
14\varnothing A(X,Y)=\varnothing
15\varnothing NEXT Y:NEXT X

```
22. Now READ a set of data ( \(\mathrm{K}, \mathrm{C}, \mathrm{Q}\) ) and test for the end-of-data condition. When you encounter the end-of-data flag, jump to 410.
```

2\emptyset\varnothing REM***READ DATA AND TEST FOR FLAG
21\varnothing
21\varnothing READ K,C,Q : IF K=-1 THEN 41\varnothing

```
\(\qquad\)
23. The heart of this program is found in line 220, where the "accumulation" takes place.
```

220 A(K,C)=A(K,C)+Q : GOTO 21\varnothing

```


Go back and read some more.

K is the kid ID number, C is the candy number \((1=\) chocolate, \(2=\) jelly beans), and Q is the quantity. Assume we have the following DATA.
\(91 \varnothing\) DATA 4,1,3
(a) The value of what array element (subscripted variable) will be increased?
\(\qquad\)
(b) By how much will it be increased? \(\qquad\)
- - - - - - - -
(a) \(\mathrm{A}(4,1)\)
(b) 3
24. If the array looked like this before:


Kid ID No.

A
\begin{tabular}{|c|c|c|}
\hline \((1,2)\) & 10 & \\
\hline \((2,2)\) & 0 & \\
\hline \((3,2)\) & 8 & \\
\hline \((4,2)\) & 12 & \\
\hline \((5,2)\) & 0 & \\
\hline \((6,2)\) & 8 & \\
\hline \((7,2)\) & 9 & \\
\hline \((8,2)\) & 10 & \\
\hline \(\uparrow \uparrow\) Jelly beans & & Quantity \\
\hline
\end{tabular}

Kid ID No.

How will it look after accumulating the data in these DATA statements?
```

91ø DATA 4,1,3, 4,2,6
92ø DATA 5,1,6, 5,2,8, 2,1,3, 2,2,ø
930 DATA 8,1,6, 8,2,12

```

A


A

\begin{tabular}{|c|c|c|c|}
\hline \multicolumn{4}{|l|}{A} \\
\hline \((1,1)\) & 7 & \((1,2)\) & 10 \\
\hline \((2,1)\) & 3 & \((2,2)\) & 0 \\
\hline \((3,1)\) & 6 & \((3,2)\) & 8 \\
\hline \((4,1)\) & 8 & \((4,2)\) & 18 \\
\hline \((5,1)\) & 9 & \((5,2)\) & 8 \\
\hline \((6,1)\) & 6 & \((6,2)\) & 8 \\
\hline \((7,1)\) & 8 & \((7,2)\) & 9 \\
\hline \((8,1)\) & 9 & \((8,2)\) & 22 \\
\hline
\end{tabular}
25. Here is our program, so far.
```

1\varnothing\varnothing REM ** CANDY COUNTER
11\varnothing REM ** INITIALIZE
12ø DIM A(8,2)
13\varnothing FOR X=\varnothing TO 8:FOR Y=\varnothing TO 2
14\varnothing A(X,Y)=\varnothing
15% NEXT Y:NEXT X
29\varnothing REM ** READ DATA \& TEST FOR FLAG
21\varnothing READ K,C,Q:IF K=-1 THEN 31\varnothing
22\varnothing A(K,C)=A(K,C)+Q:GOTO 21\varnothing
91ø DATA 4,1,3, 4,2,6
92ø DATA 5,1,6, 5,2,8, 2,1,3, 2,2,\varnothing
93ø DATA 8,1,6, 8,2,12, -1,-1,-1

```

Now let's print a preliminary report like the one in frame 19, but without any totals. You fill in the blanks in the program on the following page. This is how the report should look when the program is RUN.

```

4ø\varnothing REM***REPORT \#1
41\varnothing PRINT "KID ID *"
42ø FOR K=1 TO 8
430 PRINT K, «The comma is important.
44\varnothing FOR C=1 TO-_
450 PRINT

```
\(\qquad\)
``` , The comma is important.
46@ NEXT C
470 PRINT
48\varnothing NEXT
```

$\qquad$

```
-- - - - - - - -
41\varnothing PRINT "KID ID *", "CHOC", "J.bEANS"
440 FOR C=1 TO 2
450 PRINT A(K,C),
48@ NEXT K
```

26. In frame 25 , why are the commas placed at the end of lines 430 and 450 ?

-     -         -             -                 -                     -                         -                             -                                 - 

to suppress the normal carriage return after the PRINT (that is, to keep the computer output on the same line)
27. Why did we include line 470 PRINT where we did? $\qquad$
$\qquad$
$\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

to force a carriage return (start a new line of display), so the next KID ID No. will be printed in the correct place or position when line 420 is executed again.
28. Running our program now gives these results.

| RUN <br> KID ID <br> 1 | CHOC <br> $\varnothing$ | J.BEANS <br> 2 |
| :--- | :--- | :--- |
| 3 |  | $\varnothing$ |
| 3 | $\varnothing$ | $\varnothing$ |
| 4 |  | 3 |

Now, let's complete the program so it will print everything shown in frame 19.

When we DIMensioned our array DIM $(8,2)$ it included the 0,0 elements shown below. We are going to use these zero elements to accumulate totals.


You fill in the blank lines in the program on the following page. Line 120 is fixed to set all array elements (boxes) to zero, starting at the 0,0 element. Line 320 adds the total sales per kid (remember, jelly beans sell for $\$ .50$ per bag). And line 350 adds units sold.

```
1\varnothing\varnothing REM ** CANDY COUNTER
110 REM ** INITIALIZE
12\varnothing DIM A(8,2)
13\varnothing FOR X=\varnothing TO 8:FOR Y=\varnothing TO 2
140 A (X,Y)=\varnothing
15\varnothing NEXT Y:NEXT X
200 REM ** READ DATA & TEST FOR FLAG
21\varnothing READ K,C,Q:IF K=-1 THEN 31\varnothing
22ø A(K,C)=A(K,C)+Q:GOTO 21ø
3ø\varnothing REM ** TOTAL OF UNITS SOLD AND
3\varnothing1 REM ** TOTAL OF SALES IN DOLLARS
31\varnothing FOR K=1 TO
32\varnothing A(K,\varnothing)=A(K,1)*1.\varnothing\varnothing+A(K,2)*.5\varnothing
33\varnothingA(\varnothing,\varnothing)=A(\varnothing,\varnothing)+A(K,\varnothing)
340 FOR C=
```

$\qquad$

```
35\varnothing A(\varnothing,C)=A(\varnothing,C)+A(K,
```

$\qquad$

``` )
36』 NEXT C :
37\varnothing REM ** CALCULATE PROFITS
38\varnothing P1=A(\varnothing,1)*.55 : P2=
39@ P=P1+P2
31\varnothing FOR K=1 TO 8
340 FOR C=1 TO 2
35ø A(\varnothing,C)=A(\varnothing,C)+A(K,C)
36\varnothing NEXT C : NEXT K
38\varnothing P1=A(\varnothing,1)*.55: P2=A(\varnothing,2)*.3\varnothing
```

29. Did you understand what went on in lines 320,330 , and 350 ? If not, go back and review the problem a little more. These statements are crucial for your complete understanding of this type of problem.

Write the line numbers in the labeled boxes below to show which lines generate values for those boxes.


| $(0,0)$ | 330 | $(0,1)$ | 350 | $(0,2)$ | 350 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $(1,0)$ | 320 |  |  |  |  |
| $(2,0)$ | 320 |  |  |  |  |
| $(3,0)$ | 320 |  |  |  |  |
| $(4,0)$ | 320 |  |  |  |  |
| $(5,0)$ | 320 |  |  |  |  |
| $(6,0)$ | 320 |  |  |  |  |
| $(7,0)$ | 320 |  |  |  |  |
| $(8,0)$ | 320 |  |  |  |  |

30. In frame 28 , what does line 330 do?
$33 \varnothing \quad A(\varnothing, \varnothing)=A(\varnothing, \varnothing)+A(K, \varnothing)$

-     -         -             -                 -                     -                         -                             -                                 - 

accumulate grand total sales in $\mathbf{A}(0,0)$
31. In line 390, how would you describe what the statement $\mathrm{P}=\mathrm{P} 1+\mathrm{P} 2$ accomplishes?
$39 \varnothing P=P 1+P 2$
$\qquad$
$\qquad$
computes total profits and assigns them to variable $P$
32. Time to redo our report printing section to update everything shown in the RUN on the following page (the same RUN as in frame 19). Fill in the blanks.


```
- - - - - - - - -
40\varnothing REM ** PRINT REPORT
41\varnothing PRINT "KID ID "","TOTAL $","CHOC","J
.BEANS"
42ø FOR K=1 TO 8
430 PRINT K,
44\varnothing FOR C=\varnothing TO 2
450 PRINT A(K,C),
46@ NEXT C:PRINT
47@ NEXT K
48\varnothing PRINT "TOTALS:",A(\varnothing,\varnothing),A(\varnothing,1),A(\varnothing,2)
49\varnothing PRINT :PRINT "PROFITS:",P,P1,P2
```

Now the program is done and the RUN should look just like the one above. On the following page is a complete listing of the program.

```
1ø\varnothing REM ** CANDY COUNTER
11\varnothing REM ** INITIALIZE
12\emptyset DIM A(8,2)
130 FOR X=\varnothing TO 8:FOR Y=\varnothing TO 2
14\varnothing A(X,Y)=\varnothing
15D NEXT Y:NEXT X
2ø\emptyset REM ** READ DATA & TEST FOR FLAG
210 READ K,C,Q:IF K=-1 THEN 31\varnothing
22\varnothing A(K,C)=A(K,C)+Q:GOTO 21\varnothing
3\varnothing\varnothing REM ** TOTAL OF UNITS SOLD AND
3ø1 REM ** TOTAL OF SALES IN DOLLARS
310 FOR K=1 TO 8
32\varnothing A(K,\varnothing)=A(K,1)*1+A(K,2)*\varnothing.5
33\varnothing A(\varnothing,\varnothing)=A(\varnothing,\varnothing)+A(K,\varnothing)
340 FOR C=1 TO 2
35\varnothing A(\varnothing,C)=A(\varnothing,C)+A(K,C)
360 NEXT C:NEXT K
370 REM ** CALCULATE PROFITS
38\emptyset P1=A(\emptyset,1)*ø.55:P2=A(\varnothing,2)*ø.3
390 P=P1+P2
4ø\varnothing REM ** PRINT REPORT
41\varnothing PRINT "KID ID #","TOTAL $","CHOC","J
.BEANS"
42ø FOR K=1 TO 8
43\varnothing PRINT K,
44\varnothing FOR C=\varnothing TO 2
45ø PRINT A(K,C),
460 NEXT C:PRINT
47\varnothing NEXT K
48\varnothing PRINT "TOTALS:",A(\varnothing,\varnothing),A(\varnothing,1),A(\varnothing,2)
490 PRINT :PRINT "PROFITS:",P,P1,P2
91ø DATA 4,1,3, 4,2,6
92ø DATA 5,1,6, 5,2,8, 2,1,3, 2,2,\varnothing
930 DATA 8,1,6, 8,2,12, -1,-1,-1
```

32. Here is one final double array application. In a small class of 8 students, each student has taken 4 quizzes. The scores are shown below.

|  | Quiz 1 | Quiz 2 | Quiz 3 | Quiz 4 |
| :--- | :---: | :---: | :---: | :---: |
| Student 1 | 65 | 57 | 71 | 75 |
| Student 2 | 80 | 90 | 91 | 88 |
| Student 3 | 78 | 82 | 77 | 86 |
| Student 4 | 45 | 38 | 44 | 46 |
| Student 5 | 83 | 82 | 79 | 85 |
| Student 6 | 70 | 68 | 83 | 59 |
| Student 7 | 98 | 92 | 100 | 97 |
| Student 8 | 85 | 73 | 80 | 77 |

Let $\mathrm{S}(\mathrm{B}, \mathrm{J})$ be the score obtained by student B on quiz J . $\mathrm{S}(5,2)$ is the score obtained by student $\qquad$ on quiz $\qquad$ What is the value of $\mathrm{S}(5,2)$ ? $\qquad$
33. Another class might have 30 students and 5 quizzes per student. Still another class might have 23 students and 7 quizzes per student, and so on. Let's begin a program to read scores for N students and Q quizzes per student.

```
1\otimes\varnothing REM ** QUIZ-SCDRE PROGRAM
11\varnothing DIM S(3\varnothing,1\varnothing)
```

The DIM statement permits up to $\qquad$ students and up to $\qquad$ quizzes.


30; 10
34. Next, we want to read the values of N and Q for a particular set of scores-in this case, the scores shown in frame 32. For this set of scores the value of N (number of students) is $\qquad$ and the value of Q (number of quizzes) is
$\qquad$ .
$\qquad$
8; 4
35. We will put the values of N and Q and the scores in DATA statements. Now the program looks like this.

```
1\varnothing\varnothing REM ** QUIZ-SCORE PROGRAM
11\varnothing DIM S(30,1\varnothing)
9ø\varnothing REM ** LINE 91ø:VALUES OF N AND Q
910 DATA 8,4 < % SCORES
92ø DATA 65,57,71,75
930 DATA 80,9\varnothing,91,88
94@ DATA 78,83,77,86
950 DATA 45,38,44,46
96@ DATA 83,82,79,85
970 DATA 70,68,83,59
98ø DATA 98,92,1\varnothing\varnothing,97
99. DATA 85,73,8\varnothing,77
```

Your turn. Complete line 120, below, to READ the values of N and Q . 120 $\qquad$
$12 \varnothing$ READ N, $Q$ (That's all there is to it!)
36. The values of N and Q read by line 120 (in frame 35 ) will be read from which DATA statement? Line $\qquad$ .

910
37. Now let's read the N by Q array of scores using FOR-NEXT loops. Fill in the blanks.

```
13\varnothing FOR X=1 TO N: FOR Y=__RE__NEX_________ NEXT X
130 FOR X=1 TO N:FOR Y=1 TO Q:READ S (X,Y):NEXT Y:NEXT X
```

38. The numerical values read by line 130 are stored in the DATA statements, lines $\qquad$ through $\qquad$ .

920; 990
39. Now that we have the array in the computer, what shall we do with it? One thing someone might want is the average score for each student. Let's do it, beginning at line 200.

```
2ø\varnothing REM ** COMPUTE & PRINT AVERAGES
21\varnothing PRINT "STUD. #","AVERAGE"
220 FOR B=1 TO N
23\varnothing LET T=\varnothing
240 FOR J=1 TO Q
25% LET T=T+S(B,J)
260 NEXT J
27\varnothing LET A=T/Q Compute average for student B
28ø PRINT B,A « Print student number and average
29\varnothing NEXT B < Go back and compute scores for next student
```

Lines 230 through 280 are done for each student. That is, for $\mathrm{B}=1$, then $\mathrm{B}=2$, and so on up to $\mathrm{B}=\mathrm{N}$. For $\mathrm{B}=1$, what is the value of T computed by lines 230 through 260? T = $\qquad$ .
268. This is the sum of the 4 scores for student 1 . Remember, $Q=4$. Therefore, line 250 will be done for $\mathrm{J}=1, \mathrm{~J}=2, \mathrm{~J}=3$, and $\mathrm{J}=4$.
40. For $\mathrm{B}=1$, what is the value of A computed by line 270 ?
$\mathrm{A}=\mathrm{T} / \mathrm{Q}=$ $\qquad$ —.
67. $\mathrm{A}=\mathrm{T} / \mathrm{Q}=268 / 4=67$.
41. Here is the complete program and a RUN.

```
1\varnothing\varnothing REM ** QUIZ-SCORE PROGRAM
11\varnothing DIM S (30,1\varnothing)
120 READ N,Q
130 FOR X=1 TO N:FOR Y=1 TO Q
140 READ S:S (X,Y)=S
150 NEXT Y:NEXT X
2ø\varnothing REM ** COMPUTE & PRINT AVERAGES
21\varnothing PRINT "STUD. #","AVERAGE"
22ø FOR B=1 TO N
230 T=\varnothing
24ø FOR J=1 TO Q
250 T=T+S(B,J)
260 NEXT J
270 A=T/Q
280 PRINT B,A
290 NEXT B
9øø REM ** LINE 910:VALUES OF N AND Q
910 DATA 8,4
919 REM ** SCORES
920 DATA 65,57,71,75
930 DATA 80,90,91,88
940 DATA 78,82,77,86
950 DATA 45,38,44,46
960 DATA 83,82,79,85
97ø DATA 70,68,83,59
980 DATA 98,92,1\varnothing\varnothing,97
990 DATA 85,73,80,77
```

RUN
STUD. \# AVERAGE

| 1 | 67 |
| :--- | :--- |
| 2 | 87.25 |

$3 \quad 8 \varnothing .75$
$4 \quad 43.25$
$5 \quad 82.25$
$6 \quad 7 \varnothing$
$7 \quad 96.75$
$8 \quad 78.75$

Your turn. Beginning with line 300 , write a program segment to compute and print the average score for each quiz. For the data used in the program, the results might look like this.

| RUN |  |
| :--- | :--- |
| QUIZ \# |  |
| 1 |  |
| 2 | 75.5 |
| 2 | 72.75 |
| 3 |  |
| 4 | 78.125 |
|  |  |

```
30\varnothing REMARK COMPUTE AND PRINT AVERAGE OF EACH QUIZ
31\varnothing PRINT "QUIZ *","AVERAGE"
32\varnothing FOR J=1 TO Q
33\varnothing LET T=\varnothing
340 FOR B=1 TO N
350 LET T=T+S(B,J)
360 NEXT B
370 LET A=T/N
380 PRINT J,A
390 NEXT J
```

42. Suppose some students take a multiple-choice quiz, 10 questions with four possible answers per question. We want to know how many students gave answer number 1 to question number 1 , how many gave answer number 2 to question number 1 , and so on.

Here are the answers given by 7 students. Each set of answers is in a DATA statement. The last DATA statement is a "fictitious student" and really means "end of data."

```
9ø\varnothing REM ** STUDENT ANSWERS TO QUIZ
910 DATA 2,3,1,1,1,2,4,3,4,1
92ø DATA 2,3,2,4,1,2,4,2,1,1
930 DATA 2,3,2,4,1,2,4,2,1,1
94ø DATA 3,2,4,1,1,2,3,3,4,1
950 DATA 2,3,4,1,1,3,4,3,4,1
960 DATA 2,1,2,3,1,2,4,3,4,2
970 DATA 3,4,1,1,1,4,3,1,4,2
98\varnothing DATA - 1,\varnothing,\varnothing,\varnothing,\varnothing,\varnothing,\varnothing,\varnothing,\varnothing,\varnothing "Fictitious student"'
```

Student 1 (line 910) gave answer 1 to question 3. Student 5 (line 950) gave answer $\qquad$ to question 9. Student 7 (line 970) gave answer $\qquad$ to question 1.

4; 3
43. Complete the following table showing the number of students giving each answer ( $1,2,3$, or 4 ) to questions 1,2 , and 3 .

44. In frame 43, with your help, we have shown how the 7 students answered the first 3 questions. The totals look like a 3 by 4 array. If we had continued for all 10 questions the totals would have looked like a $\qquad$ by 4 array.
$\qquad$
10
45. Let's define an array T with 10 rows and 4 columns to hold the totals. Complete the following DIM statement.

```
1ø\varnothing REM***QUIZ ANALYSIS PROGRAM
11ø DIM
```

$\qquad$

```
_ _ _ - - - _ _ - 
11\varnothing DIM T(1ø,4)
```

46. For each student there are 10 answers. Let's define a list of answers $\mathbf{A}(1)$ through $\mathbf{A}(10)$. Complete the following DIM statement.
```
12ø DIM
```

$\qquad$
$-\ldots-\ldots-\ldots-\ldots$
47. We can save space by combining the two DIM statements into one DIM statement.

```
11\varnothing DIM T(1\varnothing,4),A(1\varnothing)
```

The above DIM statement defines a $\qquad$ called T• with at most 10 rows and 4 columns, and a $\qquad$ called A with at most 10 members.
———————————
two-dimensional array, matrix or table one-dimensional array, list, or vector

Note that a comma is used to separate $T(10,4)$ and $A(10)$.
48. Here is the beginning of a program to read the students' answers and compute the totals array.

```
1\varnothing\varnothing REM***QUIZ ANALYSIS PROGRAM
11\varnothing DIM T(1\varnothing,4),A(1\varnothing)
```

Next, we want to initialize the totals array. That is, we want it to be a zero array. You do it.

```
12ø REM ** INITIALIZE
130
140
150
12ø REM ** INITIALIZE
130 FOR X=1 TO 10:FOR Y=1 TO 4
14\varnothingT(X,Y)=\varnothing
150 NEXT Y:NEXT X
```

$\qquad$
49. Write a statement to read the list A of answers for one student.

```
2ø\varnothing REM ** READ ONE SET OF ANSWERS
210
22ø
```

$\qquad$

```
230
```

-     -         -             -                 -                     -                         -                             -                                 -                                     - 

$2 \varnothing \varnothing$ REM ** READ ONE SET OF ANSWERS
$21 \varnothing$ FOR $X=1$ TO $1 \varnothing$
220 READ $A: A(X)=A$
230 NEXT $X$
50. Now, is this a real student or a fictitious student? Recall that a fictitious student signals the end of data. If this is the case we want to print the answers, beginning with line 510. Complete the IF-THEN statement.

```
14\varnothing REM***CHECK FOR END OF DATA
250 IF
```

$\qquad$

``` THEN \(51 \varnothing\)
A(1)= -1
```

51. If the data are for a real student, we want to update the running tally in the T array. We did it this way.
```
3ø\varnothing REM ** UPDATE THE TOTALS ARRAY
31\varnothing FOR Q=1 TO 1\varnothing
32\varnothing T(Q,A(Q))=T(Q,A(Q))+1
33\varnothing NEXT Q
```

Here are the answers for one student. These are the values of $A(1)$ through $\mathrm{A}(10)$.

$$
2,3,1,1,1,2,4,3,4,1
$$

Suppose $\mathrm{Q}=1$. Then $\mathrm{A}(\mathrm{Q})=$ $\qquad$ and $T(Q, A(Q))$ is $T($ $\qquad$ ).
$\qquad$
2; $\mathrm{T}(1,2)$ (since $\mathrm{Q}=1$ and $\mathrm{A}(\mathrm{Q})=2$ )
52. In the above case (frame 51), what happens when the computer obeys line 320 ? $\qquad$
$\qquad$
The total in $\mathrm{T}(1,2)$ is increased by one. (It's just like counting votes!)
53. Since line 320 is in a FOR-NEXT loop, it will be done for each value of Q specified by the FOR statement. That is, it will be done for $Q=1,2,3,4,5,6$, $7,8,9$, and 10 . When $\mathrm{Q}=10$, which element of the T matrix is increased by one?
$\qquad$

$\mathrm{T}(10, \mathrm{~A}(10))$ or $\mathrm{T}(10,1)$ for the data in frame 51.
54. Let's move on. After tallying the answers for one student, we want the computer to return to line 210 and read another set of answers. (See frame 49.)

```
4\varnothing\varnothing REM**ANOTHER SET OF ANSWERS
41\varnothing GOTO 21\varnothing
```

Then the IF-THEN statement (frame 50) is encountered again. The IF-THEN statement causes the computer to go to line 510 if a fictitious student has been read. In that case, we want to print the headings and results, then stop.

Here is what the RUN should look like:

| RUN |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| A\#1 | A\#2 | A\#3 | A\#4 |  |
| S\#3 | $\varnothing$ | 5 | 2 | $\varnothing$ |
| S\#2 | 1 | 1 | 4 | 1 |
| S\#3 | 2 | 3 | $\varnothing$ | 2 |
| S\#4 | 4 | $\varnothing$ | 1 | 2 |
| S\#5 | 7 | $\varnothing$ | $\varnothing$ | $\varnothing$ |
| S\#6 | $\varnothing$ | 5 | 1 | 1 |
| S\#7 | $\varnothing$ | $\varnothing$ | 2 | 5 |
| S\#8 | 1 | 2 | 4 | $\varnothing$ |
| S\#9 2 | $\varnothing$ | $\varnothing$ | 5 |  |
| S\#1 $\varnothing$ | 5 | 2 | $\varnothing$ | $\varnothing$ |

Complete this section of the program.

```
5\emptyset\emptyset REM ** PRINT THE TOTALS ARRAY
501 REM ** A#=ANSWER NUMBER
5@2 REM ** S#=STUDENT NUMBER
51\varnothing PRINT " A#1"," A#2"," A#3",
"A#4"
52ø FOR X=1 TO 1\varnothing:PRINT "S#"; X;" ";
530
540
------- -- - 
530 FOR Y=1 TO 4:PRINT T(X,Y),
54\emptyset NEXT Y:PRINT :NEXT X
```

Here is a complete listing of the program.

```
1\varnothing\varnothing REM ** QUIZ ANALYSIS PROGRAM
11\varnothing DIM T(1\varnothing,4),A(1\varnothing)
12\varnothing REM ** INITIALIZE
130 FOR X=1 TO 10:FOR Y=1 TO 4
14\varnothing T(X,Y)=\varnothing
150 NEXT Y:NEXT X
2ø\varnothing REM ** READ ONE SET OF ANSWERS
21\varnothing FOR X=1 TO 1\varnothing
22\varnothing READ A:A (X)=A
230 NEXT X
24\varnothing REM ** CHECK FOR END OF DATA
250 IF A(1)=-1 THEN 51ø
3\varnothing\varnothing REM ** UPDATE THE TOTALS ARRAY
31\varnothing FOR Q=1 TO 1\varnothing
320 T(Q,A(Q))=T(Q.A(Q))+1
330 NEXT Q
4ø\varnothing REM ** ANOTHER SET OF ANSWERS
410 GOTO 21ø
50\varnothing REM ** PRINT THE TOTALS ARRAY
5ø1 REM ** A*=ANSWER NUMBER
5ø2 REM ** S*=STUDENT NUMBER
510 PRINT " A#1"," A#2"," A#3",
"A#4"
52ø FOR X=1 TO 1ø:PRINT "S#";X;" ";
53\emptyset FOR Y=1 TO 4:PRINT T (X,Y),
54\varnothing NEXT Y:PRINT :NEXT X
9\varnothing\varnothing REM ** STUDENT ANSWERS TO QUIZ
910 DATA 2,3,1,1,1,2,4,3,4,1
920 DATA 2,3,2,4,1,2,4,2,1,1
930 DATA 2,3,2,4,1,2,4,2,1,1
940 DATA 3,2,4,1,1,2,3,3,4,1
950 DATA 2,3,4,1,1,3,4,3,4,1
960 DATA 2,1,2,3,1,2,4,3,4,2
97@ DATA 3,4,1,1,1,4,3,1,4,2
98\varnothingDATA - 1,\varnothing,\varnothing,\varnothing,\varnothing,\varnothing,\varnothing,\varnothing,\varnothing,\varnothing,
```


## SELF-TEST

Good for you! You have reached the Chapter 8 Self-Test. These problems will help you review the BASIC instructions you have learned for dealing with arrays of numbers, using variables with double subscripts.

1. Indicate which of the following are legal BASIC doubly-subscripted variables.
$\qquad$ (a) $\mathrm{X}(2+2)$
(b) $X(5,5)$
$\qquad$ (c) $\mathrm{X} 1(100,100)$
(d) $\mathrm{X}(\mathrm{A}+\mathrm{B}, \mathrm{C})$
$\qquad$ (e) $\mathrm{X}(\mathrm{X}(1,2), \mathrm{X}(2,1))$
(f) $X(A, A)$

Questions 2 through 7 refer to the following array A.
Column 1 Column 2
Row $1 \quad 1 \quad 2$
Row 23
4
Row $3 \quad 5 \quad 6$
2. What are the dimensions of $\mathbf{A}$ ? $\qquad$
3. Write a DIMension statement for A , using line number 100.

100 $\qquad$
4. What variable locates the "box" in row 3, column 2 of A? $\qquad$
5. What is the value of the following?
(a) $\mathrm{A}(1,1)$
(b) $\mathrm{A}(3,1)$ $\qquad$
6. Let $\mathrm{X}=2, \mathrm{Y}=3$. What is the value of:
(a) $\mathrm{A}(\mathrm{X}, \mathrm{X})$ $\qquad$ (b) $\quad \mathrm{A}(\mathrm{X}+1, \mathrm{Y}-1)$ $\qquad$
7. What is the value of $\mathrm{A}(\mathrm{A}(1,2), \mathrm{A}(2,1)-1)$ ? $\qquad$
8. Write a program which uses two FOR-NEXT loops to fill a 10 by 10 array (M) with zeros.
9. Your city officials seek to conduct a census of the citizenry. Among other things, they want to analyze the age and sex breakdown of the community. They ask you to program your home computer to take data from the form below and prepare a report like the RUN shown.

## CITY CENSUS REPORT

DATA FORM
(check one box for each question)

Question one - Age Group
$\square$ 1. less than 10
2. $10-15$
3. 16-21
4. 22-30
5. $31-40$
6. $41-50$
7. 51-65
8. over 65

Question two - Sex
$\square$

1. male
2. female

Use the following DATA statements in your program.

```
9\varnothing\varnothing REM ** DATA: BY AGE GROUP, SEX
91\varnothing DATA 1,2,2,1,3,2,4,1,5,2,6,2,7,2
920 DATA 8,1,1,2,1,1,2,1,2,2,3,1,3,1
93ø DATA 3,2,3,1,3,2,4,1,4,2,5,1,5,1
94\varnothing DATA 5,2,5,2,6,1,6,2,7,1,7,2,7,2
95@ DATA 7,2,8,1,8,1,8,2,8,2,3,1,4,2
960 DATA 5, 2,6,1,6,1,7,1,8,2,-1,-1
969 REM ** TABLE HEADINGS
97@ DATA < 1\varnothing,1\varnothing-15,16-21,22-3@,31-4\varnothing,41-
5ø,51-65,>65
```

| RUN |  |  |  |
| :--- | :--- | :--- | :--- |
| AGE |  |  |  |
| <1 $\varnothing$ | TOTAL | MALE | FEMALE |
| $1 \varnothing-15$ | 3 | 1 | 2 |
| $16-21$ | 7 | 2 | 1 |
| $22-3 \varnothing$ | 4 | 2 | 3 |
| $31-4 \varnothing$ | 6 | 2 | 2 |
| $41-5 \varnothing$ | 5 | 3 | 4 |
| $51-65$ | 6 | 2 | 2 |
| $>65$ | 6 | 3 | 4 |
| TOTALS | $4 \varnothing$ | 19 | 3 |

10. Your brother-in-law owns the local "jeans" store. He carries a large inventory with tremendous variety but now finds he must cut back. The question is which items to cut back. He asks you to use your computer to analyze his sales and help him make the "which-item'" decisions. He wants to analyze sales of children's pants first. He carries 9 styles in children's pants, each style with 3 colors. For your program, you should number the styles 1 through 9 and the colors 1 through 3, so that each piece of data will look like that below.


Write a program to analyze the sales and prepare a report like the one below. Use the following DATA statements in your program.

```
9ø\varnothing REM ** STYLE,COLOR,DOLLAR SALES
91\varnothing DATA 1,1,12, 1,2,13, 1,3,14
911 DATA 2,1,22, 2,2,10, 2,3,12
9 1 2 ~ D A T A ~ 3 , 1 , 4 5 , ~ 3 , 2 , 1 4 , ~ 3 , 3 , 3 2
913 DATA 4,1,13, 4,2,10, 4,3,15
914 DATA 5,1,12, 5,2,13, 5,3,12
915 DATA 6,1,12, 6,2,12, 6,3,12
916 DATA 7,1,13, 7,2,13, 7,3,13
917 DATA 8,1,14, 8,2,14, 8,3,14
918 DATA 9,1,15, 9,2,15, 9,3,15
919 DATA 3,2,35, 5,1,50, 6,1,36
920 DATA 9,3,12, 2,3,40, 5,1,24
921 DATA 3,3,14, 4,1,48, 1,1,12
922 DATA 2,1,12, 3,1,13, -1,-1,-1
```

Here is the REPORT segment of our solution-you do the rest!

```
3ø\varnothing REM ** PRINT REPORT
31ø PRINT "S# TOT$","COLOR 1","COLOR 2"
    "COLOR 3"
32ø FOR S=1 TO 9
33ø PRINT S;" ";T(S,\emptyset),
34ø FOR C=1 TO 3
35@ PRINT T(S,C),
360 NEXT C;PRINT
370 NEXT S
38\varnothing FOR X=\varnothing TO 3
39ø PRINT "T=";T(\varnothing,X),
4ø\varnothing NEXT X
```

| RUN |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| S\# | TOT\$ | COLOR | 1 | COLOR 2 | COLOR |
| 1 | 51 | 24 | 13 | 14 |  |
| 2 | 96 | 34 | $1 \varnothing$ | 52 |  |
| 3 | 153 | 58 | 49 | 46 |  |
| 4 | 66 | 61 | $1 \varnothing$ | 15 |  |
| 5 | 111 | 86 | 13 | 12 |  |
| 6 | 72 | 48 | 12 | 12 |  |
| 7 | 39 | 13 | 13 | 13 |  |
| 8 | 42 | 14 | 14 | 14 |  |
| 9 | 57 | 12 | 15 | 27 |  |
| $T=7 \varnothing 7$ | $T=353$ | $T=149$ | $T=2 \varnothing 5$ |  |  |

## Answers to Self-Test

The frame numbers in parentheses refer to the frames in the chapter where the topic is discussed. You may wish to refer back to these for quick review.

1. (b), (d), (e), and (f) are legal (Longer variable names such as item (c) may be legal on your computer. Check the reference manual for your computer.) (frames 5-7)
2. 3,2 meaning 3 rows, 2 columns (frames 2-4)
3. 100 DIM A(3,2) (frame 12)
4. $\mathbf{A}(3,2) \quad$ (frames $9-11)$
5. (a) 1 ; (b) 5 (frame 11)
6. (a) 4 ; (b) 6 (frame 11)
7. 4 (frame 11)
8. $1 \varnothing$ DIM $M(1 \varnothing, 1 \varnothing)$
$2 \varnothing$ FOR R=1 TO $1 \varnothing$
$3 \varnothing$ FOR C=1 TO $1 \varnothing$
$4 \varnothing M(R, C)=\varnothing$
$5 \varnothing$ NEXT C
$6 \varnothing$ NEXT R
(frame 12)
9. $1 \varnothing \varnothing$ REM ** POPULATION AGE/SEX ANALYSISI $\varnothing$ $\varnothing$ REM ** POPULATION ANALYSIS
$11 \varnothing$ REM ** INITIALIZE
$12 \varnothing \operatorname{DIM} \vee(8,2), A \$(6)$
$13 \varnothing$ FOR $A=\varnothing$ TO 8:FOR $S=\varnothing$ TO 2
$14 \varnothing \vee(A, S)=\varnothing$
$15 \varnothing$ NEXT S:NEXT A
$2 \varnothing \varnothing$ REM ** READ DATA,TEST, ACCUMULATE
$21 \varnothing$ READ $A, S: I F A=-1$ THEN $31 \varnothing$
$22 \varnothing V(A, S)=V(A, S)+1: V(\varnothing, \varnothing)=V(\varnothing, \varnothing)+1$
$23 \varnothing V(\varnothing, S)=V(\varnothing, S)+1: V(A, \varnothing)=V(A, \varnothing)+1$
240 GOTO $21 \varnothing$
3øø REM ** PRINT REPORT
31ø PRINT "AGE", "total", "male", "FEmALE"
$32 \varnothing$ FOR $A=1$ TO 8
$33 \varnothing$ READ A\$:PRINT A\$,V(A, $\varnothing)$,
$34 \varnothing$ FOR $S=1$ TO 2
$35 \varnothing$ PRINT V(A,S),
$36 \varnothing$ NEXT S:PRINT :NEXT A:PRINT
$37 \varnothing$ PRINT "TOTALS", V( $\varnothing, \varnothing), V(\varnothing, 1), V(\varnothing, 2)$
$9 \varnothing \varnothing$ REM ** DATA: BY AGE GROUP, SEX
$91 \varnothing$ DATA $1,2,2,1,3,2,4,1,5,2,6,2,7,2$
920 DATA $8,1,1,2,1,1,2,1,2,2,3,1,3,1$
930 DATA $3,2,3,1,3,2,4,1,4,2,5,1,5,1$
940 DATA $5,2,5,2,6,1,6,2,7,1,7,2,7,2$
95@ DATA 7,2,8,1,8,1,8,2,8,2,3,1,4,2
960 DATA $5,2,6,1,6,1,7,1,8,2,-1,-1$
969 REM ** TABLE HEADINGS
$97 \varnothing$ DATA $<1 \varnothing, 1 \varnothing-15,16-21,22-3 \varnothing, 31-4 \varnothing, 41-$
50, 51-65,>65
(frame 19)
```
10. 10\varnothing REM ** SALES ANALYSIS
    11\varnothing REM ** INITIALIZE
    12\varnothing DIM T(9,3)
    13\varnothing FOR S=\varnothing TO 9:FOR C=\varnothing TO 3
    14\varnothingT(S,C)=\varnothing
    150 NEXT C:NEXT S
    2ø\varnothing REM ** READ,TEST,ACCUMULATE
    21\varnothing READ S,C,D:IF S=-1 THEN 31\varnothing
    22\varnothingT(S,C)=T(S,C)+D
    23\varnothingT(\varnothing,\varnothing)=T(\varnothing,\varnothing)+D
    24\varnothing T(\varnothing,C)=T(\varnothing,C)+D
25\varnothingT TS,\varnothing)=T(S,\varnothing)+D
26\varnothing GOTO 21\varnothing
30\varnothing REM ** PRINT REPORT
31ø PRINT "S*",TOT$","COLOR 1","COLOR 2"
,"COLOR 3"
32ø FOR S=1 TO 9
33ø PRINT S;" ";T(S,\varnothing),
340 FOR C=1 TO 3
350 PRINT T(S,C),
360 NEXT C:PRINT
37\varnothing NEXT S
38\varnothing FOR X=\varnothing TO 3
39ø PRINT "T=";T(\varnothing,x),
40\varnothing NEXT X
9ø\emptyset REM ** STYLE,COLOR,DOLLAR SALES
91ø DATA 1,1,12, 1,2,13, 1,3,14
911 DATA 2,1,22, 2,2,10, 2,3,12
912 DATA 3,1,45, 3,2,14, 3,3,32
913 DATA 4,1,13, 4,2,10, 4,3,15
914 DATA 5,1,12, 5,2,13, 5,3,12
915 DATA 6,1,12, 6,2,12, 6,3,12
916 DATA 7,1,13, 7,2,13, 7,3,13
917 DATA 8,1,14, 8,2,14, 8,3,14
918 DATA 9,1,15, 9,2,15, 9,3,15
919 DATA 3,2,35, 5,1,50, 6,1,36
92\emptyset DATA 9,3,12, 2,3,40, 5,1,24
921 DATA 3,3,14, 4,1,48, 1,1,12
922 DATA 2,1,12, 3,1,13, -1,-1,-1
```

(frame 32)

## CHAPTER NINE

## String Variables and String Functions

In Chapter 3, we showed you a few ways to use alphanumeric string variables. We also used string variables in the chapters that followed as we introduced new programming concepts. In this chapter we will review what you already know about string variables and introduce you to some new goodies, as well. Generally you will find that there is as wide a range of manipulation for string variables as for a numeric variable.

When you have completed this chapter you will be able to use the RESTORE statement with READ and DATA statements. You will also be able to use the following string functions with the string variables you will learn about in this chapter.

VAL
STR\$
CHR\$
ASC
LEN

1. So far, our use of alphanumeric (mixed alphabetic and numeric) phrases has mostly been limited to the use of strings in PRINT statements such as the following.
```
1\varnothing PRINT "THIS IS A STRING"
```

Now we can add a new feature to BASIC, the string variable.

```
5 DIM T$(50)
1\varnothing LET T$="STRING FOR THE STRING VARIABLE T$"
    4
        This is a string variable.
```

You identify a string variable by using any legal variable name followed by a dollar sign (\$). String variables permit you to manipulate alphanumeric data with greater ease. String variable instructions include LET, PRINT, INPUT, READ, DATA, and IF-THEN, plus special string functions.

As we noted in earlier chapters, you must use a DIM statement at the beginning of the program that is executed only once, to tell the computer how much memory space to save for the string variables used in the program. A string assigned to a string variable using a LET assignment statement is limited to about 99 characters. This is due to the limitations on statement line length, including the "wrap around" to the next lines on the display. How many characters in the string variable $\mathrm{T} \$$ above? $\qquad$ (Did you count blank spaces?)

33 characters
2. As you know, you can assign values to a string variable using an INPUT statement that asks for one or more string variables to be entered by the user.

## Example 1

```
5 DIM N$(30)
10 PRINT "WHAT IS YOUR NAME"; «
2\varnothing INPUT N$
```


## Example 2

```
5,DIM N$(30),S$(30)
1\varnothing PRINT "YOUR NAME AND SUN SIGN"; « _ Two string inputs
2\varnothing INPUT N$,S$
```


## Example 3

```
5 DIM N$(3\varnothing),C$(3\varnothing),S$(3\varnothing)
```

5 DIM N$(3\varnothing),C$(3\varnothing),S$(3\varnothing)
1\varnothing PRINT "YOUR NAME, CITY, AND STATE YOU « Three string inputs
1\varnothing PRINT "YOUR NAME, CITY, AND STATE YOU « Three string inputs
LIVE IN";
LIVE IN";
2\varnothing INPUT N$,C$,S$

```
2\varnothing INPUT N$,C$,S$
```

You may also assign numeric and string variables in the same INPUT statement as shown here.

## Example 4

```
5 DIM N$(3ø)
1\varnothing PRINT "WHAT IS YOUR NAME AND AGE"; Mixed inputs, one string
2ø INPUT N$,A and one numeric.
```

When an input statement with more than one variable, string or numeric, is encountered by the computer while executing a program, it types a question mark and waits for the user to enter the input string or value from the keyboard.

Let's say we have entered Example 2 above into the computer. We type RUN and hit the RETURN key. The display shows:

```
RUN
YOUR NAME AND SUN SIGN?
```

I respond by typing my name and press RETURN.

```
RUN
YOUR NAME AND SUN SIGN? JERALD R. BROWN
```

Now I type my sign, which is assigned to the second input variable.

```
RUN
YOUR NAME AND SUN SIGN? JERALD R. BROWN
? SCORPIO
```

If I had typed both of the things asked for after the first question mark, they would have both been assigned to N\$. If I had just pressed RETURN without entering anything after a question mark, a "null string" (a string with no characters) would have been assigned to the string variable.

```
5 DIM N$(3\varnothing)
1\varnothing PRINT "WHAT IS YOUR NAME AND AGE";
20 INPUT N$,A
3\varnothing PRINT "NAME: ";N$
4\varnothing PRINT "AGE: ";A
```

Show what the computer will print and how you should enter the information requested if the above program is RUN.

RUN

```
RUN
WHAT IS YOUR NAME AND AGE? PAUL ARMITIGE
?33
NAME: PAUL ARMITIGE
AGE: 33
```

```
3. 1\varnothingDIMN$(15)
    2\varnothing PRINT "YOUR NAME";
    3\varnothing INPUT N$
    4ø PRINT "YOUR NAME IS ";N$
```

Suppose I RUN this program.

```
RUN
YOUR NAME? JERALD RICHARD BROWN
YOUR NAME IS JERALD RICHARD
```

What happened? Did the computer forget my last name? Take a look at the DIM statement. Since string variable $\mathrm{N} \$$ was only dimensioned to accept 15 characters, it assigned the first 15 characters I entered (in response to the question) to the string variable $\mathrm{N} \$$, and just 'ignored" anything beyond that.

Suppose the program is RUN again.
RUN
YOUR NAME? JOHN JACOB JINGLEHIEMER SCMIDT
Now what will the computer say? $\qquad$

```
YOUR NAME IS JOHN JACOB JING
```

Moral: Dimension the string variables adequately.
4. Write a program to enter and print an auto license plate that has a 3-letter alphabetic string and a 3-digit number (such as SAM 123). Enter the letters as a string variable and the number as a numeric variable. Show what the RUN should look like.

```
10 DIM A$(3)
2\varnothing INPUT A$,B
30 PRINT A$;B
RUN
?SAM
?123
SAM123
```

5. You can also enter string variables by using READ and DATA statements.
```
1 REM ** STRING READ/DATA COURSE LIST
5 DIM A$(18),C$(1)
1\varnothing PRINT "COURSE ","HOURS","GRADE"
2% READ A$,B,C$
3\varnothing PRINT A$,B,C$
4\varnothing GOTO 2\varnothing
50 DATA ENGLISH 1A,3,B,SOC 13\varnothing ,3,A
6\emptyset DATA BUS ADM 1A,4,B,STAT 1\varnothing ,3,A
70 DATA HUMANITIES, 3,A,HISTORY 17A,3,B
8\varnothing DATA CALCULUS 3A,4,C
RUN
COURSE HOURS GRADE
ENGLISH 1A B
SOC 130 3
BUS ADM 1A 4 B
STAT 1\varnothing 3 C
HUMANITIES 3 A
HISTORY 17A 3 B
CALCULUS 3A 4 C
```

Look at line 10 of the preceding program. Notice the trailing spaces included in the string "COURSE." Since we have reserved two columns of standard print positions for course names, the extra spaces cause "HOURS" to be printed at the third print position, and "GRADE" at the last print position column. Another way we could have used would be to include an empty or "null string" for printing nothing at the second print position!

```
1ø PRINT "COURSE", "'" . "HOURS"."GRADE"
```

Since any string of 8 characters or less will occupy one print position column, we also included trailing spaces in the DATA statements (see lines 50 and 60 ) where the course name was eight or less characters in length. This forces the course names to use two print position columns. The following rules pertain to strings as DATA statement items.
(1) The first string item in a DATA statement can have no leading spaces, but will include trailing spaces up to the comma that separates the first string from the second item.
$91 \varnothing$ DATA HOW, NOW, BROWN, COW
Spaces before NOW, BROWN, and COW will be included.
(2) The last string item in a DATA statement can have leading spaces between the comma that precedes it and the first displayed character of the string, but no trailing spaces can be included.

```
910 DATA HOW , NOW, BROWN, COW
```

These spaces included in the string assignment, but no trailing space.
(3) The other items in a DATA statement will include any leading or trailing spaces as part of the string assignment.
$91 \varnothing$ DATA HOW , NOW, BROWN, COW
The two spaces before and two spaces after the word NOW will be included in the string assignment.
6. In the program in frame 5, how long is the string for the fourth data item in line 50 ? $\qquad$
$\qquad$
9 characters including two trailing spaces (SOC

7. How many print position columns will be occupied by the string SOC 130 when it is read from the DATA statement and printed by line 30 ? $\qquad$
$\qquad$
two, because strings of 9 characters or more controlled by commas in PRINT statement will cause the computer to skip the next usual print position. This is done automatically to keep the display from one column from running into the next displayed column. In summary, if the string variable size is greater than 9 characters, the print column sequence will not be followed, but will skip to the next available print position.
8. The string LET assigns a particular string to a string variable. Note that you must enclose the string in quotes as in these two examples.

```
1\varnothingDIM A$(3),B$(2),C$(3)
20 LET A$= "YES"
3\varnothing LET B$= "NO"
4\varnothing LET C$=A$ C$ now contains "YES",
```

Show what will be printed by this program when it is RUN.

```
1\varnothingDIM A$(2\varnothing),B$(2\varnothing)
2\emptyset LET A$=" A GOOD EXAMPLE"'
3\varnothing LET B$= "THIS IS"
4\varnothing PRINT B$;A$
RUN
```

```
RUN
THIS IS A GOOD EXAMPLE
```

9. Next we want you to write a program similar to the one in frame 5. Instead of courses and grades, the data should be books in your office or home library. Your DATA should include author, title, and number of pages. Our data looks like this:
```
90ø REM ** ORDER OF DATA:
9@1 REM ** AUTHOR, TITLE, PAGES
91\varnothing DATA BROWN,INSTANT BASIC, 178
92ø DATA WHITE,YOUR HOME COMPUTER,225
930 DATA KEMENY,BASIC PROGRAMMING,156
94\varnothing DATA OSBORNE,INTRO TO MICROCOMPUTERS
, 384
950 DATA NELSON,COMPUTER LIB/DREAM MACHI
NES,186
960 DATA THIAGI,GAMES FOR THE POCKET CAL
CULATOR,54
```

Our RUN looks like the following.

| RUN |  |  |
| :--- | :--- | :--- |
| TITLE | AUTHOR | PAGES |
| INSTANT BASIC | BROWN | 178 |
| YOUR HOME COMPUTER | WHITE | 225 |
| BASIC PROGRAMMING | KEMENY | 159 |
| INTRO TO MICROCOMP | OSBORNE | 384 |
| COMPUTER LIB/DREAM | NELSON | 186 |
| GAMES FOR THE POCK | THIAGI | 54 |

Before you write your program, look at line 940 above, and the corresponding line in the RUN. Review frame 3. Note that we have controlled the display of long titles, in this case, by limiting the string length assigned to variables by proper dimensioning of string variables. If a title is short, i.e., less than 9 characters, include trailing spaces so that it will occupy two columns. Limit the length of authors' names in the same manner. Go to it!

```
1 REM ** STRING/DATA HOME LIBRARY
5 DIM A$(8),T$(18)
1\varnothing PRINT "TITLE","","AUTHOR","PAGES"
2\emptyset READ A$,T$,P:IF A$="END" THEN END
3\emptyset PRINT T$,A$,P:GOTO 2\emptyset
9\emptyset\emptyset REM ** ORDER OF DATA :
9\emptyset1 REM ** AUTHOR, TITLE, PAGES
910 DATA BROWN,INSTANT BASIC, 178
92\emptyset DATA WHITE,YOUR HOME COMPUTER,225
930 DATA KEMENY,BASIC PROGRAMMING, 15%
94\varnothing DATA OSBORNE, INTRO TO MICROCOMPUTERS
, 384
95ø DATA NELSON,COMPUTER LIB/DREAM MACHI
NES,186
96\emptyset DATA THIAGI,GAMES FOR THE POCKET CAL
CULATOR,54
97\varnothing DATA END,\varnothing,\varnothing
```

10．Modify the program you just wrote for frame 9 so that it will only print those books with fewer than 200 pages．

25 IF $P>=2 \varnothing \varnothing$ THEN $2 \varnothing$
11．The string IF－THEN allows you to compare the contents of two string variables．

```
1\varnothing DIM A$(3),B$(2)
2\varnothing B$='NO"
3ø PRINT "DO YOU WANT INSTRUCTIONS";
4\varnothing INPUT A$
50 IF A$=B$ THEN 14\varnothing
6\varnothing PRINT "THIS SIMULATION PERMITS YOU TO
REGULATE...'
14\varnothing PRINT "THE SIMULATION BEGINS..."
```

Line 50 compares the contents of the string variable $\mathrm{A} \$(\mathrm{YES})$ to the contents of string variable $\mathrm{B} \$(\mathrm{NO})$ ．If you responded YES to the INPUT statement， $\mathrm{A} \$$ and B\＄are not equal（they do not have the same contents），the computer will execute the next statement，line 60 ，which in this case will print the instructions．If you respond NO to line 40 above，the program will branch to line 140 and continue execution there．

The comparison in line 50 is between $\qquad$ ＿．
the contents of two string variables， $\mathrm{A} \$$ and $\mathrm{B} \$$
12．You can compare the contents of a string variable to a string enclosed in quotes．

```
10 DIM A$(3)
2ø PRINT "DO YOU WANT INSTRUCIONS? YES
OR NO";
30 INPUT A$
4\varnothing IF AS="NO" THEN 14\varnothing
5\varnothing PRINT "THIS SIMULATION PERMITS YOU TO
    REGULATE..."
14\varnothing PRINT "THE SIMULATION BEGINS..."
```

The comparison in line 40 above is between a
and a $\qquad$ ．
－ー ーーーーーーーー
string assigned to a string variable（the contents of a string variable）and a string enclosed in quotes

13．You cannot compare a numeric variable to a string variable．

But you can change a string variable into its numeric equivalent using the VAL(\$) function. In the above example, if $A \$$ contained a number (entered as a string variable) you could compare it with numeric variable B by changing line 110 to read as follows.
$11 \varnothing \mathrm{IF} \operatorname{VAL}(A \$)=B$ THEN $14 \varnothing$
Here is another demonstration program. Circle the correct RUN for the program.

```
5 DIM A$(1\varnothing),B$(1\varnothing),C$(1\varnothing)
1\varnothing AS="32":B$="1.115":C$="-1五"
3\varnothing PRINT A$:PRINT VAL(A$)
4\varnothing PRINT B$:PRINT VAL(B$)
5ø PRINT C$:PRINT VAL(C$)
RUN RUN RUN
32 32 32
32 32 32
1.115 1.115 1.115
1.115 1.115 1.115
-10
-10
_ - - - - - _ _ -
```

First RUN is correct.
14. What will this program print when it is RUN?

```
5 DIMA$(1\varnothing),B$(1\varnothing),C$(1\varnothing)
1\varnothing A$="32":B$="1.115":C$="-1\varnothing"
3\varnothing PRINT VAL(A$)+VAL(B$)+VAL(C$)
RUN
```

-     -         -             -                 -                     -                         -                             -                                 - 

RUN
23.115
15. Using the STR\$ function, you can convert a numeric variable to a string or place a numeric variable into a string variable.

Will print the string equivalent of the numeric content of variable $X$.

$2 \varnothing$ LET AS $=\operatorname{STRS}(x)$ Will place into string variable $A \$$ the numeric content of variable X .
What will this program print?

```
1\varnothingV=112:PRINTV:PRINT STR$(V)
RUN
```

RUN
112
112
16. In a string IF-THEN, the comparison is made one character at a time. For example, if a space is introduced in the wrong place, it may cause a comparison other than what you expect.

```
5 DIM A$(2\varnothing)
1\varnothing INPUT A$
2\varnothing IF A$="MCGEE" THEN 14\varnothing
```

If the user enters MC GEE in response to the computer's prompt during the RUN, the comparison will not be equal. Why will this comparison not be equal?

The space between C and G is a character which is not present in 'MCGEE."
17. You can compare strings using the same symbols you used earlier: <>, <, $>,\langle=\rangle=$,, and $=$. It's a little tricky so you should use caution with these comparisons. The comparison is still made one character at a time from left to right. The first difference found determines the relationship. The relationship is based on position in the alphabet; C is "less than'' S ; T is 'greater than' M .

```
5 DIM A$(5),B$(5)
1\varnothing A$= "SMITH"
2ø B$= "SMYTH"
3\varnothing IF A$<B$ THEN 1\varnothing\varnothing
```

In line 30 above, will the program branch to line 100 or continue to the next statement in sequence? $\qquad$

-     -         -             -                 -                     -                         -                             -                                 - 

Jump to line 100. The first difference is the third character and since I is "less than'" Y, the IF-THEN condition is TRUE.
18. Here is another example.

```
1\varnothing\varnothing DIM D$(2\varnothing),E$(2\varnothing)
12\varnothing D$="COMPUTE"
13ø E$="COMPUTER"
14\varnothing IF D$<E$ THEN 18\varnothing
15\varnothing PRINT D$
160 END
18ø PRINT E$
```

Which statement will be executed after the comparison in line 140 ? $\qquad$
$\qquad$
Line 180. D\$ is "less than" $\mathrm{E} \$$. It is smaller in size, therefore "less than' $\mathrm{E} \$$.
19. Change line 140 in frame 18 to read as follows.

140 IF D\$ $=E \$$ THEN 180
Now which statement will be executed after the comparison of line 140 ?


Line $150 . \mathrm{D} \$$ is not equal to $\mathrm{E} \$$.
20. In frame 18 change line 140 to read as follows.
$14 \varnothing$ IF E\$ $>$ D\$ THEN $18 \varnothing$
Which statement will be executed after the comparison? $\qquad$

-     -         -             -                 -                     -                         -                             - 

Line 180. $\mathrm{E} \$$ is "greater than" $\mathrm{D} \$$.
21. To expand your understanding of string comparisons, we would like to introduce you to the ASCII (pronounced ASKEE) code. Who's ASCII, you ask? ASCII stands for the American Standard Code for Information Interchange. For each character you type on the keyboard, an ASCII code number for that character is sent to the computer. The computer sends back an ASCII code number for each character that appears on your printer or screen. That's the "information interchange" referred to by ASCII.

ATARI BASIC allows us to enter ASCII code numbers instead of keyboard characters with the use of the CHR\$ function and allows us to convert a character into its ASCII code number using the ASC function.
CHR\$(X) The ASCII number to be converted is placed in X before you use this function. Or you can place the number directly into the parentheses instead of X , as in CHR\$(65).

ASC(X\$) The string character to be converted to ASCII code is placed in $\mathrm{X} \$$ before execution.

For example, the uppercase letters we use in BASIC correspond to ASCII code numbers 65 to 90 inclusive: $A=65, B=66, C=67, \ldots X=88, Y=89, Z=90$. A complete table of ASCII code numbers and the characters they represent can be found in the Appendix.

The little program below prints a quotation from John Wayne that is found in the DATA statement in ASCII code numbers.

```
1\varnothing READ }X\mathrm{ : IF }X=-1 THEN END
2\varnothing PRINT CHR$(X); : GOTO 1\varnothing
3\emptyset DATA 89,85,8\emptyset,-1
```

RUN
YUP
Referring to that table of ASCII code numbers, tell what the following program will print when RUN.

```
1\varnothing READ A : IF A = -1 THEN END
2\emptyset PRINT CHR$(A); : GOTO 1\varnothing
3ø DATA 72,65,80,8\emptyset,89,32,67,79,77,80,85,84,73,78,71,-1
```

RUN
HAPPY COMPUTING
22. Using the ASC function you can find out the ASCII code number for a string character. Here's a demonstration.

```
5 DIM X$(1),Y$(1),Z$(1)
1\varnothing X$="A":Y$= 'B":ZS="C"
2\emptyset PRINT "A = ";ASC(X$),"B= ";ASC(Y$),"
C=";ASC(Z$)
```

RUN
$A=65 \quad B=66 \quad C=67$

Write a program using the ASC function to provide you with the ASCII code for the following characters, so that the RUN looks like this.

```
RUN
CHAR ASCII CODE
$ 36
= 61
? 63
```

Here are two possible solutions.

```
5 DIMA$(1),B$(1),C$(1)
1@ A$="$":B$="=":C$="?"
2\emptyset PRINT "CHAR.","ASCII CODE"
3% PRINT
4\varnothing PRINT A$,ASC(A$)
5% PRINT B$,ASC(B$)
6\varnothing PRINT C$,ASC(C$)
```

23. Now, let's return to string comparisons using the IF-THEN statement. Strings are compared using a character by character process and the computer uses ASCII code numbers to do the comparing. For example, in frame 12, we saw this program segment.
```
5 DIM A$(1\varnothing)
1\varnothing INPUT A$
2\varnothing IF A$ = "MCGEE" THEN 14\varnothing
```

When the program is RUN and the user enters MC GEE, the computer compares ASCII code numbers as follows.

$$
\begin{array}{ll}
" M C G E E " & \text { A\$ (user-entered) } \\
\mathrm{M}=77 \\
\mathrm{C}=67=77 \\
\mathrm{G}=71 \\
\mathrm{E}=69 \\
\mathrm{E}=69 & \mathrm{C}=67 \\
\text { space }=32 \\
\mathrm{G}=71 \\
\mathrm{E}=69 \\
\mathrm{E}=69
\end{array}
$$

The computer finds the two strings equal for the first two characters, but the third character comparison is unequal (71 vs. 32).

Show how the computer, using ASCII codes, will compare the strings in the following segment, just as we did above.

```
5 DIM A$(3)
1\varnothing INPUT "DO YOU WANT INSTRUCTIONS? YES OR NO"; A$
2\varnothing IF A$ = "NO" THEN 14\varnothing
RUN
DO YOU WANT INSTRUCTIONS? YES OR NO? YES.
```

Is the comparison true or false? $\qquad$


A\$ "NO"
$\mathrm{Y}=89 \quad \mathrm{~N}=78$
$\mathrm{E}=69 \quad \mathrm{O}=79$
$\mathrm{S}=83$
The comparison is false.
24. Before you proceed, we need to introduce the RESTORE statement and its use in connection with READ and DATA statements. A READ statement causes the next item(s) of data to be read from the DATA statements. You may find that you want the program to read through the data from the beginning again.

To do so, use a RESTORE statement, which causes the next DATA item to be READ to be the first piece of data in the first DATA statement. In other words, with the next READ statement that the computer comes to, it starts at the beginning of the DATA. See Line 30 below.

Now that you have seen how to use string variable comparisons, you can understand this simple information retrieval program that permits retrieving information from DATA statements.

The program in frame 5 prints courses, hours, and grades. The program below permits the operator to enter the course: the computer will then print the course, hour, and grade.

```
1 REM ** COURSE INFO RETRIEVAL
5 DIM A$(18),D$(18),C$(1)
1\varnothing PRINT "ENTER COURSE NAME';
2\varnothing INPUT D$
3\varnothing RESTORE
4\varnothing READ A$,B,C$: IF A$=D$ THEN 60
5\varnothing GOTO 4\varnothing
6\emptyset PRINT A$,B,C$:PRINT :GOTO 1\varnothing
9ø\varnothing REM ** COURSE,UNITS,GRADE
910 DATA ENGLISH 1A,3,B,SOC 130,3,A
920 DATA BUS ADM 1A,4,B,STAT 1\varnothing,3,C
930 DATA HUMANITIES,3,A,HISTORY 17B,3,B
RUN
ENTER COURSE NAME? HUMANITIES
HUMANITIES 3 A
ENTER COURSE NAME? STAT 1\varnothing
STAT 1\varnothing 3 C
ENTER COURSE NAME? ECON 1A «ఒWhoops, no such course. The com-
ERROR- 6 AT LINE 40
```

puter read through all the data and found no such course; therefore, it printed this error message.

Let's look at another RUN of the program.

```
RUN
ENTER COURSE NAME? SOC13\varnothing
ERROR- 6 AT LINE 4\varnothing
```

Why did we get an error message this time?

The course name is stored SOC 130, but the user typed SOC130 without a space between SOC and 130.

Note also that you cannot leave leading and trailing spaces when you INPUT from the keyboard, so do not leave leading or trailing spaces in DATA statement string items that are to be compared to INPUT items, or the comparisons will not work as expected.
25. Refer back to the program in frame 24.
(a) What is the purpose of this part of line 40 ?
...IF $A \$=D \$$ THEN $6 \varnothing$
(b) Under what conditions will line 50 be executed? 50 GOTO 40
$\qquad$
(a) to test whether or not the course read from the DATA statement is the course requested in the INPUT statement
(b) when the course read by line 40 is not the course requested in the INPUT statement
26. Modify the program in frame 24 so it will print the message "NO SUCH COURSE" instead of the data error message, indicating that the course entered by the user does not exist in the computer's information system. You should put a flag at the end of the regular data.

Add these statements (or ones similar to them).

```
4 5 ~ I F ~ A \$ ~ = ~ " E N D " ~ T H E N ~ P R I N T ~ " N O ~ S U C H ~ C O U R S E " ~ : ~ G O T O ~ 1 \varnothing ~
94\varnothing DATA END, \varnothing,\varnothing
```

Remember, the end-of-data signal must contain a string, followed by a numeric value, followed by a string, because the READ statement calls for three variables at once.
27. It's your turn. Write a program that contains the names and phone numbers of your friends and business associates that you would like to "retrieve" using your computer. When you type in a name, the computer should respond with the correct phone number, as shown below.

```
NAME? ADAM OZ
ADAM OZ 415-555-2222
NAME? JUDY WIL
JUDY WIL 112-555-0075
NAME? JERRY
ERROR- 6 AT LINE 4\varnothing
```

```
1 REM ** TELEPHONE NUMBER RETRIEVAL
1\varnothing DIM N$(8),D$(8),T$(12)
2\varnothing PRINT "NAME";:INPUT N$
3\varnothing RESTORE
4\varnothing READ D$,T$
50 IF N$=D$ THEN PRINT :PRINT D$,T$:PRIN
T :GOTO 2\varnothing
60 GOTO 4\varnothing
9ø\varnothing REM ** DATA:NAME,PHONE NUMBER
910 DATA TONY BOD,415-555-8117
920 DATA MARY JAY,213-555-6144
930 DATA MARY MMM,213-555-1212
94ø DATA JUDY WIL,112-555-ø075
950 DATA ADAM OZ,415-555-2222
960 DATA BOBBY ALL,312-555-1667
97\varnothing DATA END,END
```

28. Next, we will show you another function that allows you to manipulate and examine parts of strings, called substrings. A substring is a part of a string and is defined by using subscripts after the string variable, $\mathrm{A} \$(10)$ or $\mathrm{A} \$(1,5)$.
```
5 DIM AS(3D)
1\varnothing LET A$="MY HUMAN UNDERSTANDS ME"
2ø PRINT AS (1\varnothing) ఒ\longmapsto The substring begins at the 10th
RUN
    character and includes all the characters
    that follow
```

UNDERSTANDS ME

Replace Line 20 with PRINT A\$(15). What will be printed when the new Line 20 is RUN?

STANDS ME
29. Now look at these examples. To isolate one character you need to use the value twice indicating the first and the last character of the substring.

```
5 DIM A$(30)
1\varnothing LET A$="MY HUMAN UNDERSTANDS ME"
2\emptyset PRINT AS (4,4) & Will print H, the 4th character in the
RUN
string. (A space counts as one character)
```

H

Here we have a substring that starts at character 1 and includes all of the characters through and including the 9th character.

```
5 DIM A$( 30)
1\varnothing LET A$= "MY HUMAN UNDERSTANDS ME"
2\varnothing PRINT A$(1,9)
RUN
MY HUMAN
```

In the program directly above, change Line 20 to read PRINT A\$(4,8). What will be printed when the new Line 20 is executed?

```
_ - - - - - - - -
```

HUMAN
30. What will be printed by the following program?

## $1 \varnothing$ DIM A\$(2ø)

$2 \varnothing$ LET $A \$=$ "GAMES COMPUTERS PLAY"
$3 \varnothing$ PRINT $A \$(7,15), A \$(17), A \$(1,5)$

RUN
COMPUTERS PLAY GAMES
31. Here are parts of a program to print the string variable $\mathrm{A} \$$ backwards, one character at a time. Fill in the blanks and show the RUN.

```
5 DIM A$(__)
1\varnothing LET A$="ABCDEFGHIJKLMNOPQRSTUVWXYZ"
2. FOR X=__TO__STEP - }
30 PRINT A$(X,___);
4ø
```

```
5 DIM A$(26)
1ø LET A$="ABCDEFGHIJKLMNOPQRSTUVWXYZ"
20 FOR X=26 TO 1 STEP - 1
30 PRINT AS ( }x,x)\mathrm{ ;
4\varnothing NEXT X
RUN
32. Let's go all the way back to frame 9 of Chapter 1 and change our number guessing game to a letter guessing game. Here's the old program. All its logic should still apply.
```

1\emptyset\emptyset REMARK***THIS IS A SIMPLE COMPUTER GAME
11\varnothingLET X = INT(1Ø考RND(1))+1
120 PRINT
13\varnothing PRINT "I'M THINKING OF A NUMBER FROM 1 TO 1\varnothing\varnothing."
14\emptyset PRINT "GUESS MY NUMBER!!!"
150 PRINT : INPUT "YOUR GUESS"; G
16\emptyset IF G<X THEN PRINT "TRY A BIGGER NUMBER" : GOTO 15\emptyset
17\varnothing IF G>X THEN PRINT "TRY A SMALLER NUMBER" : GOTO 150
18\varnothing IF, G=X THEN PRINT "THAT'S IT!!'! YOU GUESSED MY NUMBER." : GOTO 11\varnothing

```

We should first add line 101 to DIM A\$ and INPUT variable G\$; also X\$ to store the computer's letter to be guessed. Line 105, a LET statement with all the letters of the alphabet assigned to A\$.

101 \(\qquad\)
105 \(\qquad\)
\(1 \varnothing 1\) DIMA\$(26),G\$(1),X\$(1)
105 LET A\$ = "ABCDEFGHIJKLMNOPQRSTUVW \(X Y Z\) "
33. Now change line 110 to randomly select a number between 1 and 26 .

110 \(\qquad\)
- - - - - - - - -
\(11 \varnothing\) LET \(x=\operatorname{INT}\left(26^{*}\right.\) RND (1) \()+1\)
34. Let's place our selected choice into \(\mathrm{X} \$\).

115 LET \(\mathrm{X} \$=\) \(\qquad\)

LET \(X \$=A \$(X, X)\)
35. You complete lines 140 and 150 .

130 PRINT "I'M THINKING OF A LETTER FORM A TO \(Z\) "
\(14 \varnothing\)
\(15 \varnothing\)
- - - - - - - - -
\(14 \boldsymbol{0}\) PRINT "GUESS MY LETTER!!!" : PRINT
15ø PRINT "YOUR GUESS": INPUT G\$
36. Change lines 160,170 , and 180 as necessary. RUN your new game.
\(\qquad\)
- - - - - - - - -

Here's the entire LIST and a RUN.
```

1ø凤 REMARK***A SIMPLE COMPUTER GAME
1\varnothing1 DIM A$(26),G$(1),X$(1)
1ø5 LET A$ = "ABCDEFGHIJKLMNOPQRSTUVWXYZ"
11\varnothing LET }X=\operatorname{INT}(26*RND(1))+
115 LET X\$ = A\$ ( X,X)
120 PRINT
13\varnothing PRINT ''I'M THINKING OF A LETTER FROM A TO Z''
14\varnothing(PPRINT "GUESS MY LETTER!!!":PRINT
150 PRINT "YOUR GUESS"; INPUT G\$
160 IF G$<X$ THEN PRINT "TRY A BIGGER LETTER." : GOTO 15\varnothing
17\varnothing IF G$>X$ THEN PRINT "TRY A SMALLER LETTER." : GOTO 15\varnothing
18\varnothing IF G$=X$ THEN PRINT "THAT'S IT!!! YOU GUESSED MY LETTER.": GOTO 11\varnothing
RUN
I'M THINKING OF A LETTER FROM A TO Z
GUESS MY LETTER!!!
YOUR GUESS? L
TRY A SMALLER LETTER.
YOUR GUESS? G
TRY A BIGGER LETTER.
YOUR GUESS? H
TRY A BIGGER LETTER.
YOUR GUESS? K
TRY A SMALLER LETTER.
YOUR GUESS? I
TRY A BIGGER LETTER.
YOUR GUESS? J
THAT'S IT!!! YOU GUESSED MY LETTER.

```
37. Using the data from the program in frame 27, write a program that will print a list of phone numbers of people whose first name begins with the letter M.
```

RUN

```

```

REM ** TELEPHONE DIRECTORY
1\varnothing DIM D$(8),T$(12)
2ø RESTORE
3@ READ D$,T$:IF D$(1,1)=''M" THEN PRINT
D$,T\$
4\varnothing GOTO 3ø
9\varnothing\varnothing REM ** DATA: NAME, PHONE \#
910 DATA TONY BOD,415-555-8117
920 DATA MARY JAY,213-555-ø144
930 DATA MARY MMM,213-555-1212
940 DATA JUDY WIL,112-555-@\varnothing75
950 DATA ADAM OZ,415-555-1667
960 DATA BOBBY ALL,312-555-1667
970 DATA END,999

```
38. Modify your program in frame 37 so that the computer will print telephone numbers and names located in area code 415 (you are going there for a visit and want to call old friends).
```

RUN
415-555-8117 TONY BOD
415-555-2222 ADAM OZ
ERROR- 6 AT LINE 4\varnothing

```
1 REM ** TELEPHONE DIRECTORY
\(1 \varnothing\) DIM D\$(8),T\$(12)
2ø RESTORE
30 READ D\$,T\$: IF T\$(1,3)<>"415" THEN 3ø
\(4 \varnothing\) PRINT T\$,D\$:GOTO 3ø
\(9 \varnothing \varnothing\) REM ** DATA: NAME, PHONE *
\(91 \varnothing\) DATA TONY BOD,415-555-8117
92ø DATA MARY JAY, \(213-555-\varnothing 144\)
\(93 \%\) DATA MARY MMM, 213-555-1212
\(94 \varnothing\) DATA JUDY WIL,112-555-Øø75
950 DATA ADAM OZ,415-555-1667
960 DATA BOBBY ALL, 312-555-1667
\(97 \varnothing\) DATA END,999
39. Sometimes we need to know the length of the contents of a string variable (how many characters). And, of course, BASIC has a special function, LEN, to help you find the answer. LEN(A\$) will tell you the number of characters including blanks in the string \(\mathrm{A} \$\). Here are some examples.
```

1\varnothing LET A = LEN(A$)
2\emptyset PRINT LEN(C$)
3\varnothing IF LEN(A$)<>LEN(B$) . . .

```

You can use the substring specifier to check answers to questions, to "edit" responses, and a host of other things. Below is a portion of a history teaching program. The program asks a question, requests a user response, and then checks the answer and makes an appropriate remark.
```

1\varnothing DIM A$(3\varnothing)
20 PRINT "WHO WAS THE FIRST PRESIDENT OF
THE U.S."::INPUT A$
30 FOR X=1 TO LEN(A$)-9
4\varnothing IF A$ ( }x,q+x)=\mp@subsup{}{}{\prime\prime}WASHINGTON" THEN PRIN
"CORRECT":END
5% NEXT X
6\varnothing PRINT "YOUR ANSWER IS WRONG"
7\varnothing GOTO 2\varnothing
RUN
WHO WAS THE FIRST PRESIDENT OF THE U.S.?

```

If you answer GEORGE WASHINGTON, what will the computer respond?

CORRECT. To see how the computer checks through your response, add this line and RUN the program with the same input response.

39 PRINT \(A \$(X, X+9)\)
40. Using the program in frame 39, if the user answered WASHINGTON IRVING to the question, what will the computer print? \(\qquad\)

CORRECT (We only tested for WASHINGTON. Think of what might happen if we only tested for WASH-even WASHING MACHINE would qualify for a correct answer!)
41. The LEN function can be used to "edit" data entered by users that might have to be a certain size, and no bigger because of forms you use or because of the size of your computer memory. Examine the example below and answer the questions which follow.
```

1\varnothingDIM A$(3\varnothing),N$(3\emptyset)
2\varnothing PRINT "YOUR NAME";:INPUT N\$
3\varnothing IF LEN(N$)>2\varnothing THEN PRINT "LIMIT YOUR
NAME TO 2\varnothing CHARACTERS PLEASE":GOTO 2\varnothing
4\varnothing PRINT "YOUR ADDRESS";:INPUT A$
5ø IF LEN(A\$)>15 THEN PRINT "PLEASE ABBR
EVIATE YOUR ADDRESS":GOTO 30

```

How many characters are allowed for name? \(\qquad\) For address? \(\qquad\)

\footnotetext{
- - - - - - - - -
}

20; 15

\section*{SELF-TEST}

Try this Self-Test, so you can evaluate how much you have learned so far.
1. Write a program to permit INPUT of a 5-letter word and then print the word backwards.
2. Write a program to read a series of 4-letter words from DATA statements and print only those words that begin with the letter A.
3. Modify the program in question 2 to print only words that begin with \(\mathbf{A}\) and end with S.
4. Some years ago, the auto industry was hard-pressed to come up with names for new cars. They used a computer to generate a series of 5 -letter words. Write a program to generate 1005 -letter words with randomly selected consonants in the first and third and fifth places and randomly selected vowels in the second and fourth places.

\section*{Answers to Self-Test}
```

1. 1ヵ REM ** STRING SELF-TEST 9-1
2ø DIM A$(5)
30 INPUT AS
4\varnothing FOR X=5 TO 1 STEP - 1
5\varnothing PRINT A$( }X,X)\mathrm{ ;
6\varnothing NEXT X
7\varnothing PRINT :GOTO 3\varnothing
2. 1\varnothing REM ** STRING SELF-TEST 9-2
3. DIM A$(4)
3\varnothing READ A$:IF A$(1,1)<>"'A" THEN 3\varnothing
40 PRINT A$:GOTO 3\varnothing
50 DATA ANTS,GNAT,LOVE,BALD,APES
6\emptyset DATA BAKE,MIKE,KARL,BARD,ALAS
4. 1\varnothing REM ** STRING SELF-TEST 9-3
20 DIM AS(4)
30 READ A$:IF A$(1,1)<>"'A" THEN 3\varnothing
35 IF A$(4,4)<>"S" THEN 3\varnothing
4\varnothing PRINT A$:GOTO 3ø
50 DATA ANTS,GNAT,LOVE,BALD,APES
6\varnothing DATA BAKE,MIKE,KARL,BARD,ALAS
5. 1\varnothing REM ** STRING SELF-TEST 9-4
2\varnothing DIM A$(5),B$(21)
3\varnothing A$="AEIOU"
4ø B$="BCDFGHJKLMNPQRSTVWXYZ"
50 FOR X=1 TO 2\varnothing
60 FOR Z=1 TO 2
7\varnothing B=INT(21*RND(1))+1
8\varnothing PRINT B$(B,B);
9\varnothing A=INT(5*RND(1))+1
1\varnothing\varnothing PRINT A$(A,A);
110 NEXT Z
12ø B=INT(21*RND(1))+1
13\varnothing PRINT B\$(B,B)
14\varnothing NEXT X
```

\section*{CHAPTER TEN}

\section*{Color Graphics and Sound}

In this chapter we introduce one of the most exciting capabilities of the ATARI computer. You will learn to control the color of the objects that appear on the video screen and also the color of the background on which the objects appear. In addition, you will learn to "paint" pictures which you have designed yourself. Several new graphic and color statements and commands will aid these enhancements to the output of your programs. When finished with this chapter, you will be able to:
- change the background color of the video screen to any one of 16 colors;
- draw designs on the video screen using any one of 16 colors;
- print text along with your pictures in a special text 'window';
- change the color of the text window to any one of 16 colors;
- change the number of plotting positions so that pictures can be drawn in more detail.
1. You can draw lines on the screen by selecting a screen mode that allows graphics to be mixed with text in several different ways. This is done by giving the GRAPHICS command (which may be abbreviated GR.). Eight different modes are provided. They are selected by a number 0-7. For example:
\(1 \varnothing\) GR. 3
would select a 40 column by 20 row graphics grid with provision for 4 lines of text.
(a) What command provides for drawing graphics?
(b) What is it's abbreviation? \(\qquad\)
(c) How many different screen modes are there? \(\qquad\)

(a) GRAPHICS
(b) GR. (Yes, the period is necessary!)
(c) eight (0 through 7)
2. Type in the following and examine the video screen.
```

GRAPHICS 3

```
(a) Did the top part of the screen change color?
(b) What color is the bottom portion of the screen?
(a) yes, it blanked the top portion-no color now.
(b) purple (this may vary with different TV sets)
3. In graphics mode 3, the top portion of the screen provides for a \(40 \times 20\) grid for plotting points. The smaller portion at the bottom is provided for printing text material. Four lines of text can be used.
(a) Where do you plot points on the screen in graphics mode 3?
(b) In what area may text be printed?
- - - - - - - - -
(a) in the top area of the screen
(b) in the bottom area
4. You have been using graphics mode zero (GRAPHICS 0) throughout the book so far. When your ATARI is turned on, the screen mode is automatically set to GRAPHICS 0 . When answering the following question, remember that mode 3 (GRAPHICS 3 or GR. 3) allows for 4 lines of text below the graph area. Enter and run the following program. When you have finished, type :
GRAPHICS 0 and press the RETURN key. This returns you to the text mode.
```

1\varnothing GRAPHICS 3
2\varnothing PRINT "LINE 1"
3\varnothing PRINT "LINE 2"
4\varnothing PRINT "LINE 3"
5\emptyset PRINT "LINE 4";
6』 GOTO 6』

```

What can you read at the bottom of the screen?
```

-     -         -             -                 -                     -                         -                             -                                 - 

LINE 1
LINE 2
LINE 3
LINE 4*

```
5. Here is a table of the graphic screen modes 3 through 7 .
\begin{tabular}{cccc} 
MODE & NUMBER OF & GRAPHIC POSITIONS & TEXT \\
NO. & COLUMNS & ROWS & WINDOW \\
3 & 39 & 20 & 4 lines \\
4,5 & 79 & 40 & 4 lines \\
6,7 & 158 & 80 & 4 lines
\end{tabular}

Which graphic mode(s) provide(s) the largest number of graphic positions?

6 and 7 ( \(158 \times 80\) positions)
6. Change line 10 in the program given in frame 4 to
```

1\varnothing GRAPHICS 4

```

If you run this revised program, will there be more room for text?
7. When we are using graphics, we use the PLOT statement to tell the computer what point we want plotted. Both the column and the row desired must be given in the PLOT statement. The screen positions are numbered from the upper-left corner of the screen starting with the number zero (0). Thus, the position 2,5 would be the third position to the right \((0,1,2)\) and the sixth position down ( \(0,1,2,3,4,5\) ). Suppose we execute the statement:
```

30 PLOT 2,5

```

Here is a sketch of the point plotted.


What does the PLOT statement tell the computer to do?

It tells the computer to plot a point at a stated position (column, row).
8. Examine this program
```

10 GR. 3
2ø PLOT 2,5
$3 \varnothing$ PRINT "THIS IS PLOT POSITION 2,5"

```

What does each line in the program tell the computer to do?
(a) Line 10 sets \(\qquad\)
(b) Line 20 tells where \(\qquad\)
(c) Line 30 \(\qquad\)
(a) Line 10 sets the graphic mode for a \(39 \times 20\) grid.
(b) Line 20 tells where to plot the point.
(c) Line 30 tells what message to print in the text window.
9. To see the point, we select a set of colors with the statement:
\[
15 \text { COLOR } 1
\]

Insert this line into the program of frame 8 and run the program.
(a) Did you see the point? \(\qquad\)
(b) If line 20 is changed to PLOT 10,5 , would the point plotted be to the right or would it be below our original point? \(\qquad\)
\(\qquad\)
(a) yes, the point 2,5 is plotted in gold.
(b) to the right.
10. To return from GR. 3 to the text mode: Type GR.0, then write a program to plot the four points shown below. Use GRAPHICS 3 and COLOR 1.
(1) 5,5
(2) 15,5
(3) 5,15
(4) 15,15

Our program:
```

10 GR. 3
20 COLOR 1
30 PLOT 5,5: PLOT 15,5
4ø PLOT 5,15: PLOT 15,15

```

We are using multiple statements per line.
11. When your program is run, which plotted point \((1,2,3\) or 4\()\) is:
(a) at the upper left? \(\qquad\)
(b) at the lower right? \(\qquad\)
(c) at the upper right? \(\qquad\)
(d) at the lower left? \(\qquad\)
- - - - - - - - -
(a) \(1(5,5)\)
(b) \(4(15,15)\)
(c) \(2(15,5)\)
(d) \(3(5,15)\)
12. Complete the program below to put a point in each corner of the graphics area, using graphics mode 3. Remember, rows and columns start numbering with zero (0). Consult the table in frame 5 . Type GR. 0 to return to fullscreen text. Enter and try your completed program.
```

1% GR. 3
2% COLOR 1
3\varnothing PLOT \varnothing,\varnothing: PLOT

```
\(\qquad\)
```

4\varnothing PLOT \varnothing,19: PLOT

```
\(\qquad\)
```

_ - - _ - - - _ -
3\varnothing PLOT \varnothing, \varnothing: PLOT 38,19
4\varnothing PLOT }\varnothing,19: PLOT 38,\varnothing

```
13. According to the table in frame 5 , graphics modes 4 and 5 provide \(79 \times 40\) points. This gives us 79 columns ( 0 through 78 ) and 40 rows ( 0 through 39 ).

Since the columns and rows are numbered from zero, the upper right hand corner of the screen would be plotted by the statements:
```

1\varnothing GR. }
2\varnothing COLOR 1

```
\(3 \varnothing\) PLOT
\(\qquad\) ,
\(3 \varnothing\) PLOT 78, \(\varnothing\)
14. Write a program, using graphics mode 6 , that will place a point in each corner of the graphic area for this mode. Refer to frame 12 to see how it was done for mode 3 .

\section*{- - - - - - -}

Our sample program:
```

1\varnothing GR. 6
20 COLOR 1
3\varnothing PLOT \varnothing,\varnothing: PLOT 157,79
4ø PLOT ø,79: PLOT 157,\varnothing

```
15. Type GRAPHICS 0 to return to the text mode. Type NEW, enter and run the program below. Then draw a sketch of the result. Type GRAPHICS 0 when your sketch is finished to return to the text mode.
```

1\emptyset GRAPHICS 3
2\emptyset COLOR 1
3\varnothing PLOT \varnothing,\varnothing: PLOT 1,1: PLOT 2,2
40 PLOT 3,3: PLOT 4,4: PLOT 5,5
5\emptyset PLOT 6,6: PLOT 7,7: PLOT 8,8
6\varnothing PLOT 9,9: PLOT 1\varnothing,1\varnothing: PLOT 11,11
70 PLOT 12,12: PLOT 13,13: PLOT 14,14
8\emptyset PLOT 15,15: PLOT 16,16: PLOT 17,17
90 PLOT 18,18: PLOT 19,19

```

16. You can also use a FOR-NEXT loop to plot points. Type NEW, enter and run the following:
```

1\varnothing GRAPHICS 3
2\varnothing COLOR 1
3\varnothing FOR I=\varnothing TO 19 STEP 2
4 PLOT I,I
5\emptyset NEXT I

```

How do the results of this run compare with that of frame 14 ?

The results are the same.
17. A third way to plot a straight line is to use the DRAWTO statement along with the PLOT statement. The PLOT statement tells the computer where to start the line, and the DRAWTO statement gives the position where the line will end. The line is drawn from the PLOT position to the DRAWTO position.

Enter and run this program.
\(1 \varnothing\) GR. 3
\(2 \varnothing\) COLOR 1
\(3 \varnothing\) PLOT \(\varnothing, \varnothing\)
\(4 \varnothing\) DRAWTO 19,19
Complete these statements.
(a) The PLOT statement tells the computer to
\(\qquad\) -.
(b) The DRAWTO statement tells the computer to
\(\qquad\)
(c) Compare the results of this program with those in frames 15 and 16.
——————————
(a) start the line at the position given.
(b) end the line at the position given.
(c) the same
18. Complete this program which will draw a line from the top left to the lower right of the graphics area. Use graphics mode 4.
```

1\varnothing GR. }
2ø COLOR 1
3\varnothing PLOT \varnothing.\varnothing
40

```
\(\qquad\)
```

------_-_-
4\varnothing DRAWTO 78,39

```
19. After running the program in frame 18, the screen should look similar to this sketch.


Now, add two lines to the program of frame 18 so that a second line will be drawn from the upper right corner to the lower left corner. A very large \(\mathbf{X}\) should now be displayed as in this sketch.


Complete these lines and add them to the program of frame 18.
```

50 PLOT

```
\(\qquad\)
6』 DRAWTO \(\qquad\)
```

_ - - - - - - _ -

```
50 PLOT \(78, \varnothing\)
\(6 \varnothing\) DRAWTO \(\varnothing, 39\)
20. Add another line to the same program so that the text window will say : X MARKS THE PLOT.
\(\qquad\)
70
\(\ldots-\ldots-\ldots-\ldots\)
\(7 \varnothing\) PRINT " \(X\) MARKS THE PLOT"
21. Given the following program, draw a sketch of the results which will appear on the screen.
```

1\varnothing GRAPHICS 4
2ø COLOR 1
3\varnothing FOR N= 39 TO Ø STEP-13
4\varnothing PLOT \varnothing,\varnothing
5\emptyset DRAWTO 78,N
6\varnothing NEXT N

```

22. Add or change these lines to the program of frame 21. After running the program, press the BREAK key to stop. Then type 'GRAPHICS 0' to return to the text mode as before.
\begin{tabular}{llll} 
Add & 15 & FOR \(M=\varnothing\) TO 1 \\
Change & \(2 \varnothing\) & COLOR \(M\) \\
Add & \(7 \varnothing\) & NEXT \(M\) \\
Add & \(8 \varnothing\) & GOTO 15
\end{tabular}

How do these changes effect the result? \(\qquad\)
- - - - - - - - -

You can see each line being drawn and 'erased' repeatedly.
23. Now that you can use graphics with color, let's see how we can change the colors. We select a color with the statement:
```

SETCOLOR \varnothing,C,2

```

The variable \(C\), can be any integer from 0 through 15 . Each value for \(C\) will give us a different color for the plotted points.
The statement used to change color points on the screen is
\(\qquad\) _.

SETCOLOR \(\varnothing, C, 2\)
24. A complete color graphics program must have the three statements: GRAPHICS, COLOR, and SETCOLOR. Of course, we must also plot some points.
```

1% GR. 3
2ø COLOR 1
3\varnothing SETCOLOR \varnothing, \varnothing,2
4\varnothing PLOT \varnothing, 3
50 DRAWTO 38,3
6\varnothing PRINT "WHAT COLOR DO YOU SEE?"

```

Examine the program before you run it. What do you think will appear on the screen
(a) in the graphics area? \(\qquad\)
(b) in the text area? \(\qquad\)
(c) Run the program to confirm your answers to (a) and (b).
— - - - - - - - -
(a) a long grey color bar (color may vary for your TV).
(b) The words: What color do you see?
(c) We trust your answers were correct. If not, you have learned something new.
25. A few changes and additions will convert the program of frame 24 to show each of the 16 colors available. The colors are changed by the values of the variable in the SETCOLOR statement in line 30.
(a) Complete the program
\begin{tabular}{ll} 
& \(1 \varnothing\) GR. 3 \\
& \\
& \(2 \varnothing\) COLOR 1 \\
25 & \\
& 25 FOR N \(=\varnothing\) TO 15
\end{tabular}
\(\begin{array}{ll}\text { Change } & 3 \varnothing \text { SETCOLOR } \varnothing, \\ & 4 \varnothing \text { PLOT } \varnothing, 3 \\ & 5 \varnothing \text { DRAWTO } 38,3\end{array}\)
Change 60 FOR \(W=1\) TO 500: NEXT
Add \(7 \varnothing\) PRINT: PRINT: PRINT: PRINT \(N\)
Add \(8 \varnothing\) NEXT \(\qquad\)
(b) Describe what happens when you run the program.
(a) \(3 \varnothing\) SETCOLOR \(\varnothing, N, 2\)
\(6 \varnothing\) FOR \(W=1\) TO \(5 \varnothing \varnothing\) : NEXT \(W\)
8 Ø NEXT N
(b) The color bar varies from grey through green with several shades of the same color.
26. You have just observed the 16 colors available on your ATARI. They were demonstrated by changing the color of the bar in the graphics area. We will now try a variation. You decide what happens on the screen.

Change line 30 in the program of frame 25 to:
\(3 \varnothing\) SETCOLOR 2,N,2
Run this revised program and describe what happens.
- - - - - - - - -

The color bar is gold throughout the run, but the color of the text window goes through the 16 colors.
27. One more variation can be observed by changing line 30 once more.

Change line 30 to:
\(3 \varnothing\) SETCOLOR \(4, N, 2\)
Run the program again with this change. Describe the new results.
\(\qquad\)
\(\qquad\)
- - - - - - - - -

This time, the background of the graphics area changes. The bar remains gold, and the text window turns dark and remains dark.
28. In frames 25,26 , and 27 , we varied the values for the variables A and N in the statement: SETCOLOR A,N,2.
(a) When A was set to 0 where, on the screen, were the colors varied?
(b) When A was set to 2 , where were the colors varied?
(c) When A was set to 4, where were the colors varied?
(a) The plotted bar
(b) The text window
(c) The background of the graphics area
29. The effects shown in frames 25,26 , and 27 can all be shown in one program.
(a) Fill in the missing blanks in lines 60, 80, 90 and 100.
```

10 GR. 3
2ø COLOR 1
3ø PRINT "WATCH MY COLORS CHANGE!!!"
4\varnothing FOR M = \varnothing TO 4 STEP 2
5ø FOR N = \varnothing TO 15
6% SETCOLOR
7\varnothing PLOT 5,5: DRAWTO' 3^,5
80 FOR W = 1 TO 200: NEXT _
9\varnothing NEXT

```
\(\qquad\)
```

1\varnothing\varnothing NEXT ___

```
(b) Briefly describe the results.
\(\qquad\)
\(\qquad\)
(a) 60 SETCOLOR \(M, N, 2\) \(8 \varnothing\) FOR \(W=1\) TO \(2 \varnothing \varnothing:\) NEXT \(W\) \(9 \varnothing\) NEXT N \(1 \varnothing\) NEXT M
(b) First the color bar varies through 16 colors, then the text window varies through 16 colors, and finally the background of the graphics area varies through 16 colors.
30. You can now plot points and create many colors on the video screen. Here is a program that combines both. Before you run the program, see if you can show where the points will be plotted. Shade the points in on the grid which is provided beside the program.

Plot the points that you think will be colored on this grid.
```

1\varnothing GR. 3
2\varnothing COLOR 1
30 SETCOLOR 4,1,2
4ø PLOT 5,5: DRAWTO 7.5
5ø PLOT 6,6: DRAWTO 6,1\varnothing
60 DRAWTO 4,15
7ø PLOT 6,1ø: DRAWTO 8,15
8\varnothing PLOT 5,7: DRAWTO 3,9
9ø PLOT 7,7: DRAWTO 9,9
1\varnothing\varnothing PRINT "WHAT A FUNNY MAN!!!"

```


31. By changing the screen modes, we can change the size of the figure "drawn" in frame 30. Make these changes and additions to the program of frame 30.

Add \(\quad 5\) FOR \(A=7\) TO 3 STEP-2
Change \(1 \varnothing\) GRAPHICS \(A\)
Add \(\quad 93\) FOR \(W=1\) TO 2ø0: NEXT \(W\)
Add 95 NEXT A
(a) Run the revised program and describe the results.
\(\qquad\)
\(\qquad\)
(b) How many screen modes were used? \(\qquad\)
- - - - - - - -
(a) The man appears to move from the upper left corner, and his size increases. (b) 3
32. The program of frame 31 changed the graphics mode from many small divisions, to fewer very large divisions. Pictures can be drawn in more detail when many smaller points are used rather than larger points. In the program of frame 31,
(a) Which statement caused the change in graphics mode? \(\qquad\)
(b) The first value used for the variable A in the FOR-NEXT loop was
\(\qquad\) , the second value was \(\qquad\) and the third value was
\(\qquad\) .
\(\qquad\)
(a) Line \(1 \varnothing\) GRAPHICS A
(b) first value \(=7\), second value \(=5\), third value \(=3\)
33. The table in frame 5 shows the number of graphics positions for the screen modes. Modes 6 and 7 have \(158 \times 80\), or 12,640 individual points. Modes 4 and 5 have \(79 \times 40\), or 3,160 points. Mode 3 has \(39 \times 20\), or 780 points. This program will allow you to examine some rectangles in the three sizes.
```

1ø GRAPHICS 7
2\varnothing COLOR 1
3\varnothing SETCOLOR \varnothing,15,2
35 X = 80:Y = 48
40 PLOT X,Y
50 PLOT X-2,Y-2: DRAWTO X+2,Y-2
6\emptyset DRAWTO X+2,Y+2: DRAWTO X-2,Y+2
7\varnothing DRAWTO X-2,Y-2
8\emptyset PLOT X-4, Y-4: DRAWTO. X+4,Y-4
9@ DRAWTO X+4,Y+4: DRAWTO X-4,Y+4
1\varnothing\varnothing DRAWTO X-4,Y-4

```

First run the program and notice the width of the lines that were drawn and the size of the rectangle.

Second, change line 10 to: \(1 \varnothing\) GRAPHICs 5
and line 35 to: \(35 \quad x=40: \quad Y=24\).
Run the program again and compare the line width and rectangle size to your first run.

Third, change line 10 to: \(1 \varnothing\) GRAPHICS 3
and line 35 to: \(35 \quad \mathrm{X}=2 \varnothing\) : \(\mathrm{Y}=12\).
Run the program again.
(a) How did the line width change for runs 1,2 , and 3 ?
(b) How did the rectangle size change?
- - - - - - - - -
(a) It got wider each time.
(b) It got larger each time.
34. You can create an interesting visual effect by combining the three graphics modes in one program. Our revised program looks like this.
```

1\varnothing M = 1
2\emptyset FOR N = 7 TO 3 STEP-2
30 GRAPHICS N
40 COLOR 1
5\varnothing SETCOLOR Ø,1,2
60 X = 80/M: Y = 48/M
7\varnothing PLOT X,Y
8\varnothing PLOT X-2,Y-2: DRAWTO X+2,Y-2
9\varnothing DRAWTO }X+2,Y+2: DRAWTO X-2,Y+
1\varnothing\varnothing DRAWTO X-2,Y-2
11\varnothing PLOT X-4,Y-4: DRAWTO X+4,Y-4
12\varnothing DRAWTO }X+4,Y+4: DRAWTO X-4,Y+
130 DRAWTO X-4,Y-4
14ø FOR W = 1 TO 2ø\varnothing: NEXT W
150 M = 2*M
160 NEXT N
17\varnothing GOTO 1\varnothing

```

Before you run the program:
(a) Which line would allow you to change the rectangle's color? \(\qquad\)
(b) What key would you press to stop the program?
(c) Which line would let you vary the time that each graphics mode stays on the screen? \(\qquad\)
```

-     -         -             -                 -                     -                         -                             -                                 - 

```
(a) line 50
(b) BREAK
(c) line 140
35. You now have color graphics under control, so we'll move on to the discovery of sound. Four variables are used with the SOUND statement. We'll call them V (for Voice), N (for Note), T (for Tone), and L (for Loudness).
\(2 \varnothing\) SOUND \(\mathrm{V}, \mathrm{N}, \mathrm{T}, \mathrm{L}\)
In the line (20) above, tell what each variable represents.
(a) \(\quad \mathrm{V}=\) \(\qquad\)
(b) \(\mathrm{N}=\) \(\qquad\)
(c) \(\mathrm{T}=\) \(\qquad\)
(d) \(\mathrm{L}=\) \(\qquad\)
(a) \(\mathrm{V}=\) voice
(b) \(\mathrm{N}=\) note
(c) \(\mathrm{T}=\) tone
(d) \(\mathrm{L}=\) loudness
36. Enter and use this two-line program to adjust the volume of your TV set to a reasonable level. Press the BREAK key when you have the volume adjusted satisfactorily.
```

1\varnothing SOUND \varnothing,115,1\varnothing,8
2\varnothing GOTO 2\varnothing

```

Tell what each value used with the SOUND statement represents.
(a) 8
(b) 115 \(\qquad\)
(c) 0
(d) 10
- - - - - - - - -
(a) \(8=\) loudness
(b) \(115=\) note
(c) \(0=\) voice
(d) \(10=\) tone
37. We'll experiment with loudness first. Values for the variable \(L\) may be any integer from 0 through 15 . Using 0 for voice, 115 for note, and 10 for tone, write a program to generate all 16 sound levels. Use an INPUT statement for L. Insert a statement: IF \(L=-5\) THEN \(\qquad\) to shut the sound off when finished.
```

Our program:* $1 \varnothing$ input L $2 \varnothing$ IF L $=-5$ THEN $5 \varnothing$ $3 \varnothing$ SOUND $\varnothing, 115,1 \varnothing, L$ $4 \varnothing$ GOTO 1ø 50 END

```
* note: it may be done in other ways.
38. In the program of frame 37, each sound level will keep playing until a new input is received. Write a new program that uses a time delay to keep the note playing for a reasonable length of time. Use a FOR-NEXT loop to change the level of loudness.

Our program: \(\quad 1 \varnothing\) FOR L \(=\varnothing\) TO 15
```

2ø SOUND \varnothing,115,1\varnothing,L
30 FOR W = 1 TO 2øø: NEXT W
4% NEXT L

```
39. For normal use, the loudness level can be left at 8 . Let's try the tone variable next. We have used a value of 10 so far. The variable N may range from 0 through 15. Write a revision of our program of frame 38 so that T (tone) will be varied. Set the loudness level at 8 .
\(-\ldots-\ldots-\ldots-\ldots\)

Our revised program: \(\quad 1 \varnothing\) FOR \(T=\varnothing\) TO 15
\(2 \varnothing\) SOUND \(\varnothing, 115, T, 8\)
30 FOR \(W=1\) TO 200: NEXT \(W\)
\(4 \varnothing\) NEXT T
40. Would you care to describe the sounds produced by the last program?
\(\qquad\)
\(\qquad\)
_ - - - - - - - -
I heard a couple of nice sounding tones, some funny noises, and some nice quiet.
41. Now let's put the tone back to 10 , leave the loudness at 8 , and stay with voice 0 . This time we'll vary the note. The values used may range from 0 through 255. Shorten the time delay of the program of frame 39 to 50 and re-write the program to vary the notes.

Our program: \(\quad 1 \varnothing\) FOR \(N=\varnothing\) TO 255 \(2 \varnothing\) SOUND \(\varnothing, N, 1 \varnothing, 8\) \(3 \varnothing\) FOR \(W=1\) TO 5ø: NEXT \(W\) \(4 \varnothing\) NEXT N
42. If you were writing a song, you probably wouldn't need all those 256 notes. Here is a table of values we will use that covers two and one-half octaves (when tone is set to 10 ).
\begin{tabular}{|l|l|}
\hline N & Note \\
\hline 26 & \(\mathrm{D} \#\) \\
27 & D \\
29 & \(\mathrm{C} \#\) \\
31 & C \\
32 & B \\
34 & \(\mathrm{~A} \#\) \\
36 & A \\
38 & \(\mathrm{G} \#\) \\
41 & G \\
43 & \(\mathrm{~F} \#\) \\
46 & F \\
48 & E \\
51 & \(\mathrm{D} \#\) \\
54 & D \\
58 & \(\mathrm{C} \#\) \\
& \\
\hline
\end{tabular}
\begin{tabular}{|c|l|}
\hline N & Note \\
\hline 61 & C \\
65 & B \\
69 & A\# \\
73 & A \\
77 & \(\mathrm{G} \#\) \\
82 & G \\
86 & \(\mathrm{~F} \#\) \\
92 & F \\
97 & E \\
103 & \(\mathrm{D} \#\) \\
109 & D \\
115 & \(\mathrm{C} \#\) \\
122 & C \\
129 & B \\
137 & \(\mathrm{~A} \#\) \\
145 & A \\
\hline
\end{tabular}
(a) From the results of the program in frame 41, which value of the note table gives the highest note? \(\qquad\)
(b) Which gives the lowest? \(\qquad\)
(a) 26
(b) 145
43. To play a musical scale, we can store notes in a table and read them in when we need them.

Fill in the data values in this program. Do NOT use sharps (\#). Start with the lowest note shown in the table in frame 42.
```

1\varnothing FOR A = 1 TO 16
2ø READ N
3ø SOUND \emptyset,N,1\varnothing,8
4\varnothing FOR W = 1 TO 2\varnothing\varnothing: NEXT W
5\varnothing SOUND \varnothing, \varnothing,1\varnothing,8
6\varnothing FOR W = 1 TO 1\varnothing: NEXT W
7\varnothing NEXT A

```
\(8 \varnothing\) DATA
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)

90 DATA \(\qquad\) , , \(\qquad\) , ,
\(\qquad\) , ,

80 DATA \(145,129,122,109,97,92\)
90 DATA \(82,73,65,61,54,48\)
100 DATA 46,41,36,32
44. To make color and sound work together, add these lines to the program of frame 43.
```

5 GR. 5
15 COLOR 1
34 SETCOLOR \varnothing,A-1,2
35 PLOT 5,11,: DRAWTO 15,11

```
(a) When you run this program, how many notes will be played? \(\qquad\)
(b) How many colors will be displayed? \(\qquad\)
- - - - - - - - -
(a) 16
(b) 16
45. Cold is blue, and warm is red. Complete this program to play 8 notes.

Display warm colors with high notes and cold colors with low notes. Use these colors:
\begin{tabular}{ll} 
dark purple & yellow-green \\
blue & yellow \\
blue-green & orange \\
green & red
\end{tabular}

Put both NOTE and COLOR in the data statements.
```

1\varnothing GR. 3
20 FOR A = 1 TO 8
30 COLOR 1
4% READ N,C
5\varnothing SETCOLOR \varnothing,
_,
6\varnothing PLOT 1\varnothing,9-A: DRAWTO 2\varnothing,9-A
7\varnothing SOUND \varnothing,_,_1\varnothing,8
8\emptyset FOR W = 1 TO 2ø\varnothing: NEXT W
9\varnothing SETCOLOR \varnothing, },
1\varnothing\varnothing SOUND \varnothing,\varnothing,1\varnothing,8
11\varnothing FOR W = 1 TO 1\varnothing: NEXT W
120 NEXT A
130 DATA

```
\(\qquad\)
``` , ,
``` \(\qquad\)
```

14\varnothing DATA ________________
150 DATA

```
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)
\(\qquad\)

Our choices, yours may vary.
```

5\varnothing SETCOLOR \varnothing,C,2
7\varnothing SOUND Ø,N,1\varnothing,8
13\emptyset DATA 122,9,1\varnothing9,1\varnothing
140 DATA 97,13,92,15
15\emptyset DATA 82,1 ,73,2
16\emptyset DATA 65,3,61,5

```
46. As your programming ability increases, the size of your programs also tend to increase. Long programs can be more easily written and understood if you break them up into functional parts. Often, you will find some of those functional parts being used at several places in your program. Rather than repeat them each time, a SUBROUTINE can be used. The GOSUB statement tells the computer to leave your main program and go to the subroutine. When the subroutine has been finished, a RETURN statement in the subroutine tells the computer to go back to the main program to the line that follows the GOSUB statement.

Here is a short program to demonstrate the use of the GOSUB and
RETURN statements. Try it on your computer.
```

10 N = 122
2\varnothing GOSUB 1\varnothing\varnothing
3\varnothingN = 109
4\varnothing GOSUB 1\varnothing\varnothing
50 N=97
6\varnothing GOSUB 1ø\varnothing
70 END
1\varnothing\varnothing SOUND \varnothing,N,1\varnothing,8
11\varnothing FOR W = 1 TO 2\varnothing\varnothing: NEXT W
12\varnothing SOUND \varnothing,\varnothing,1\varnothing,8
13\varnothing FOR W = 1 TO 1\varnothing: NEXT W
14\emptyset RETURN

```
(a) Which lines contain the subroutine?
(b) How many times is the subroutine used? \(\qquad\)
(c) How many notes are played? \(\qquad\)
(a) \(100,110,120,130,140\)
(b) 3
(c) 3
47. Here is a program that uses "nested subroutines." At line 110 subroutine 1000 is called. At line 1020 in the first subroutine, subroutine 2000 is called.
Subroutine 2000 returns from line 2010 to line 1030 of the first subroutine. Then the program goes back to the main program. The program below plays a oneoctave scale and plots the notes on the video screen in color.
```

1\varnothing GR. }
20 COLOR 1
3\varnothing SETCOLOR 1,1\varnothing,2
40 FOR N = 5 TO 13 STEP 2
5\varnothing PLOT \varnothing,N: DRAWTO 38,N
60 PLOT Ø,15: DRAWTO 35,15
7\varnothing PLOT 3\varnothing, 15: DRAWTO 35,15
8\varnothing GOSUB 2\varnothing\varnothing\varnothing
90 SETCOLOR 4,4,2
10\varnothing COLOR 2
11\varnothing X=3: Y=15: N=122: GOSUB 1\varnothing\varnothing\varnothing
12\varnothing X=5: Y=14: N=1\varnothing9: GOSUB 1ø\varnothing\varnothing
130 X=7: Y=13:N=97: GOSUB 100\varnothing
14\varnothing X=9: Y=12: N=92: GOSUB 1øø\varnothing
15\varnothing X=11: Y=11: N=82: GOSUB 10ø\varnothing
160 X=13: Y=10: N=73: GOSUB 10\varnothing0
170 X=15: Y=9:N=65: GOSUB 1ø\varnothing\varnothing
18\varnothing X=17: Y=8:N=61: GOSUB 1ø\varnothing\varnothing
19\varnothing END
1\varnothingD\varnothing PLOT X,Y
1\varnothing1\varnothing SOUND \varnothing,N,1\varnothing,8
1ø2\varnothing GOSUB 2ø\varnothing\varnothing
1ø3\varnothing RETURN
2000 FOR W= 1 TO 200: NEXT W
2ø1\varnothing RETURN

```

Replace line 190 and add lines which will come back down the scale in sound and plot the notes. (Our program only plays from low to high.)

One way to do it:
```

19\varnothing X=15: Y=9: N=65: GOSUB 1\varnothing\varnothing\varnothing
2\varnothing\varnothing X=13: Y=1\varnothing:N=73: GOSUB 1\varnothing\varnothing\varnothing
21\varnothing X=11: Y=11:N=82: GOSUB 1\varnothing\varnothing\varnothing
22\varnothing X=9: Y=12:N=92: GOSUB 1\varnothing\varnothing\varnothing
230 X=7: Y=13:N=97: GOSUB 1\varnothing\varnothing\varnothing
24\varnothing X=5: Y=14:N=1\varnothing9: GOSUB 1\varnothing\varnothing\varnothing
25\varnothing X=3: Y=15:N=122: GOSUB 1\varnothing\varnothing\varnothing
260 END

```
48. Your ATARI sound system allows the use of four voices simultaneously by varying V in the sound statement:

SOUND \(V, N, T, L\)
We have only used one voice so far, but that is going to change now.
```

1\varnothingL\varnothing=8:L1=\varnothing
2\varnothingN\varnothing=41:N1=129
3\varnothing GOSUB 1\varnothing\varnothing\varnothing
4\varnothingL1=8: GOSUB 1\emptyset\emptyset\emptyset
5\varnothingL\varnothing=\varnothing: GOSUB 1\varnothing\varnothing\varnothing
6\varnothingL1=\varnothing: GOSUB 1\varnothing\varnothing\varnothing
7\varnothing STOP
1\varnothing\varnothing\varnothing SOUND \varnothing,N\varnothing,1\varnothing,L\varnothing
1\varnothing1\varnothing SOUND 1,N1,1\varnothing,L1
1\varnothing2\varnothing FOR W = 1 TO 1\varnothing\varnothing: NEXT W
1\varnothing3\varnothing RETURN

```
(a) How many notes will you hear when line 30 is executed? \(\qquad\)
(b) How many notes can be heard when line 40 is executed? \(\qquad\)
(c) How many notes can be heard when line 60 is executed? \(\qquad\)
(d) Which voice does line 50 turn off?
\(\qquad\)
(a) 1 since the loudness of voice 1 is set to zero.
(b) 2
(c) none
(d) voice 0
49. The following program demonstrates a simple tune with two voices. Three subroutines are used to play the notes for the proper length of time. Each line of the main program 'calls" a subroutine to play a pair of notes.
```

1\varnothingN\varnothing = 41:N1 = 129: GOSUB 2øøø
2ø N\varnothing = 32: N1 = 1ø9: GOSUB 1øøø
3\varnothingND = 27:N1 = 92: GOSUB 30.0
4\varnothingN\varnothing = 31:N1 = 97: GOSUB 2øø\varnothing
5ø N\varnothing = 32: N1 = 1ø9: GOSUB 1ø\varnothing\varnothing
60 N\varnothing = 36:N1 = 122: GOSUB 3000
7\varnothingN\varnothing = 41:N1 = 129: GOSUB 1ø\varnothing\varnothing
8\varnothingN\varnothing = 36: N1 = 122: GOSUB 1ø\varnothing\varnothing
9\varnothingN\varnothing = 32:N1 = 1ø9: GOSUB 1ø\varnothing\varnothing
1ø\varnothing N\varnothing = 36: N1 = 122: GOSUB 3øøø
11\varnothing N\varnothing = 27: N1 = 92: GOSUB 2øø\varnothing
12\varnothingN\varnothing = \varnothing: N1 = \varnothing: GOSUB 1\varnothing\varnothing\varnothing
13\varnothing N\varnothing = 41: N1 = 129: GOSUB 2øø\varnothing
14\varnothing N\varnothing = 32: N1 = 109: GOSUB 1\varnothing\varnothing\varnothing
15ø N\varnothing = 25:N1 = 92: GOSUB 30ø\varnothing
160 N\varnothing = 36:N1 = 122: GOSUB 2000
170 N\varnothing = 32: N1 = 109: GOSUB 1000
180 N\varnothing = 31:N1 = 97: GOSUB 1000
19ø N\varnothing = 32:N1 = 109: GOSUB 10ø\varnothing
2\varnothing\varnothing N\varnothing = 36: N1 = 122: GOSUB 1\varnothing\varnothing\varnothing
210 N\varnothing = 27: N1 = 92: GOSUB 2ø\varnothing\varnothing
22\varnothing N\varnothing = 41:N1 = 129: GOSUB 1\varnothing\varnothing\varnothing
230 Nø = 32: N1 = 109: GOSUB 2ø\varnothing\varnothing
24\varnothingN\varnothing = 36:N1 = 122: GOSUB 100\varnothing
250 N\varnothing = 41: N1 = 129: GOSUB 3000
26\varnothing GOSUB 1\varnothing\varnothing\varnothing
27ø GR. \varnothing
280 END

```

Fill in the missing blanks in the subroutines.
```

1\varnothing\varnothing\varnothing SOUND \varnothing,___________
1\varnothing1\varnothing SOUND 1,
____________
1ø2\varnothing FOR W = 1 TO 5\emptyset: NEXT W
1030
2ø\varnothing\varnothing SOUND \varnothing,_____________
2010 SOUND 1,___
-
2ø2\varnothing FOR W = 1 TO 1ø\varnothing: NEXT W
2ø3\varnothing
3øøø SOUND ø,
,________
3ø1\varnothing SOUND 1,
,_
,___ ,

``` \(\qquad\)
```

3ø2\varnothing FOR W = 1 TO 15\varnothing: NEXT W
3030
M
_ - - - - - _ _ -
1\varnothing\varnothing\varnothing SOUND \varnothing,N\varnothing, 1\varnothing,8
1\varnothing1\varnothing SOUND 1,N1,1\varnothing,8
1030 RETURN
2ø\varnothing\varnothing SOUND \varnothing,N\varnothing,1\varnothing,8
2ø1ø SOUND 1,N1,1\varnothing,8
2ø3\varnothing RETURN
3\varnothing\varnothing\varnothing SOUND \varnothing,N\varnothing,1\varnothing,8
3ø1ø SQUND 1,N1,1ø,8
303\varnothing RETURN

```
50. Change the subroutines in the last program so that graphics mode 3 is used. In subroutine 1000 plot a blue bar near the middle of the screen. For subroutine 2000 make the bar gold, and for subroutine 3000 make the bar red.

1011 \(\qquad\)
\(\qquad\)
\(\qquad\)
\(1 \varnothing 14\) \(\qquad\)
\(2 \not 211\) \(\qquad\)
2012 \(\qquad\)
2013 \(\qquad\)
3011 \(\qquad\)
3012 \(\qquad\)
3013 \(\qquad\)
3014 \(\qquad\)

1011 GR. 3
\(1 \not 12\) COLOR 1
\(1 \varnothing 13\) SETCOLOR \(\varnothing, 8,2\)
\(1 \varnothing 14\) PLOT ø,12: DRAWTO 5,12
2011 GR. 3
\(2 \not 212\) COLOR 1
\(2 \varnothing 13\) SETCOLOR \(\varnothing, 1,2\)
```

2.14 PLOT \varnothing,12: DRAWTO 1\varnothing,12

```
\(3 \varnothing 11\) GR. 3
\(3 \not 212\) COLOR 1
\(3 \varnothing 13\) SETCOLOR ø,4,2
\(3 \varnothing 14\) PLOT \(\varnothing, 12:\) DRAWTO 15,12
51. The next program will cover frames 51 to 55 . We will add some two, three, and four part harmony to our sound. The program is quite long so we'll break it up into several sections.

One of the voices plays a repeating background series of three notes.
Therefore, we have used three subroutines for the sound statements with each subroutine containing one of these background notes. In addition, the subroutines also contain the sound statements for two other voices. Since the subroutines are the most important part of the program, we'll look at them first.
```

```
1ø\varnothing\emptyset SOUND \varnothing, 183,1\varnothing,8
```

```
1ø\varnothing\emptyset SOUND \varnothing, 183,1\varnothing,8
1\varnothing1\varnothing SOUND 1,N1,1\varnothing,8
1\varnothing1\varnothing SOUND 1,N1,1\varnothing,8
1\varnothing2\varnothing SOUND 2,N2,1\varnothing,8
1\varnothing2\varnothing SOUND 2,N2,1\varnothing,8
1ø3\varnothing FOR W=1 TO 25: NEXT W
1ø3\varnothing FOR W=1 TO 25: NEXT W
1\varnothing4\varnothing RETURN
1\varnothing4\varnothing RETURN
2øø\varnothing SOUND Ø,137,1\varnothing,8
2øø\varnothing SOUND Ø,137,1\varnothing,8
2ø1ø SOUND 1,N1,1\varnothing,8
2ø1ø SOUND 1,N1,1\varnothing,8
2ø2\varnothing SOUND 2,N2,1\varnothing,8
2ø2\varnothing SOUND 2,N2,1\varnothing,8
2030 FOR W=1 TO 25: NEXT W
2030 FOR W=1 TO 25: NEXT W
204\varnothing RETURN
204\varnothing RETURN
3øø\varnothing SOUND \varnothing,145,1\varnothing,8
3øø\varnothing SOUND \varnothing,145,1\varnothing,8
3ø1\varnothing SOUND 1,N1,1\varnothing,8
3ø1\varnothing SOUND 1,N1,1\varnothing,8
3ø2\varnothing SOUND 2,N2,1\varnothing,8
3ø2\varnothing SOUND 2,N2,1\varnothing,8
303\varnothing FOR W=1 TO 25: NEXT W
303\varnothing FOR W=1 TO 25: NEXT W
3\varnothing4\varnothing RETURN
```

```
3\varnothing4\varnothing RETURN
```

```
first background note
voice 1 , note 1 ,tone,loudness
voice 2 , note 2 ,tone,loudness
time delay to hold notes on
second background note
voice 1 again
voice 2 again
hold the notes on again
third background note
voice 1
voice 2
hold the notes again

Each of these subroutines provides for playing a certain number of notes simultaneously for a given period of time.
(a) How many notes at one time? \(\qquad\)
(b) Which statements determine the time the note is played?
(a) 3
(b) the FOR-NEXT loops at lines 1030, 2030, and 3030.
52. Now let's look at the main beginning of the program, which sets up the notes to be played.
```

1\varnothing N1=\varnothing: N2=\varnothing: GOSUB 1\varnothing\varnothing\varnothing
2ø GOSUB 2000
30 GOSUB 3\varnothingø\varnothing
40 GOSUB 100\varnothing
50 GOSUB 2ø0\varnothing
6\varnothing N2=61:GOSUB 3ø\varnothing\varnothing
7\varnothing N2=46:GOSUB 1ø\varnothing\varnothing
8\varnothing GOSUB 2øø\varnothing
9ø GOSUB 3øøø
10% END

```

Enter this much of the program along with the subroutines and run it.
(a) How many notes heard at line 10 ? \(\qquad\)
(b) Does line 20 change the sound?
(c) Which line causes a second note to be heard?
(a) Only one, the background note (183).
(b) The background note changes to 137 .
(c) Line 60 (also 2 notes at 70,80,90).
53. Replace line 100 and continue as below.
\begin{tabular}{|c|c|c|c|c|}
\hline 100 & \(\mathrm{N} 1=48: \mathrm{N} 2=41\) : & GOSUB & \(1 \varnothing 0\). & Voice 1 and 2 on \\
\hline 118 & N1=46:N2=36: & GOSUB & \(2 \varnothing 0 \varnothing\) & Change notes \\
\hline 120 & N1=41:N2=34: & Gosub & 3000 & Change again \\
\hline 130 & N1=36:N2=31: & gosub & 1000 & and again \\
\hline 140 & GOSUB \(2 \varnothing 0 \varnothing\) & & & Change only background \\
\hline 150 & GOSUB 3øø日 & & & Change background again \\
\hline 160 & N1=48: \(\mathrm{N}^{2}=41\) : & GOSUB & 1000 & Change all three notes \\
\hline 178 & GOSUB 2øø日 & & & Change only background \\
\hline 188 & GOSUB 3000 & & & Change background again \\
\hline 198 & END & & & \\
\hline
\end{tabular}

Now run the program again.
(a) How many notes caused by line 100 ?
(b) Do all the lines \(100-180\) play three notes? \(\qquad\)
(a) 3
(b) yes
54. The next section continues in the same manner except for the last three lines.280-320.
```

19\emptyset N1=46:N2=36:GOSUB 1\varnothing\varnothing\varnothing
2ø\emptyset GOSUB 2ø\emptyset\emptyset
210N1=48: GOSUB 3ø\varnothing\emptyset
22\emptysetN1=54:N2=34: GOSUB 1\varnothing\varnothing\varnothing
23\varnothingN1=61:N2=36: GOSUB 20\varnothing\varnothing
24\varnothingN1=69:N2=41:GOSUB 3\varnothing\varnothing\emptyset
25\emptyset N1=73:N2=46: GOSUB 1\varnothing\varnothing\emptyset
26\varnothing GOSUB 2øø\emptyset
27\varnothingN1=69:N2=54: GOSUB 3ø\varnothing\varnothing
28\varnothing SOUND \varnothing,183,1\varnothing,8: This time we can't
29\varnothing SOUND 1,82,1\varnothing,8 use any of our three
3ø\varnothing SOUND 2,69,1\varnothing,8
31\varnothing SOUND 3,61,1\varnothing,8
32\emptyset FOR W=1 TO 5\varnothing:NEXT W
330 END
This time we can't use any of our three subroutines, so we do it in the main program.

```
(a) How many voices are heard during the execution of line 320 ? \(\qquad\)
(b) How does the time delay compare with that of the three subroutines?
(a) 4
(b) twice as long (FOR W \(=1\) TO 50)
55. Here is the final portion of the program.
```

33\varnothingN1=61:N2=\varnothing:N3-\varnothing:GOSUB 3\varnothing\varnothing\varnothing turn off voices 2 and 3
34ø N1=73:N2=46:GOSUB 10øø
350 GOSUB 2øøø
36\varnothingN1=46:N2=\varnothing:GOSUE 3\varnothing\varnothing\varnothing
37\varnothingN1=61:N2=41:GOSUB 1ø\varnothing\varnothing
380 N1=46:N2=36:GOSUB 20øø
390 N1=41:N2=34:GOSUB 3\varnothing日\varnothing
40\varnothingN1=36:N2=31:GOSUB 1øøø
410 GOSUB 2øø\varnothing
42ø N1=46:GOSUB 3\varnothingø\varnothing
430 N1=48:N2=41:GOSUB 10ø0
440 GOSUB 2000
450 N1=\varnothing:N2=36:GOSUB 3\varnothingø\varnothing
460 N1=54:N2=34:GOSUB 1øø|
470 GOSUB 2000
48\varnothingN1=\varnothing:GOSUB 3\varnothingø\varnothing
49ø N1=61:N2=34:GOSUB 1øø\varnothing
50% N2=36:GOSUB 2øø\varnothing
510 N1=69:N2-41:GOSUB 30ø\varnothing
52ø N1=73:N2=61:GOSUB 1|||
530 N2=46:GOSUB 20ø0
540 N1=82:N2=61:GOSUB 3\varnothing\varnothing\varnothing
55ø SOUND ø,183,1\varnothing,8
56% SOUND 1,92,1\varnothing,8
570 SOUND 2,46,10,8
580 FOR W=1 TO 75: NEXT W
59% END

```
(a) The last tone played contained how many notes?
(b) How did the duration of the last tone compare with that of each of the subroutines?
(a) 3
(b) three times as long

\section*{SELF-TEST}

Congratulations!!! You covered a lot of ground in Chapter Ten. We have given you some fundamentals which you can use to build your understanding of the color graphics and sound capabilities of your ATARI computer. Use this self-test to demonstrate your new knowledge.
1. There are eight screen modes provided for mixing graphics and text in your ATARI computer. They are numbered from 0-7. In previous chapters all programs were printed in a pure text mode.
(a) What graphics statement is used to provide pure text?
\(1 \varnothing\) \(\qquad\)
(b) Give a mixed text-graphics mode with approximately \(160 \times 80\) graphics positions.
\(1 \varnothing\) \(\qquad\)
2. Shade in the rectangle for the points that would be plotted by the statement:
2. PLOT 4,1

3. Complete this program so that it draws a vertical line from the top of the screen at the left side to the text window at the extreme right side of the screen.
```

1\varnothing GRAPHICS 4
2ø COLOR 1
30 PLOT
4@ DRAWTO

```
\(\qquad\)
4. Write a program, using graphics mode 6 , that will draw the largest possible rectangle in the graphics area. Also draw the diagonals of the rectangle as shown below.

5. Use the following program and your computer to answer questions 5 (a), (b), and (c).
```

1\varnothing GR. 3
2ø COLOR 1
3\varnothing FOR M = \varnothing TO 4 STEP 2
4\varnothing FOR N = Ø TO 15
50 SETCOLOR M,N,2
60 PLOT 2,1\varnothing: DRAWTO 12,1\varnothing
70 FOR W = 1 TO 200: NEXT W
8\varnothing NEXT N
9\varnothing NEXT M

```

Fill in the blanks with the words BAR, TEXT WINDOW, or BACKGROUND.
(a) When the value of M is 0 , what changes color? \(\qquad\)
(b) When the value of M is 2 , what changes color? \(\qquad\)
(c) When the value of M is 4 , what changes color? \(\qquad\)
6. If the following program is run, describe what would happen on the video screen.
```

1\varnothing GR. 3
20 COLOR 1
3\varnothing FOR N = \varnothing TO 15
4\varnothing SETCOLOR Ø,N+3,2
5\emptyset PLOT 2,5: DRAWTO 2,1\varnothing
60 FOR W = 1 TO 2ø\varnothing: NEXT W
7@ SETCOLOR 4,N,2
8\emptyset FOR W = 1 TO 2øø: NEXT W
90 NEXT N

```
7. Write a program to fill the plotting area for graphics mode 3 with alternate points (that is, 0,\(0 ; 0,2 ; 0,4 \ldots 2,0 ; 2,2 \ldots\). . Use nested FOR-NEXT loops. Choose your favorite colors.
8. Using the SOUND statement:
(a) How many different voices may be played at one time? \(\qquad\)
(b) Loudness levels may be set to any integer in the range of
\(\qquad\) to \(\qquad\)
(c) The note variable may range from \(\qquad\) to \(\qquad\) .
9. In the following program, the SOUND statement causes a note to be played. How long will it stay on? \(\qquad\)
```

10 INPUT N
2ø SOUND \varnothing,97,1\varnothing,8
3\varnothing GOTO 1\varnothing

```
10. Using the table in frame 42, write a program to play a one octave scale (C to C) with no sharps.
11. Given the program:
```

1\varnothingN}N=36:N1=122: GOSUB 10\varnothing\varnothing
2ø Nø=32:N1=1ø9: GOSUB 2øø\varnothing
3\varnothing END

```
write the subroutines so they play the notes. Subroutine 1000 should hold the notes for a count of 50 and subroutine 2000 for a count of 100 .

\section*{Answers to Self-Test}
1. (a) \(1 \varnothing\) GRAPHICS \(\varnothing\) (frame 4)
(b) \(1 \varnothing\) GRAPHICS 6 or \(1 \varnothing\) GRAPHICS 7 (frame 5)
2. 20 PLOT 4,1 would color the shaded rectangle in the fifth column and second row.

3. \(3 \varnothing\) PLOT \(\varnothing, \varnothing\)

48 DRAWTO 78,39
4. 10 GRAPHICS 6
\(2 \varnothing\) COLOR 1
\(3 \varnothing\) SETCOLOR \(\varnothing, 12,2\)
\(4 \varnothing\) PLOT \(\varnothing, \varnothing\)
\(5 \varnothing\) DRAWTO 157, \(\varnothing\)
6ø DRAWTO 157,79
\(7 \varnothing\) DRAWTO \(\varnothing, 79\)
8』 DRAWTO \(\varnothing, \varnothing\)
9ø DRAWTO 157,79
\(1 \varnothing \varnothing\) PLOT Ø, 79
\(11 \varnothing\) DRAWTO 157, \(\varnothing\)
(Your setcolor values may differ.)
Lines 50-110 may be different for your program. As long as your rectangle looks like the sketch, it's OK.
(frames 5,7,18,20)
5. (a) BAR (frames 23,26 )
(b) TEXT WINDOW (frames 24,26 )
(c) BACKGROUND (frames 25,26 )
6. The color BAR and the BACKGROUND both change color. (frames 23-26)
7. Our program: 10 GRAPHICS 3 \(2 \varnothing\) COLOR 1 \(3 \varnothing\) SETCOLOR \(\varnothing, 2,2\) \(4 \varnothing\) FOR \(N=\varnothing\) TO 39 STEP 2 \(5 \emptyset\) FOR \(M=\varnothing\) TO 19 STEP 2 60 PLOT N,M \(7 \varnothing\) NEXT M 8ø NEXT N
(frames 5,9,23)
8. (a) 4 (frame 47)
(b) 0 to 15 (frame 37)
(c) 0 to 255 (frame 41)
9. Until a new note is INPUT. (frame 38)
10. Yours should be similar to this:
```

1\varnothing FOR A = 1 TO 8
2ø READ N
3\varnothing SOUND }\varnothing,N,1\varnothing,
40 FOR W = 1 TO 2\varnothing\varnothing: NEXT W
50 NEXT A
60 DATA 122,1ø9,97,92
70 DATA 82,73,65,61

```
lines 60 and 70 might also be:
```

60 DATA 61,54,48,46
70 DATA 41,36,32,31

```
(frame 42)
11. \(1 \varnothing \varnothing \varnothing\) SOUND \(\varnothing, N \varnothing, 1 \varnothing, 8\)
\(1 \varnothing 1 \varnothing\) SOUND \(1, N 1,1 \varnothing, 8\)
\(1 \varnothing 20\) FOR \(W=1\) TO 50: NEXT \(W\)
1030 RETURN
\(2 \varnothing \varnothing \varnothing\) SOUND \(\varnothing, N \varnothing, 1 \varnothing, 8\)
\(2 \varnothing 1 \varnothing\) SOUND \(1, N 1,1 \varnothing, 8\)
\(2 \varnothing 2 \varnothing\) FOR \(W=1\) TO \(1 \varnothing 0:\) NEXT W
2030 RETURN

\section*{Final Self-Test}

Now that you're done with the book, try this final examination to test all your skills. The answers follow the test. Use separate paper for your programs and calculations.
1. STARS is a number guessing game that was first published in People's Computer Company newspaper. It's fun to use with players of all ages and you should find it challenging to program as well.

Here are the rules typed by the computer. You don't have to include them in your program.
"I will think of a whole number from 1 to 100 . Try to guess my number. After you guess my number, I will type one or more stars (*). The closer you are to my number, the more stars I will type. One star ( \({ }^{*}\) ) means you are far away from my number. Seven stars ( \({ }^{* * * * * * *) ~ m e a n s ~ y o u ~ a r e ~}\) very, very close to my number!!"

Logic: If the guess is 64 or more away, one star; 32-63 away, two stars; 16-31 away, 3 stars; \(8-15\) away, 4 stars; 4-7 away, 5 stars) 2-3 away, 6 stars; 1 away, 7 stars. You will need to use the absolute value function, something new to you but easy to use.

Clues: \(\operatorname{ABS}(1 \varnothing)=1 \varnothing\)
ABS \((-1 \varnothing)=1 \varnothing\)
IF \(\operatorname{ABS}(X-Y)=1 \varnothing\) THEN \(1 \varnothing \varnothing\)
```

RUN
ENTER YOUR GUESS? 1\varnothing
**
ENTER YOUR GUESS? }2
***
ENTER YOUR GUESS? 5\emptyset
******
ENTER YOUR GUESS? 6\varnothing
****
ENTER YOUR GUESS? }4
******
ENTER YOUR GUESS? 42
*****
ENTER YOUR GUESS? 47
*******
ENTER YOUR GUESS? 48
WINNER!!!

```
2. You may have used matrix commands on some other computer. (Matrix is just another name for array.) Versions of BASIC for home computers generally do not include matrix commands. However, they are easy to simulate. Try it.

You have two 5 by 3 arrays called A and B, filled with small numbers that are read into the elements or boxes in the array from DATA statements. Write a program to add the contents of each element in array A to the corresponding element in array B, and place the results in the proper place in a third array, C.
A \begin{tabular}{|c|c|c|}
\hline 7 & 8 & 9 \\
\hline 3 & 4 & 1 \\
\hline 6 & 8 & 2 \\
\hline 1 & 4 & 1 \\
\hline 8 & 10 & 2 \\
\hline
\end{tabular}
B
\begin{tabular}{|c|c|c|}
\hline 3 & 6 & 8 \\
\hline 2 & 4 & 7 \\
\hline 1 & 3 & 1 \\
\hline 8 & 4 & 9 \\
\hline 6 & 6 & 6 \\
\hline
\end{tabular}
C
\begin{tabular}{|r|r|r|}
\hline 10 & 14 & 17 \\
\hline 5 & 8 & 8 \\
\hline 7 & 11 & 3 \\
\hline 9 & 8 & 10 \\
\hline 14 & 16 & 8 \\
\hline
\end{tabular}

Example: \(\quad A(1,1)+B(1,1)=C(1,1)\)
\[
\mathrm{A}(1,2)+\mathrm{B}(1,2)=\mathrm{C}(1,2) \text { etc. }
\]
```

RUN
A ARRAY CONTENTS

| 7 | 8 | 9 |
| :--- | :--- | :--- |
| 3 | 4 | 1 |
| 6 | 8 | 2 |
| 1 | 4 | 1 |
| 8 | 10 | 2 |

B ARRAY CONTENTS

| 3 | 6 | 8 |
| :--- | :--- | :--- |
| 2 | 4 | 7 |
| 1 | 3 | 1 |
| 8 | 4 | 9 |
| 6 | 6 | 6 |

C ARRAY CONTENTS

| $1 \varnothing$ | 14 | 17 |
| :--- | :--- | :--- |
| 5 | 8 | 8 |
| 7 | 11 | 3 |
| 9 | 8 | $1 \varnothing$ |
| 14 | 16 | 8 |

```
3. Your child plans to set up a weekend sidewalk stand selling "junk" from around the house (also known as a garage sale). Your youngster has no trouble finding merchandise and no trouble pricing it. But he or she really doesn't understand the money system and is worried about making change when people buy these "goods."

Write a program to allow the child to enter the amount of the sale and the amount of money received, and have the computer then print exactly how much and what kind of change to give back. The RUN is shown below.
```

RUN
ENTER TOTAL SALES AMOUNT? . 35
ENTER AMOUNT RECEIVED? 1.\varnothing\emptyset
COIN CHANGE . }6
1 HALF DOLLAR
1 DIME
1 NICKEL
ENTER TOTAL SALES AMOUNT? 3.45
ENTER AMOUNT RECEIVED? 20. }
BILL CHANGE IS 16
1 \$1\varnothing BILL
1 \$ 5 BILL
1 \$1 BILL
COIN CHANGE . }5
1 HALF DOLLAR
1 NICKEL

```

Warning: Some versions of BASIC will round off numbers in peculiar ways (deep inside the computer) because of the way the electronics perform arithmetic. So beware! 4.9999 pennies is no fair. Write your program to avoid this kind of problem by checking for integer values for change that includes pennies.
4. Write a program to perform conversions from selected U.S. standard measures to their metric equivalents and vice versa. Set up your program so that the user can select conversions as shown in the RUN below.
```

RUN
DO YOU WANT CONVERSIONS FOR
(1) METRIC TO U.S. STANDARD MEASURES
(2) U.S. STANDARD MEASURES TO METRIC
TYPE 1 OR 2? 1
WANT LIST OF CONVERSIONS (Y OR N)? Y
SELECT CONVERSION FROM THIS LIST:
(1) CENTIMETERS TO INCHES
(2) METERS TO FEET
(3) KILOMETERS TO MILES
(4) KILOGRAMS TO POUNDS
(5) GRAMS TO OUNCES
(6) LITERS TO QUARTS
(7) DEGREES CELSIIUS TO DEGREES FAHRENHEIT
ENTER NUMBER OF CONVERSION DESIRED? 5
HOW MANY GRAMS? 1\varnothing
1\varnothing GRAMS = . 35 OUNCES
DO YOU WANT CONVERSIONS FOR
(1) METRIC TO U.S. STANDARD MEASURES
(2) U.S. STANDARD MEASURES TO METRIC
TYPE 1 OR 2? 2
WANT LIST OF CONVERSIONS (Y OR N)? Y
SELECT CONVERSION FROM THIS LIST:
(1) INCHES TO CENTIMETERS
(2) FEET TO METERS
(3) MILES TO KILOMETERS
(4) POUNDS TO KILOGRAMS
(5) OUNCES TO GRAMS
(6) QUARTS TO LITERS
(7) DEGREES FAHRENHEIT TO DEGREES CELSIUS
ENTER NUMBER OF CONVERSION DESIRED? 3
HOW MANY MILES? 2
2 MILES = 3.218 KILOMETERS
DO YOU WANT CONVERSIONS FOR
(1) METRIC TO U.S. STANDARD MEASURES
(2) U.S. STANDARD MEASURES TO METRIC
TYPE 1 OR 2? 1
DO YOU WANT THE LIST OF CONVERSIONS (Y OR N)? N<<< Since the list
ENTER NUMBER OF CONVERSION DESIRED? 1
HOW MANY CENTIMETERS? 5\varnothing
5ø CENTIMETERS = 19.5 INCHES
DO YOU WANT CONVERSIONS FOR
was printed
above, no need
to repeat it
again.

```

And so on.

We suggest the following manner of organizing the program, making extensive use of subroutines. The main program is shown at the top; here the user selects which type of conversion is to be made. The program then branches to subroutines which list the specific conversions. From these subroutines, the program GOSUBs again, to one of fourteen sub-subroutines (seven for each "direction" of conversion).
```

DO YOU WANT CONVERSIONS FOR
(1) METRIC TO U.S. STANDARD MEASURES
(2) U.S. STANDARD MEASURES TO METRIC
TYPE 1 OR 2? 2

```


From any one of these subroutines, return to the subroutine that sent it, and from there, return immediately to the main program to start over again.

Here are the conversion values to include in the program.
\[
\begin{aligned}
& \text { Metric to } U . S . \text { Standard } \\
& 1 \text { centimeter }=.39 \text { inches } \\
& 1 \text { meter }=3.28 \text { feet } \\
& 1 \text { kilometer }=.62 \text { miles } \\
& 1 \text { kilogram }=2.2 \text { pounds } \\
& 1 \text { gram }=.035 \text { ounces } \\
& 1 \text { liter }=1.0567 \text { quarts } \\
& \mathrm{C}^{\circ}=5 / 9\left(\mathrm{~F}^{\circ}-32\right)
\end{aligned}
\]
U.S. Standard to Metric 1 inch \(=2.54 \mathrm{~cm}\)
\(1 \mathrm{ft} .=.3048\) meters 1 mile \(=1.609\) kilometers
1 pound \(=.45\) kilograms
1 quart \(=.946\) liters
\(\mathrm{F}^{\circ}=9 / 5 \mathrm{C}^{\circ}+32\)

\section*{Answers to Final Self-Test}
```

1. 1\varnothing REMARK***STARS GAME
2\varnothing LET N=INT(1@目RND(1))+1
3\varnothing PRINT "ENTER YOUR GUESS";:INPUT G
35 IF G=N THEN PRINT "WINNER!!!"": GOTO 2\emptyset
4% LET D=ABS (G-N)
5@ IF D>=64 THEN 17\varnothing
6\varnothing IF D>=32 THEN 16\varnothing
7\emptyset IF D>=16 THEN 150
8@ IF D>=8 THEN 14\varnothing
90 IF D>=4 THAN 130
100 IF D>=2 THAN 12ø
11\varnothing PRINT "*";
12\varnothing PRINT "*";
13@ PRINT "*";
14\varnothing PRINT "*";
15@ PRINT "*";
16@ PRINT "*";
17\varnothing PRINT "*": GOTO 3\varnothing
```
2.
```

1\varnothing REMARK***SIMULATION OF MATRIX ADDITION
15 REMARK INITIALIZE
2\emptyset DIM A(5,3), B(5,3),C(5,3)
25 REM LOAD A AND B ARRAY FROM DATA STATEMENTS. PRINT ARRAYS
27 PRINT "A ARRAY CONTENTS" : PRINT
30 FOR X=1 TO 5
35 FOR Y=1 TO 3
40 READ A(X,Y) : PRINT A(X,Y),
4 5 ~ N E X T ~ Y ~
5% PRINT
5 5 NEXT X : PRINT : PRINT
57 PRINT "B ARRAY CONTENTS" : PRINT
60 FOR X=1 TO 5
65 FOR Y=1 TO 3
7% READ B(X,Y) : PRINT B (X,Y),
75 NEXT Y
8% PRINT
8 5 NEXT X : PRINT : PRINT
90 REM ADD A + B INTO C
92 PRINT "C ARRAY CONTENTS" : PRINT
95 FOR X=1 TO }
1\varnothing\varnothing FOR Y=1 TO 3
1\varnothing5 LET C(X,Y)=A(X,Y)+B(X,Y) : PRINT C(X,Y),
110 NEXT Y
115 PRINT
12g NEXT X
13\varnothing REM DATA FOR A ARRAY
135 DATA 7, 8,9,3,4,1,6,8,2,1,4,1,8,-10,2
14\varnothing REM DATA FOR B ARRAY
145 DATA 3,6,8,2,4,7,1,3,1,8,4,9,6,6,6

```
3. 1ø REMARK*** COIN CHANGER
\(2 \varnothing\) PRINT "ENTER TOTAL SALES AMOUNT"; :INPUT T
\(3 \varnothing\) PRINT "ENTER AMOUNT RECEIVED";:INPUT M
\(4 \varnothing\) IF M<T THEN PRINT "NOT ENOUGH MONEY RECEIVED": GOTO \(2 \varnothing\)
5ø IF M=T THEN PRINT "EXACT CHANGE, NO CHANGE REQUIRED":PRINT:GOTO \(2 \boldsymbol{\square}\)
\(6 \varnothing\) LET C=M-T:IF C<1.øø THEN \(15 \varnothing\)
65 PRINT
\(7 \varnothing\) LET \(B=C-(C-I N T(C)): P R I N T\) "BILL CHANGE IS "; B
75 LET C=C-B
\(8 \varnothing\) LET B \(1=I N T(B / 2 \varnothing): I F B 1=\varnothing\) THEN \(1 \varnothing \varnothing\)
85 PRINT B1; " \(\$ 2 \varnothing\) BILL"
\(9 \varnothing\) LET \(B=B-(B 1 * 2 \varnothing)\)
\(1 \varnothing \varnothing\) LET B2=INT(B/1ø):IF B2= \(\varnothing\) THEN \(12 \varnothing\)
105 PRINT B2; " \(\$ 1 \varnothing\) BILL"
\(11 \varnothing\) LET B=B-(B2*1ø)
\(12 \varnothing\) LET B3=INT(B/5):IF B3= \(\varnothing\) THEN \(14 \varnothing\)
125 PRINT B3; " \(\$ 5\) BILL"
\(13 \varnothing\) LET B=B-(B3*5)
140 IF B<1 THEN 15ø
145 PRINT B; " \$1 BILL":PRINT
\(15 \varnothing\) LET C=INT( \((C+. \varnothing \varnothing 5) * 1 \varnothing \varnothing)\)
152 LET \(\mathrm{C}=\mathrm{INT}(\mathrm{C})\)
155 PRINT "COIN CHANGE ": C/1øø:PRINT
160 IF C \(<5 \varnothing\) THEN \(18 \varnothing\)
\(17 \varnothing\) PRINT " 1 HALF DOLLAR": LET \(C=C-5 \varnothing\)
180 IF C<25 THEN 200
\(19 \varnothing\) PRINT "1 QUARTER":LET C=C-25
\(2 \varnothing \varnothing\) LET C=INT (C/1ø):IF \(D=\varnothing\) THEN \(22 \varnothing\)
\(21 \varnothing\) PRINT D; " DIME":LET C=C-(D* \(1 \varnothing\) )
22. LET \(N=1 N T(C / 5):\) IF \(N=\varnothing\) THEN \(24 \varnothing\)
\(23 \varnothing\) PRINT N; "NICKEL": LET C=C-(N*5)
\(24 \varnothing\) IF C<1 THEN PRINT:GOTO \(2 \varnothing\)
\(25 \varnothing\) PRINT INT(C); " PENNY":PRINT:GOTO \(2 \varnothing\)
4. \(1 \varnothing \varnothing\) REM***SELECTED MEASUREMENT CONVERSIONS
\(11 \varnothing\) PRINT "DO YOU WANT CONVERSIONS FOR"
\(12 \emptyset\) PRINT "(1) METRIC TO U.S. STANDARD MEASURES"
\(13 \varnothing\) PRINT "(2) U.S. STANDARD MEASURES TO METRIC"
\(14 \varnothing\) PRINT "TYPE 1 OR 2"; : INPUT N
\(15 \varnothing\) ON N GOSUB \(1 \varnothing \varnothing \varnothing, 11 \varnothing \varnothing\)
\(16 \varnothing\) GOTO \(11 \varnothing\)
\(1 \varnothing \varnothing \varnothing\) REM***USER SELECTS DESIRED METRIC TO U.S. CONVERSION
\(1 \not ⿴ 1 \varnothing\) PRINT "WANT LIST OF CONVERSIONS (Y OR N)"; : INPUT A\$
\(1 ø 2 \varnothing\) IF \(A \$=" N\) " THEN \(1 \varnothing 4 \varnothing\)
\(1 \varnothing 3 \varnothing\) PRINT "SELECT CONVERSION FROM THIS LIST:"
\(1 ø 31\) PRINT "(1) CENTIMETERS TO INCHES"
\(1 \not ⿴ 32\) PRINT "(2) METERS TO FEET"
\(1 \not 033\) PRINT "(3) KILOMETERS TO MILES"
1034 PRINT "(4) KILOGRAMS TO POUNDS"
1035 PRINT "(5) GRAMS TO OUNCES"
\(1 \varnothing 36\) PRINT "(6) LITERS TO QUARTS"
\(1 \not 037\) PRINT "(7) DEGREES CELSIUS TO DEGREES FAHRENHEIT"
\(1 \varnothing 4 \varnothing\) PRINT "ENTER NUMBER OF CONVERSION DESIRED"; : INPUT M
1050 ON M GOSUB \(210 \varnothing, 220 \varnothing, 230 \varnothing, 24 \varnothing \varnothing, 250 \varnothing, 2600,27 \varnothing \varnothing\)
\(1 \varnothing 6 \varnothing\) RETURN
\(11 \varnothing \varnothing\) REM***USER SELECTS DESIRED U.S. TO METRIC CONVERSION
\(111 \varnothing\) PRINT "WANT LIST OF CONVERSIONS (Y OR N)"; : INPUT A\$
1120 IF A \(\$=\) " \(N\) " THEN \(114 \varnothing\)
\(113 \varnothing\) PRINT "SELECT CONVERSION FROM THIS LIST:"
1131 PRINT "(1) INCHES TO CENTIMETERS"
1132 PRINT "(2) FEET TO METERS"
1133 PRINT "(3) MILES TO KILOMETERS"
1134 PRINT "(4) POUNDS TO KILOGRAMS"
1135 PRINT "(5) OUNCES TO GRAMS"
1136 PRINT "(6) QUARTS TO LITERS"
1137 PRINT "(7) DEGREES FAHRENHEIT TO DEGREES CELSIUS"
\(114 \varnothing\) PRINT "ENTER NUMBER OF CONVERSION DESIRED"; : INPUT \(S\)
\(115 \varnothing\) ON S GOSUB \(31 \varnothing \varnothing, 32 \varnothing \varnothing, 33 \varnothing \varnothing, 34 \varnothing \varnothing, 35 \varnothing \varnothing, 36 \varnothing \varnothing, 37 \varnothing \varnothing\)
\(116 \varnothing\) RETURN
\(21 \varnothing \varnothing\) REM***CM TO INCHES
\(211 \varnothing\) PRINT "HOW MANY CENTIMETERS"; : INPUT \(C\)
\(212 \varnothing\) PRINT C; "CENTIMETERS ="; C*.39; "INCHES"
2130 PRINT: RETURN
22øø REM***METERS TO FEET
\(221 \varnothing\) PRINT "HOW MANY METERS"; : INPUT M
222ø PRINT M; "METERS ="; M*3.28; "FEET"
\(223 \varnothing\) PRINT : RETURN
\(23 \varnothing \varnothing\) REM***KM TO MILES
2310 PRINT "HOW MANY KILOMETERS"; : INPUT K
232ø PRINT K; "KILOMETERS ="; K*. 62; "MILES"
2330 PRINT : RETURN
2400 REM***KG TO POUNDS
\(241 \varnothing\) PRINT "HOW MANY KILOGRAMS"; : INPUT K
\(242 \varnothing\) PRINT K; "KILOGRAMS ="; K*2.2;"POUNDS"
\(243 \varnothing\) PRINT : RETURN
2500 REM***GRAMS TO OUNCES
\(251 \varnothing\) PRINT "HOW MANY GRAMS"; : INPUT G
\(252 \varnothing\) PRINT G; "GRAMS ="; G*.ø35; "OUNCES"
2530 PRINT : RETURN
```

26øø REM***LITERS TO QUARTS
2610 PRINT "HOW MANY LITERS"; : INPUT L
262ø PRINT L; "LITERS ="; L*1.ø567; "QUARTS"
2630 PRINT : RETURN
270\varnothing REM***DEGREES C TO DEGREES F
271ø PRINT "HOW MANY DEGREES CELSIUS"; : INPUT D
272\emptyset PRINT D; "DEGREES CELSIUS ="; 9*D/5+32; "DEGREES FAHRENHEIT"
2730 PRINT : RETURN
31\varnothing\varnothing REM***INCHES TO CM
311\varnothing PRINT "HOW MANY INCHES"; : INPUT I
312\varnothing PRINT I; "INCHES ="; I*2.54; "CENTIMETERS"
3130 PRINT : RETURN
32øø REM***FEET TO METERS
321\varnothing PRINT "HOW MANY FEET"; : INPUT F
3220 PRINT F; "FEET ="; F*.3048; "METERS"
3230 PRINT : RETURN
330\varnothing REM***MILES TO KM
331\varnothing PRINT "HOW MANY MILES"; : INPUT M
3320 PRINT M; "MILES ="; M*1.609; "KILOMETERS"
3330 PRINT : RETURN
3400 REM***POUNDS TO KG
341\varnothing PRINT "HOW MANY POUNDS"; : INPUT P
342\varnothing PRINT P; "POUNDS ='; P*.45; "KILOGRAMS"
3430 PRINT : RETURN
350\varnothing REM***OUNCES TO GRAMS
351\varnothing PRINT "HOW MANY OUNCES"; : INPUT O
3520 PRINT O; "OUNCES ='"; 0*28.35; "GRAMS"
3530 PRINT : RETURN
36ø\varnothing REM***QUARTS TO LITERS
361ø PRINT "HOW MANY QUARTS"; : INPUT Q
362\varnothing PRINT Q; "QUARTS ="; Q*.946; "LITERS"
363\varnothing PRINT : RETURN
37\varnothing\varnothing REM***DEGREES F TO DEGREES C
371\varnothing PRINT "HOW MANY DEGREES FAHRENHEIT"; : INPUT D
372\varnothing PRINT D; "DEGREES FAHRENHEIT ="; 5/9*(D-32); "DEGREES CELSIUS"
3730 PRINT : RETURN

```

\section*{Appendixes}

\section*{BASIC FUNCTIONS}

This Appendix describes some of the more common and useful functions included in most versions of BASIC used on personal computers. It is by no means an exhaustive list, and the functions may perform differently on the computer you use. Check the reference manual for your computer system for the complete list of functions available in your version of BASIC.

\section*{Arithmetic Functions}
(In the following, "exp" stands for any BASIC expression, variable, or number.)
\(\mathrm{ABS}(\exp )\) : Gives the absolute value of the expresion, i.e., \(\mathrm{ABS}(\mathrm{A})=\mathrm{A}\) if \(\mathrm{A}>=0\), \(\operatorname{ABS}(A)=-A\) if \(A<0\).
Example: IF ABS(X-G)>=64 THEN PRINT "**"
EXP(exp): Computes the exponential function, base e, where \(e=2.71828\). . . Usually there is an upper limit on the value of the variable. In BASIC, the value in the parentheses must be less than 87.3365.
Examples: \(\mathrm{B}=\mathrm{EXP}(\mathrm{X})\)
\[
\mathrm{Y}=\mathrm{C}^{*} \operatorname{EXP}\left(-\mathrm{A}^{*} \mathrm{~T}\right)
\]

FRE(0): Used to determine how much space is left in the computer's memory that is not being used by BASIC or the program stored in memory. Enter it in a print statement, with zero in the parentheses, and the number of unused bytes is given.
Example: PRINT FRE(0)
See also FRE(string variable) under String Functions.

INT(exp): Computes the greatest integer less than or equal to exp. Notice that \(\operatorname{INT}(3.14)=3\), but \(\operatorname{INT}(-3.14)=-4\). You may wish to check the reference manual for your version of BASIC for the similar function FIX.

LOG(exp): Gives the natural logarithm, base e, of exp.
Example: \(\mathrm{D}=\mathrm{LOG}(1+\mathrm{X} \uparrow 2)\)
RND(parameter): Generates a random number between 0 and 1 with control by the parameter value. For example, in BASIC, any positive value in the parentheses gives a new random number each time. A zero in the parentheses gives the same random number as was last generated by a RND function. Each different negative number (including fractions) gives a different random number, but the same random number is always given for the same negative value in the parentheses. The RND function may not work as described above for other versions of BASIC, so check your reference manual for details.

SGN(exp): Gives a 1 if the expression evaluates to a positive value ( \(>0\) ); gives a 0 if the expression evaluates to zero \((=0)\); gives \(\mathrm{a}-1\) if the expression evaluates to a negative value \((<0)\).
Example: ON SGN(X) + 2 GOTO 100, 200, 300
If X is negative, the above statement will branch to line 100 ; If \(\mathrm{X}=0\), it will branch to line 200; if X is positive, it will branch to line 300 .

SQR(exp): Gives the positive square root of exp. Expression in parentheses must be zero or a positive value (no negative values).

\section*{Trigonometric Functions}

SIN(exp), COS(exp), TAN(exp), ATN(exp): The SIN, COS, and TAN functions give the sine, cosine, or tangent of exp, where exp is assumed to be given in radians. ATN computes the principal value of the arctangent, in radians. The value of \(\operatorname{ATN}(\exp )\) will be in the range: \(-\pi / 2<\mathrm{ATN}(\exp )<\pi / 2\).

\section*{String Functions}

ASC(string): Gives the ASCII code numeric value for the first character in a string.
Example: PRINT ASC(B\$)
CHR\$(exp): Converts a number to the corresponding ASCII character.
Example: The ASCII code number 7 rings the bell on a teletypewriter or causes a beep on many CRT's. To ring the bell, use CHR\$(7) in a PRINT statement, like this: PRINT CHR\$(7)

FRE(string variable: Gives the number of free (unused) bytes in the memory's reserved string space. See also FRE function under Arithmetic Functions.

LEN(string): Gives the number of characters included in the string; spaces are always counted as characters.
Examples: FOR K-1 TO LEN(X\$)
STR\$(exp): Converts a numeric expression to a string. The minus sign in a negative value is included in the string, and the leading space for the assumed " + " in a positive value is included in the string.
Example: B\$=STR\$(X*Y)
VAL(string): Converts a string representation of a number to a numeric value.
String must be numeric character.
Example: X\$= '33.3"'
\(\mathrm{X}=\mathrm{VAL}(\mathrm{X} \$)\)

\section*{ASCII CHARACTER CODES}
\begin{tabular}{|c|c|c|c|c|c|}
\hline Decimal & Character & Decimal & Character & Decimal & Character \\
\hline 000 & NUL & 043 & + & 086 & V \\
\hline 001 & SO11 & 044 & ' & 087 & W \\
\hline 002 & STX & 045 & - & 088 & X \\
\hline 003 & ETX & 046 & . & 089 & Y \\
\hline 004 & EOT & 047 & 1 & 090 & Z \\
\hline 005 & ENQ & 048 & 0 & 091 & [ \\
\hline 006 & ACK & 049 & 1 & 092 & 1 \\
\hline 007 & BEL & 050 & 2 & 093 & ] \\
\hline 008 & BS & 051 & 3 & 094 & \(\uparrow\) \\
\hline 009 & HT & 052 & 4 & 095 & \(\leftarrow\) \\
\hline 010 & LF & 053 & 5 & 096 & , \\
\hline 011 & VT & 054 & 6 & 097 & a \\
\hline 012 & FF & 055 & 7 & 098 & b \\
\hline 013 & CR & 056 & 8 & 099 & c \\
\hline 014 & SO & 057 & 9 & 100 & d \\
\hline 015 & SI & 058 & : & 101 & e \\
\hline 016 & DLE & 059 & ; & 102 & f \\
\hline 017 & DC1 & 060 & < & 103 & g \\
\hline 018 & DC2 & 061 & \(=\) & 104 & h \\
\hline 019 & DC3 & 062 & > & 105 & - \\
\hline 020 & DC4 & 063 & ? & 106 & j \\
\hline 021 & NAK & 064 & @ & 107 & k \\
\hline 022 & SYN & 065 & A & 108 & 1 \\
\hline 023 & ETB & 066 & B & 109 & m \\
\hline 02\% & CAN & 067 & C & 110 & n \\
\hline 025 & EM & 068 & D & 111 & o \\
\hline 026 & SUB & 069 & E & 112 & p \\
\hline 027 & ESCAPE & 070 & F & 113 & q \\
\hline 028 & FS & 071 & G & 114 & r \\
\hline 029 & GS & 072 & H & 115 & s \\
\hline 030 & RS & 073 & I & 116 & t \\
\hline 031 & US & 074 & J & 117 & u \\
\hline 032 & SPACE & 075 & K & 118 & v \\
\hline 033 & ! & 076 & L & 119 & w \\
\hline 034 & " & 077 & M & 120 & x \\
\hline 035 & \# & 078 & N & 121 & y \\
\hline 036 & \$ & 079 & O & 122 & z \\
\hline 037 & \% & 080 & P & 123 & \{ \\
\hline 038 & \& & 081 & Q & 124 & I \\
\hline 039 & , & 082 & R & 125 & \} \\
\hline 040 & ( & 083 & S & 126 & \(\sim\) \\
\hline 041 & ) & 084 & T & 127 & DEL \\
\hline 042 & * & 085 & U & & \\
\hline \multicolumn{2}{|l|}{LF = Line Feed FF} & rm Feed & \multicolumn{2}{|l|}{CR = Carriage Return} & DEL = Delete \\
\hline
\end{tabular}

\section*{ERROR MESSAGES}

Errors will cause a message of the form:
"ERROR xx at LINE nnnn."
The error number (' \(x x\) '' above) may be in the range 1 to 199.
ERRNUM 1 ; POWER NOT ON
ERRNUM 2 ; MEMORY FULL
ERRNUM 3 ; VALUE ERROR
ERRNUM 4 ; VARIABLE TABLE FULL (TOO MANY VARIABLES)
ERRNUM 5 ; STRING LENGTH ERROR
ERRNUM 6 ; READ OUT OF DATA
ERRNUM 7 ; VALUE NOT + INTEGER
ERRNUM 8 ; INPUT STMT ERROR
ERRNUM 9 ; ARRAY/STRING DIM ERROR
ERRNUM 10 ; ARG STACK OVERFLOW
ERRNUM 11 ; FLOATING POINT OVERFLOW
ERRNUM 12 ; LINE NOT FOUND (GOSUB/GOTO)
ERRNUM 13 ; NO MATCHING FOR
ERRNUM 14 ; LINE TOO LONG
ERRNUM 15 ; GOSUB/FOR LINE DELETED
ERRNUM 16 ; BAD RETURNS
ERRNUM 17 ; EXECUTION OF GARBAGE
ERRNUM 18 ; STRING DOES NOT START WITH VALID NUMBER
ERRNUM 19 ; LOAD PGM TOO BIG
ERRNUM 20 ; DEVICE NUMBER GRATER THAN 7
ERRNUM 21 ; NOT A LOAD FILE

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\section*{NOTES}

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[^0]:    *(The computer ignores everything following REM. See frame 39.)

